## Lesson 6.6 Extra Practice Answers

1. a) $f(x)=\sin x$ has been stretched vertically by a factor of 28 ;
$\mathrm{D}=\{x \in \mathbf{R}\} ; \mathbf{R}=\{y \in \mathbf{R} \mid-28 \leq y \leq 28\}$
b) $f(x)=\sin x$ has been compressed vertically by a factor of $\frac{3}{22}$ and reflected across the $x$-axis;
$\mathrm{D}=\{x \in \mathbf{R}\} ; \mathbf{R}=\left\{y \in \mathbf{R} \left\lvert\,-\frac{3}{22} \leq y \leq \frac{3}{22}\right.\right\}$
c) $f(x)=\sin x$ has been stretched vertically by a factor of 21.5 and reflected across the $x$-axis;
$\mathrm{D}=\{x \in \mathbf{R}\} ; \mathbf{R}=\{y \in \mathbf{R} \mid-21.5 \leq y \leq 21.5\}$
d) $f(x)=\sin x$ has been compressed vertically by a
factor of $\frac{1}{18} ; \mathrm{D}=\{x \in \mathbf{R}\}$;
$\mathrm{R}=\left\{y \in \mathbf{R} \left\lvert\,-\frac{1}{18} \leq y \leq \frac{1}{18}\right.\right\}$
e) $f(x)=\sin x$ has been stretched vertically by a factor of $33 ; \mathrm{D}=\{x \in \mathbf{R}\}$;
$\mathbf{R}=\{y \in \mathbf{R} \mid-33 \leq y \leq 33\}$
f) $f(x)=\sin x$ has been stretched vertically by a factor of $\frac{9}{8}$ and reflected across the $x$-axis;
$\mathrm{D}=\{x \in \mathbf{R}\} ; \mathbf{R}=\left\{y \in \mathbf{R} \left\lvert\,-\frac{9}{8} \leq y \leq \frac{9}{8}\right.\right\}$
2. a) $f(x)=-\frac{7}{8} \sin x$
b) $f(x)=23.5 \sin x$
c) $f(x)=\frac{2}{3} \sin x$
d) $f(x)=-26 \sin x$
e) $f(x)=-\frac{10}{11} \sin x$
f) $f(x)=60 \sin x$
3. a) $f(x)=-11 \sin x ; \mathrm{D}=\{x \in \mathbf{R}\}$;
$\mathrm{R}=\{y \in \mathbf{R} \mid-11 \leq y \leq 11\}$
b) $f(x)=\frac{1}{5} \sin x ; \mathrm{D}=\{x \in \mathbf{R}\}$;
$\mathrm{R}=\left\{y \in \mathbf{R} \left\lvert\,-\frac{1}{5} \leq y \leq \frac{1}{5}\right.\right\}$
c) $f(x)=60 \sin x ; \mathrm{D}=\{x \in \mathbf{R}\}$;
$\mathrm{R}=\{y \in \mathbf{R} \mid-60 \leq y \leq 60\}$
d) $f(x)=-\frac{3}{4} \sin x ; \mathrm{D}=\{x \in \mathbf{R}\}$;
$\mathbf{R}=\left\{y \in \mathbf{R} \left\lvert\,-\frac{3}{4} \leq y \leq \frac{3}{4}\right.\right\}$
4. a) amplitude: 20 ; period: $360^{\circ}$; equation of the axis:

$$
\begin{aligned}
& y=-3 ; \mathbf{D}=\{x \in \mathbf{R}\} ; \\
& \mathbf{R}=\{y \in \mathbf{R} \mid-23 \leq y \leq 17\}
\end{aligned}
$$

b) amplitude: $\frac{17}{21}$; period: $360^{\circ}$; equation of the axis:

$$
y=1 ; \mathrm{D}=\{x \in \mathbf{R}\} ;
$$

$$
\mathbf{R}=\left\{y \in \mathbf{R} \left\lvert\, \frac{4}{21} \leq y \leq 1 \frac{17}{21}\right.\right\}
$$

c) amplitude: 23 ; period: $360^{\circ}$; equation of the axis: $y=-7 ; \mathrm{D}=\{x \in \mathbf{R}\} ;$ $\mathbf{R}=\{y \in \mathbf{R} \mid-30 \leq y \leq 16\}$
d) amplitude: $\frac{1}{25}$; period: $360^{\circ}$; equation of the axis:

$$
y=-2 ; \mathrm{D}=\{x \in \mathbf{R}\} ;
$$

$\mathbf{R}=\left\{y \in \mathbf{R} \left\lvert\,-2 \frac{1}{25} \leq y \leq-1 \frac{24}{25}\right.\right\}$
e) amplitude: 4; period: $360^{\circ}$; equation of the axis:

$$
\begin{aligned}
& y=-75 ; \mathrm{D}=\{x \in \mathbf{R}\} ; \\
& \mathrm{R}=\{y \in \mathbf{R} \mid-79 \leq y \leq-71\}
\end{aligned}
$$

f) amplitude: $\frac{49}{50}$; period: $360^{\circ}$; equation of the axis:
$y=4 ; \mathrm{D}=\{x \in \mathbf{R}\} ;$
$\mathbf{R}=\left\{y \in \mathbf{R} \left\lvert\, 3 \frac{1}{50} \leq y \leq 4 \frac{49}{50}\right.\right\}$
5. a) Yes, the transformations have been applied in the correct order.
b) No, the transformations have not been applied in the correct order.
c) Yes, the transformations have been applied in the correct order.

