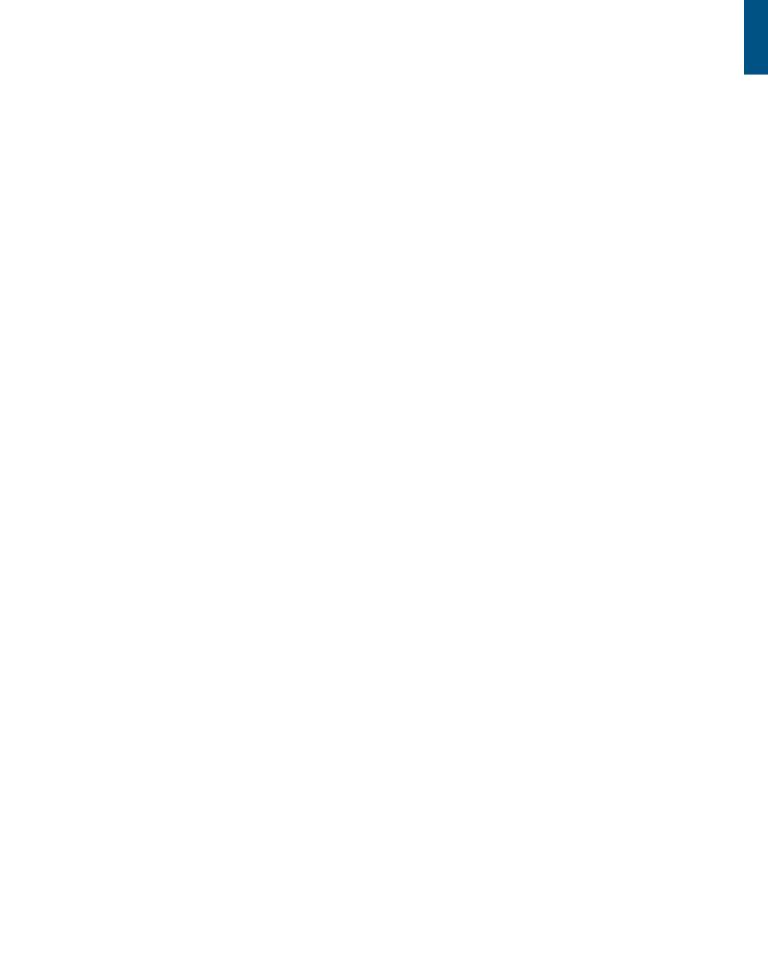
FUNCTIONS 11



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Table of Contents

| Chapter 1: Introduction to Functions | | 1 | 2.7 | Adding and Subtracting Rational | |
|--------------------------------------|---|-----|----------------------------------|---|-----|
| Getting Started | | 2 | | Expressions | 124 |
| 1.1 Relations and Functions | | 4 | Chapter Review | | 131 |
| | Curious Math | 13 | Cha | pter Self-Test | 134 |
| 1 2 | Function Notation | 14 | Cha | pter Task | 135 |
| | Exploring Properties of Parent Functions | 25 | | | |
| 1.4 | 1 0 1 | | Cha | pter 3: Quadratic Functions | 136 |
| | Function | 29 | Get | ting Started | 138 |
| Mid | -Chapter Review | 38 | 3.1 | Properties of Quadratic Functions | 140 |
| 1.5 | The Inverse Function and Its Properties | 41 | 3.2 | Determining Maximum and Minimum Values of a Quadratic Function | 148 |
| 1.6 | Exploring Transformations of Parent Functions | 50 | 3.3 | The Inverse of a Quadratic Function | 155 |
| 1.7 | Investigating Horizontal Stretches, | 30 | | Operations with Radicals | 163 |
| | Compressions, and Reflections | 52 | Mid | -Chapter Review | 169 |
| 1.8 | Using Transformations to Graph Functions of the Form $y = af[k(x - d)] + c$ | 61 | | Curious Math | 171 |
| Chapter Review | | 74 | 3.5 | Quadratic Function Models: Solving Quadratic Equations | 172 |
| Chapter Self-Test | | 78 | 3.6 | The Zeros of a Quadratic Function | 179 |
| Chapter Task | | 79 | 3.7 | Families of Quadratic Functions | 187 |
| | | | 3.8 | Linear-Quadratic Systems | 194 |
| Chapter 2: Equivalent Algebraic | | 00 | Cha | pter Review | 200 |
| EXP | pressions | 80 | Chapter Self-Test | | 204 |
| Get | ting Started | 82 | Cha | pter Task | 205 |
| 2.1 | Adding and Subtracting Polynomials | 84 | | | |
| 2.2 | Multiplying Polynomials | 91 | Chapters 1–3 Cumulative Review | | 206 |
| | Curious Math | 97 | | | |
| 2.3 | Factoring Polynomials | 98 | Chapter 4: Exponential Functions | | 210 |
| Mid-Chapter Review | | 105 | Get | ting Started | 212 |
| 2.4 | Simplifying Rational Functions | 108 | 4.1 | Exploring Growth and Decay | 214 |
| 2.5 | Exploring Graphs of Rational Functions | 115 | 4.2 | Working with Integer Exponents | 217 |
| 2.6 | Multiplying and Dividing Rational | | 4.3 | Working with Rational Exponents | 224 |
| | Expressions | 117 | 4.4 | Simplifying Algebraic Expressions Involving Exponents | 231 |

Table of Contents vii

| Mid-Chapter Review | | 238 | 6.1 | 6.1 Periodic Functions and Their Properties | |
|---|---|-------------------|--|--|------------|
| 4.5 | Functions | 240 | 6.2 | Investigating the Properties of Sinusoidal Functions | 357 |
| 4.6 | Transformations of Exponential Functions | 244 | | Interpreting Sinusoidal Functions | 365 |
| | Applications Involving Exponential Functions | 254 | | -Chapter Review | 374 |
| | Curious Math | 264 | 6.4 | Exploring Transformations of Sinusoidal Functions | 377 |
| Chapter Review Chapter Self-Test | | 265 | 6.5 | of Sinusoidal Functions | |
| | | 270 | 6.6 | | 380 |
| Chapter Task | | 271 | Investigating Models of Sinusoidal Functions | 386 | |
| | | | 6.7 | Solving Problems Using Sinusoidal Models | 394 |
| Cha | apter 5: Trigonometric Ratios | 272 | | Curious Math | 402 |
| Get | ting Started | 274 | Cha | Chapter Review | |
| 5.1 | Trigonometric Ratios of Acute Angles | 276 | Cha | pter Self-Test | 406 |
| 5.2 | Evaluating Trigonometric Ratios for Special Angles | 283 | Cha | pter Task | 407 |
| | Curious Math | 288 | Cha | pters 4–6 Cumulative Review | 408 |
| 5.3 | Exploring Trigonometric Ratios for Angles Greater than 90° | 289 | Cha | pter 7: Discrete Functions: | |
| 5.4 Evaluating Trigonometric Ratios for Any Angle Between 0° and 360° | | 293 | | uences and Series | 412 |
| Mid | -Chapter Review | 302 | | ting Started | 414 |
| 5.5 | Trigonometric Identities | 305 | 7.1 | Arithmetic Sequences | 416 |
| 5.6 | The Sine Law | 312 | 7.2 7.3 | Geometric Sequences Creating Rules to Define Sequences | 426 433 |
| 5.7 | The Cosine Law | 321 | 7.4 | Exploring Recursive Sequences | 441 |
| 5.8 | Solving Three-Dimensional Problems by Using Trigonometry | 328 | | Curious Math | 444 |
| Chapter Review | | 336 | Mid | -Chapter Review | 445 |
| Chapter Self-Test | | ₃₄₀ 7. | 7.5 | Arithmetic Series | 448 |
| Chapter Task | | 341 | 7.6 | Geometric Series | 454 |
| | | | 7.7 | Pascal's Triangle and Binomial Expansions | 462 |
| Chapter 6: Sinusoidal Functions | | 342 | | pter Review | 467 |
| Getting Started | | 344 | | pter Self-Test | 470 |
| | | J., | Cha | pter Task | 471 |

viii Table of Contents

| Chapter 8: Discrete Functions: Financial Applications 472 | | cial | Chapter Review | 532 |
|---|--|------|--|-----|
| | | 472 | Chapter Self-Test | |
| Get | ting Started | 474 | Chapter Task | 537 |
| 8.1 | Simple Interest | 476 | | |
| 8.2 | Compound Interest: Future Value | 483 | Chapters 7–8 Cumulative Review | 538 |
| 8.3 | Compound Interest: Present Value | 493 | | |
| | Curious Math | 500 | Appendix A: Review of Essential Skills and Knowledge | 540 |
| Mid | -Chapter Review | 501 | Appendix B: Review of Technical Skills | 576 |
| 8.4 | Annuities: Future Value | 504 | Glossary | 610 |
| 8.5 | Annuities: Present Value | 513 | Answers | 617 |
| 8.6 | Using Technology to Investigate Financial Problems | 523 | Index | 687 |
| | | | Credits | 690 |

Table of Contents ix