

Today's Learning Goal(s):

By the end of the class, I will be able to:



a) convert an entire radical to a mixed radical in simplest form.

MPM 2DI

2.E Radicals

Date: Sept. 28/16

Today we will convert an entire radical to a mixed radical in simplest form.

Copy-> A radical is any number with a root, or radical sign. $\sqrt{\quad}$

Copy-> An **entire** radical has its number entirely beneath the radical. Ex. $\sqrt{2}$

Copy-> A **mixed** radical has a coefficient in front of the radical. Ex. $4\sqrt{3}$

Radicals occur frequently when using the length formula, which we will begin using in the next class.

$$\begin{array}{l} \sqrt{9} \\ = 3 \end{array} \quad \begin{array}{l} \sqrt[3]{8} \\ = 2 \end{array}$$

Observe:

$$\begin{aligned} &\sqrt{9} \times \sqrt{4} \\ &= 3 \times 2 \\ &= 6 \end{aligned}$$

Now:

$$\begin{aligned} &\sqrt{9} \times \sqrt{4} \\ &= \sqrt{9 \times 4} \\ &= \sqrt{36} \\ &= 6 \end{aligned}$$

$$\begin{aligned} \text{Rule: } &\sqrt{a} \times \sqrt{b} \\ &= \sqrt{a \times b} \\ &= \sqrt{ab} \end{aligned}$$

$$\sqrt{a} \times \sqrt{b} = \sqrt{ab}$$

Note: $a, b \geq 0$ 

Next:

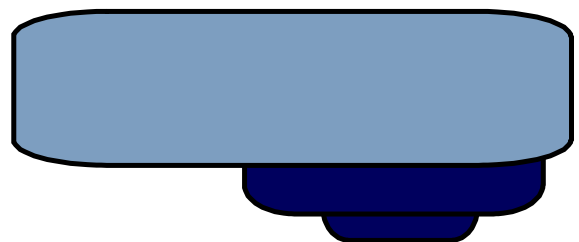
$$\begin{aligned} &\sqrt{4} \times \sqrt{3} \\ &= 2 \times \sqrt{3} \\ &= 2\sqrt{3} \end{aligned}$$

but

$$\begin{aligned} &\sqrt{4} \times \sqrt{3} \\ &= \sqrt{12} \end{aligned}$$

$$\therefore 2\sqrt{3} = \sqrt{12}$$

mixed radical \rightarrow *entire* radical



An introductory video: (Click anywhere on the blue link below...play until the 5:36 mark)

Play until **5:36**
<http://www.khanacademy.org/math/arithmetic/exponents-radicals/radical-radicals/v/simplifying-radicals>

Ex.1 Express as a mixed radical in simplest form.

| | | | | |
|----------------------|----------------------|----------------------|------------------------------|------------------------------|
| a) $\sqrt{8}$ | b) $\sqrt{12}$ | c) $\sqrt{18}$ | d ₁) $\sqrt{32}$ | d ₂) $\sqrt{32}$ |
| $= \sqrt{4}\sqrt{2}$ | $= \sqrt{4}\sqrt{3}$ | $= \sqrt{9}\sqrt{2}$ | $= \sqrt{4}\sqrt{8}$ | $= \sqrt{16}\sqrt{2}$ |
| $= 2\sqrt{2}$ | $= 2\sqrt{3}$ | $= 3\sqrt{2}$ | $= 2\sqrt{8}$ | $= 4\sqrt{2}$ |
| | | | $= 2\sqrt{4}\sqrt{2}$ | |
| | | | $= 2(2)\sqrt{2}$ | |
| | | | $= 4\sqrt{2}$ | |

Now try with a partner:

| | | |
|-----------------------|-----------------------|-------------------------|
| e) $\sqrt{98}$ | f) $\sqrt{150}$ | g) $-3\sqrt{40}$ |
| $= \sqrt{49}\sqrt{2}$ | $= \sqrt{25}\sqrt{6}$ | $= -3\sqrt{4}\sqrt{10}$ |
| $= 7\sqrt{2}$ | $= 5\sqrt{6}$ | $= -3(2)\sqrt{10}$ |
| | | $= -6\sqrt{10}$ |

Challenge Question:

h) $3\sqrt{5} \times 7\sqrt{10}$

$$= 21\sqrt{50}$$

$$= 21\sqrt{25}\sqrt{2}$$

$$= 21(5)\sqrt{2}$$

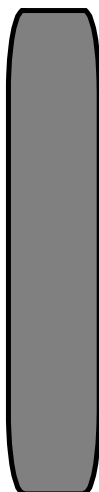
$$= 105\sqrt{2}$$

Reducing radicals is easier if you "memorize/recognize" the first 20 squares.

| n | n ² |
|---|----------------|
| 1 | 1 |
| 2 | 4 |
| 3 | 9 |
| 4 | 16 |
| 5 | 25 |
| 6 | 36 |
| 7 | 49 |
| 8 | 64 |



| n | n ² |
|----|----------------|
| 9 | 81 |
| 10 | 100 |
| 11 | 121 |
| 12 | 144 |
| 13 | 169 |
| 14 | 196 |
| 15 | 225 |
| 16 | 256 |



| n | n ² |
|----|----------------|
| 17 | 289 |
| 18 | 324 |
| 19 | 361 |
| 20 | 400 |



Today's Worksheet#1 and 4

Note: Do NOT do #2 until next class!!

and Pythagorean Review p.327 #5, 6

Simplifying Radicals

- Express each of these as mixed radicals in simplest form.
 - $\sqrt{72}$
 - $\sqrt{64}$
 - $\sqrt{75}$
 - $\sqrt{48}$
 - $\sqrt{162}$
 - $\sqrt{192}$
- Find the length of the line segments with the given endpoints. Express your answers as simplified radicals.
 - A(-2, 3) and B(4, 7)
 - C(4, 8) and D(7, -4)
 - E(-1, -6) and F(4, 4)
 - G(-5, 2) and H(7, 8)
- Express as a mixed radical in simplest form.
 - $2\sqrt{125}$
 - $5\sqrt{147}$
 - $-6\sqrt{72}$
 - $9\sqrt{24}$
 - $-4\sqrt{50}$
 - $0.5\sqrt{108}$

Solutions to Radicals Worksheet:

1, 4

Simplifying Radicals

1. Express each of these as mixed radicals in simplest form.
- a) $\sqrt{72}$
 - b) $\sqrt{64}$
 - c) $\sqrt{75}$
 - d) $\sqrt{48}$
 - e) $\sqrt{162}$
 - f) $\sqrt{192}$
4. Express as a mixed radical in simplest form.
- a) $2\sqrt{125}$
 - b) $5\sqrt{147}$
 - c) $-6\sqrt{72}$
 - d) $9\sqrt{24}$
 - e) $-4\sqrt{50}$
 - f) $0.5\sqrt{108}$

Simplifying Radicals Answers

1. a) $6\sqrt{2}$
- b) 8
 - c) $5\sqrt{3}$
 - d) $4\sqrt{3}$
 - e) $9\sqrt{2}$
 - f) $8\sqrt{3}$
4. a) $10\sqrt{5}$
- b) $35\sqrt{3}$
 - c) $-36\sqrt{2}$
 - d) $18\sqrt{6}$
 - e) $-20\sqrt{2}$
 - f) $3\sqrt{3}$