

## Today's Learning Goal(s):

Date: \_\_\_\_\_

By the end of the class, I will be able to:

- a) simplify a radical.
- a) multiply, add and subtract radical expressions.

Last day's work:

pp. 160-162 #1 – 5, 7, 9, 13 [17]

## 3.4 Operations with Radicals

Date: Oct. 13/15

Recall: When working with radicals all answers must be in lowest terms.  
Look for factors of the radicand that are perfect squares!

Ex.1: Simplify

**Entire radical****Mixed radical**

a)  $\sqrt{50}$

$$= \sqrt{25 \cdot 2}$$

$$= 5\sqrt{2}$$

b)  $5\sqrt{45}$

$$= 5\sqrt{9 \cdot 5}$$

$$= 5(3)\sqrt{5}$$

$$= 15\sqrt{5}$$

Ex.2: Compare

$4\sqrt{5}$  and  $3\sqrt{10}$

$$= \sqrt{4 \times 4 \times 5} = \sqrt{9 \times 10}$$

$$= \sqrt{16 \cdot 5} = \sqrt{90}$$

$$= \sqrt{80} \therefore 4\sqrt{5} < 3\sqrt{10}$$

Ex.3: Simplify

a)  $\sqrt{6} \times \sqrt{3}$

$$= \sqrt{18}$$

$$= \sqrt{9 \cdot 2}$$

$$= 3\sqrt{2}$$

b)  $(-2\sqrt{7})(3\sqrt{7})$

$$= -6\sqrt{7 \cdot 7}$$

$$= -6\sqrt{49}$$

$$= -6(7)$$

$$= -42$$

$$\left\{ \begin{array}{l} \sqrt{6} \times \sqrt{3} \\ = \sqrt{3 \times 2 \times 3} \end{array} \right\}$$

Note: Many rules are similar to algebra:

Ex.4: Simplify

radicals

algebra

Summarizing some rules

$$\begin{aligned} \text{a) } \sqrt{2} + \sqrt{2} + \sqrt{2} \\ = 3\sqrt{2} \end{aligned}$$

$$\begin{aligned} x + x + x \\ = 3x \end{aligned}$$

$$\begin{aligned} \sqrt{a} + \sqrt{a} \\ = 2\sqrt{a} \end{aligned}$$

$$\begin{aligned} \sqrt{a} \times \sqrt{a} \\ = a \end{aligned}$$

$$\begin{aligned} \text{b) } 2\sqrt{3} + 5\sqrt{3} \\ = 7\sqrt{3} \end{aligned}$$

$$\begin{aligned} 2x + 5x \\ = 7x \end{aligned}$$

$$\sqrt{\frac{a}{b}}$$

$$\sqrt{a} \times \sqrt{b}$$

$$\text{c) } 2\sqrt{3} + 3\sqrt{7}$$

$$2x + 3y$$

$$= 2\sqrt{3} + 3\sqrt{7}$$

$$= 2x + 3y$$

$$= \frac{\sqrt{a}}{\sqrt{b}}$$

$$= \sqrt{ab}$$

Ex.5: Simplify

$$\text{a) } 3(4 - \sqrt{6})$$

$$= 12 - 3\sqrt{6}$$

$$\text{b) } (2 - 3\sqrt{5})(6 + \sqrt{5})$$

$$\begin{aligned} &= 12 + 2\sqrt{5} - 18\sqrt{5} - 3(5) \\ &= 12 - 16\sqrt{5} - 15 \\ &= -3 - 16\sqrt{5} \end{aligned}$$

$$\text{c) } \sqrt{\frac{2}{9}}$$

$$= \frac{\sqrt{2}}{\sqrt{9}}$$

$$= \frac{\sqrt{2}}{3}$$

$$\text{d) } \sqrt{50} + \sqrt{27} - \sqrt{72} + 2\sqrt{12}$$

$$= \sqrt{25}\sqrt{2} + \sqrt{9}\sqrt{3} - \sqrt{36}\sqrt{2} + 2\sqrt{4}\sqrt{3}$$

$$= 5\sqrt{2} + 3\sqrt{3} - 6\sqrt{2} + 2(2)\sqrt{3}$$

$$= \underline{5\sqrt{2}} + 3\sqrt{3} - \underline{6\sqrt{2}} + \underline{4\sqrt{3}}$$

$$= -\sqrt{2} + 7\sqrt{3}$$

Note: The textbook gives answers with the denominator rationalized.  
 This means that there is not a radical sign in the denominator.  
 In order to accomplish this, just multiply by an equivalent of 1.

Ex.6: Simplify

You Try: Simplify

$$\begin{aligned} \text{a) } & \frac{\sqrt{7}}{\sqrt{3}} \\ &= \frac{\sqrt{7}}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \\ &= \frac{\sqrt{21}}{3} \end{aligned}$$

$$\begin{aligned} \text{b) } & \frac{2\sqrt{3}}{\sqrt{20}} \\ &= \frac{2\sqrt{3}}{\sqrt{4}\sqrt{5}} \\ &= \frac{2\sqrt{3}}{2\sqrt{5}} \\ &= \frac{\sqrt{3}}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} \\ &= \frac{\sqrt{15}}{5} \end{aligned}$$

$$\begin{aligned} & \frac{\sqrt{6}}{2\sqrt{18}} \\ &= \frac{\sqrt{6}}{2\sqrt{9}\sqrt{2}} \\ &= \frac{1}{2\sqrt{2}} \end{aligned}$$

$$\begin{aligned} \text{c) } & \frac{3\sqrt{2}}{2\sqrt{27}} \\ &= \frac{3\sqrt{2}}{2\sqrt{9}\sqrt{3}} \\ &= \frac{3\sqrt{2}}{2(3)\sqrt{3}} \\ &= \frac{\sqrt{2}}{2\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \\ &= \frac{\sqrt{6}}{2(3)} \\ &= \frac{\sqrt{6}}{6} \end{aligned}$$

$$\begin{aligned} \text{d) } & \frac{\sqrt{6}}{2\sqrt{18}} \\ &= \frac{\sqrt{6}}{2\sqrt{9}\sqrt{2}} \\ &= \frac{\sqrt{6}}{2(3)\sqrt{2}} \\ &= \frac{\sqrt{6}}{6\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} \\ &= \frac{\sqrt{12}}{6(2)} \\ &= \frac{\sqrt{4}\sqrt{3}}{12} \\ &= \frac{2\sqrt{3}}{12} \\ &= \frac{\sqrt{3}}{6} \end{aligned}$$

Are there any Homework Questions you would like to see on the board?

Last day's work: pp. 160-162 #1 – 5, 7, 9, 13 [17]

4/6c

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Today's Homework Practice includes:

pp. 167-168 #(1 – 7)ace, 8–10, 12 [15–17]