

Today's Learning Goal(s):

By the end of the class, I will be able to:

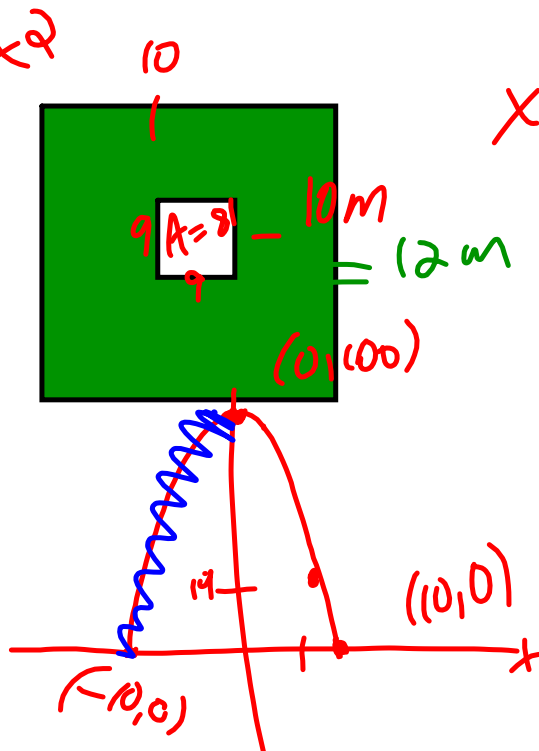
- a) graph a quadratic relation written in vertex form: $y = a(x - h)^2 + k$
- b) determine the equation of a quadratic relation in vertex form

p.179 #9 $= 100 - x^2$

$A = -x^2 + 100$

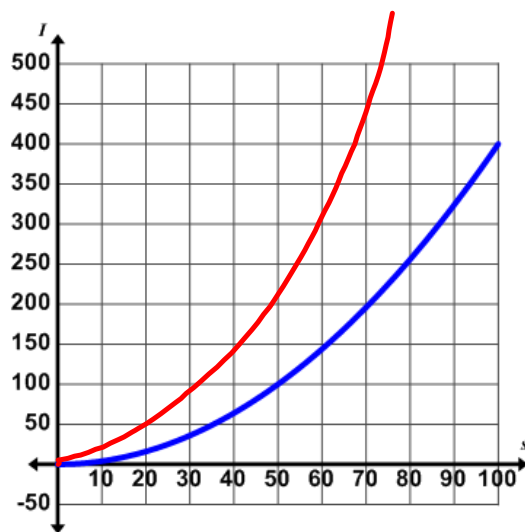
$v(0, 100)$

$A = -x^2 + 144$



$$l = 0.04 s^2$$

p.179 #10e



Today's plan:

Correct yesterday's graphs from worksheets **(10 minutes)**
Use slides at the end of file

Lesson 4.4 Day2 Finding an Equation **(20 minutes)**

pp. 185-187 #3 to 6, 7ab, 9, 11, 12, 14

Enrichment: pp. 186-188 #8, 10, 13, 15, 20

MPM 2DI

4.4 Graph $y = a(x-h)^2 + k$ (if $a \neq \pm 1$) (Day2)

Date: Apr. 12/16

The vertex form of a quadratic relation is $y = a(x-h)^2 + k$. The vertex is (h, k) .

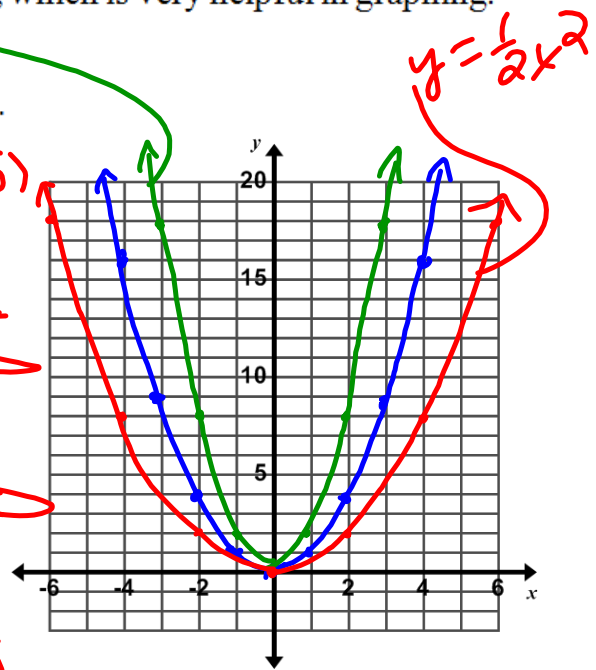
As we have learned, the “ a ” value determines the direction of opening, and represents the stretch or compression factor.

The “ a ” value also determines the step pattern, which is very helpful in graphing.

Ex. 1

On the same grid, graph $y = x^2$, $y = 2x^2$, and $y = \frac{1}{2}x^2$.

MG	$V(0,0)$	$V(0,0)$	$V(0,0)$
Over	Over	ups	Over
ups	ups	ups	ups
1	1	1	1
2	4	2	2
3	9	3	3
4	16	4	4
		6	6



Ex. 2

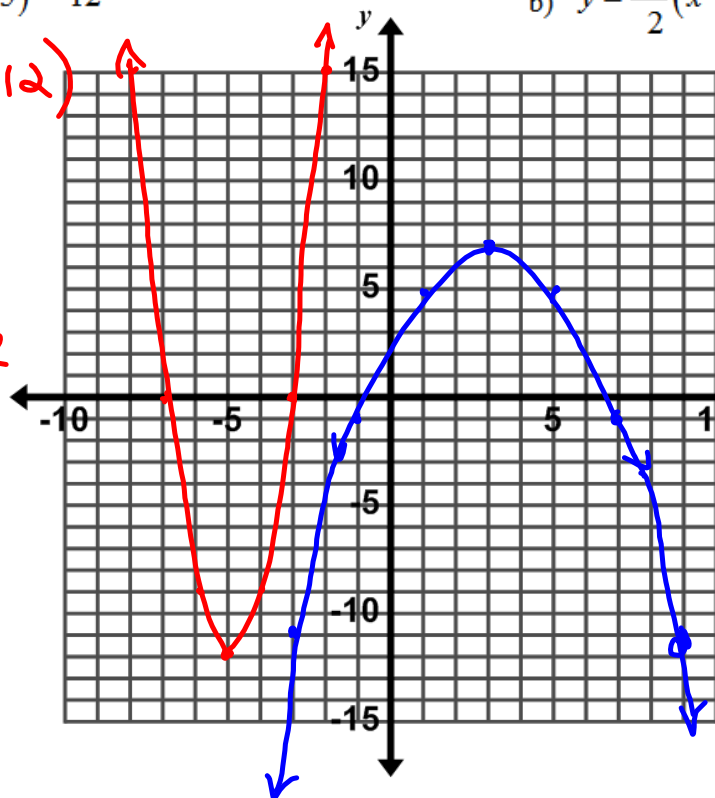
State the coordinates of the vertex, then graph.

a) $y = 3(x+5)^2 - 12$

b) $y = -\frac{1}{2}(x-3)^2 + 7$

$V(-5, -12)$
~~1~~ $3x$
~~2~~ $\rightarrow 12$
~~3~~ $\rightarrow 27$

$V(3, 7)$
~~1~~ $\frac{1}{2}$
~~2~~ 4 2
~~3~~ 9
~~4~~ 16 8
~~6~~ 18



Finding an Equation of a Parabola

Ex. 3 $y = a(x - h)^2 + k$

Find an equation for the parabola with vertex at $(4, 3)$ that passes through the point $(3, 0)$.

- ① **Begin with finding the vertex.**
- ② **Write the "starter" equation. (We don't know "a" yet.)**
- ③ **Find another point on the graph other than the vertex.**
- ④ **Substitute the new point's coordinates in the equation.**
- ⑤ **Write the conclusion...this is the final equation.**

$$\textcircled{2} \text{ } \rightarrow y = a(x - 4)^2 + 3$$

$$\textcircled{3} \textcircled{4} \text{ } \rightarrow (0) = a(3 - 4)^2 + 3$$

$$\rightarrow 0 = a(-1)^2 + 3$$

$$\rightarrow 0 = a(1) + 3$$

$$\rightarrow -3 = 1a$$

$$\textcircled{5} \text{ } \rightarrow \therefore y = -3(x - 4)^2 + 3 \text{ is the equation}$$

 (x, y)

Ex. 4

Find an equation for the parabola shown with vertex at $(-5, 3)$.

$$\rightarrow y = a(x + 5)^2 + 3$$

$$\rightarrow (1) = a((-3) + 5)^2 + 3$$

$$\rightarrow 1 = a(2)^2 + 3$$

$$\rightarrow 1 = a(4) + 3$$

$$1 = 4a + 3$$

$$\rightarrow 1 - 3 = 4a$$

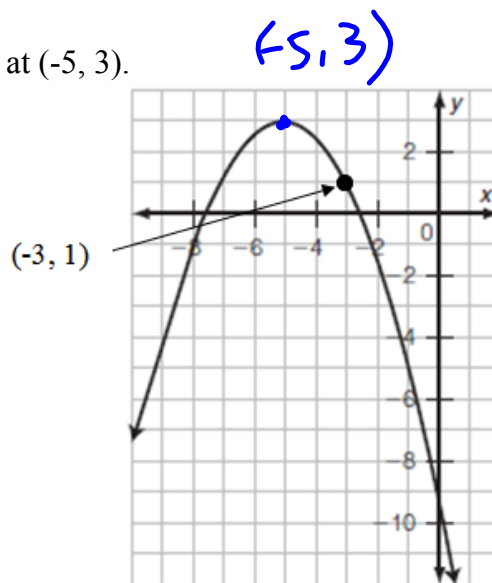
$$\rightarrow -2 = 4a$$

$$\rightarrow \frac{-2}{4} = a$$

$$\rightarrow \frac{-1}{2} = a$$

$$\therefore y = \frac{-1}{2}(x + 5)^2 + 3$$

is the equation.

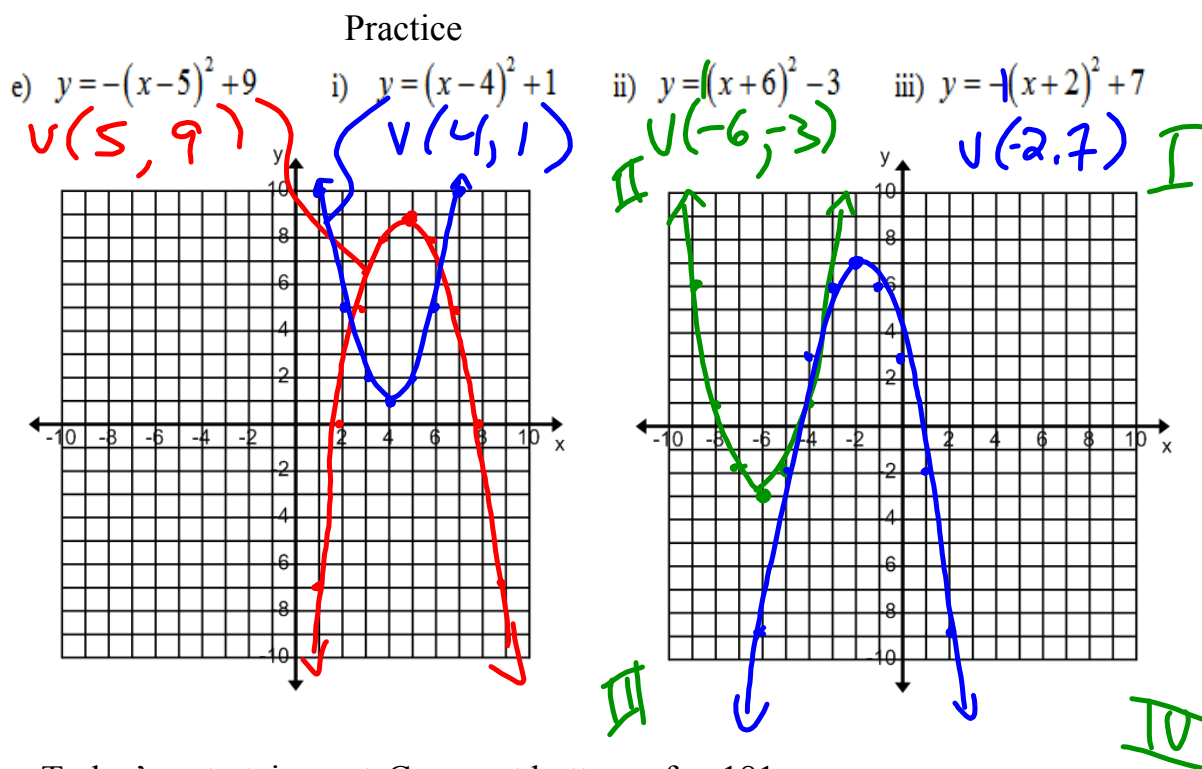


Ex. 5

Find an equation for the parabola with vertex at $(-2, -3)$ that passes through the point $(2, 3)$.

$$\begin{aligned}
 & \uparrow y = a(x+2)^2 - 3 \\
 & \uparrow (3) = a(2+2)^2 - 3 \\
 & \uparrow 3 = a(4)^2 - 3 \\
 & \uparrow 3 = a(16) - 3 \\
 & \uparrow 3 + 3 = 16a \\
 & \uparrow \rightarrow 6 = 16a \\
 & \uparrow \frac{6}{16} = a \\
 & \uparrow \frac{3}{8} = a \\
 & \uparrow \therefore y = \frac{3}{8}(x+2)^2 - 3
 \end{aligned}$$

Correct yesterday's graphs using next 3 pages.



Today's entertainment: Copy out bottom of p. 181

READ p.184 "Key Concepts"

p. 185 #1*, 2 *use the chart I gave you

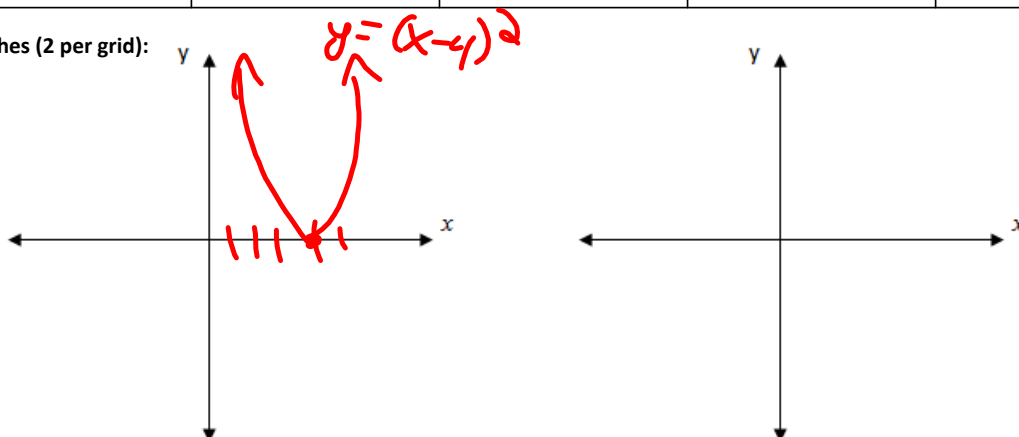
Practice i-iii above

Enrichment: pp.185-186 #6, 7

For yesterday's homework: $y = a(x - h)^2 + k$

Relation: \rightarrow	a) $y = (x - 4)^2$	b)	c)	d)
Property: \downarrow				
Vertex	(4, 0)			
(Equation of the) Axis of Symmetry	$x = 4$			
Stretch or compression factor relative to $y = x^2$	Neither a stretch nor a compression since the factor is $a=1$			
Direction of opening	Up			
Values x may take (called Domain)	Anything $\{x \in R\}$			
Values y may take (called Range)	$y \geq 0 \quad \{y \in R / y \geq 0\}$			

Sketches (2 per grid):



Relation: \rightarrow	e)	f)	g) $y=2(x-4)^2-5$	h) $y=-3(x+4)^2-2$
Property: \downarrow				
Vertex			$V(4, -5)$	$V(-4, -2)$
(Equation of the) Axis of Symmetry			$X=4$	$X=-4$
Stretch or compression factor relative to $y=x^2$			Stretched vertically by a factor of 2	Stretched vertically by a factor of 3
Direction of opening			up	down
Values x may take (called Domain)			$\{x \in \mathbb{R}\}$	$\{x \in \mathbb{R}\}$
Values y may take (called Range)			$\{y \in \mathbb{R} / y \geq -5\}$	$\{y \in \mathbb{R} / y \leq -2\}$

Sketches (2 per grid):

