

Before we begin, are there any questions from last day's work?

Read p.267 Example 2, Method 1: Complete the Square

pp. 270-272 #4c, 5, 6a, 8abce, 17ab, 19

Enrichment: pp. 272-273 #17d, 27

Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) find the vertex of a quadratic relation when it is presented in standard form.
- b) solve a word problem involving finding the maximum or minimum value of a quadratic function.

p.272 #17

$$\begin{aligned}
 \text{a) } y &= 1.5x^2 + 6x - 7 \\
 &= 1.5(x^2 + 4x) - 7 \\
 &= 1.5(x^2 + 4x + 4 - 4) - 7 \\
 &= 1.5(x+2)^2 - 6 - 7 \\
 &= 1.5(x+2)^2 - 13 \\
 &\therefore V(-2, -13) \\
 &\therefore \text{the min. point is } (-2, -13)
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } y &= -0.1x^2 - 2x + 1 \\
 &= -0.1(x^2 + 20x) + 1 \\
 &= -0.1(x^2 + 20x + 100 - 100) + 1 \\
 &= -0.1(x+10)^2 + 10 + 1 \\
 &= -0.1(x+10)^2 + 11 \\
 &\therefore \text{the max point is } (-10, 11).
 \end{aligned}$$

$$\begin{aligned}
 \#19 \text{ a) } x^2 + 8x + c &= (x+h)^2 \\
 x^2 + 8x + 16 &= (x+4)^2
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } x^2 + 6x + 36 &= (x+h)^2 \\
 x^2 + 12x + 36 &= (x+6)^2
 \end{aligned}$$

MPM 2DI

6.1 **Maxima and Minima**-Completing the Square (Day2)Date: Dec. 1/16

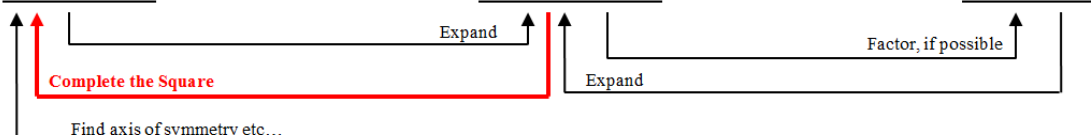
$$y = a(x-h)^2 + k$$

Vertex Form

$$y = ax^2 + bx + c$$

Standard Form

$$y = a(x-r)(x-s)$$

Factored Form

Warm-up: Find the vertex by completing the square.

a) $y = -x^2 + 12x - 40$

$$= -(x^2 - 12x) - 40$$

$$= -\underbrace{(x^2 - 12x + 36 - 36)} - 40$$

$$= -(x - 6)^2 + 36 - 40$$

$$= -(x - 6)^2 - 4$$

$$\therefore V(6, -4)$$

b) $y = 2x^2 + 16x + 29$

$$= 2(x^2 + 8x) + 29$$

$$= 2\underbrace{(x^2 + 8x + 16 - 16)} + 29$$

$$= 2(x + 4)^2 - 32 + 29$$

$$= 2(x + 4)^2 - 3$$

$$\therefore V(-4, -3)$$



Ex. 1 A ball is slingshot from the roof of the school.

It's height, h , in metres is given by $h = -4.9t^2 + 29.4t + 12$, where t , is the time in seconds.

- a) What is the height of the school?
 b) What is the maximum height reached by the ball and when does it reach it?



a) Let $t = 0$

$$h = -4.9(0)^2 + 29.4(0) + 12$$

$$= 12$$

\therefore the height of the school is 12 m.

b)

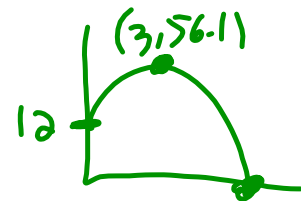
$$h = -4.9t^2 + 29.4t + 12$$

$$= -4.9(t^2 - 6t) + 12$$

$$= -4.9(t^2 - 6t + 9 - 9) + 12$$

$$= -4.9(t - 3)^2 + 44.1 + 12$$

$$= -4.9(t - 3)^2 + 56.1$$



$\cup(3, 56.1)$

the maximum height reached by the ball is 56.1 m,
 and it reaches it at 3 sec.

Today's practice: Worksheet #1 to 6
Enrichment: #7 to 10

$\frac{1}{2} \times 3$

Worksheet #1

Decimal

$$h = -2x^2 + 6x + 5$$

$$= -2(x^2 - 3x) + 5$$

$$= -2\left(x^2 - 3x + \left(\frac{3}{2}\right)^2 - \left(\frac{3}{2}\right)^2\right) + 5$$

$$= -2\left(x^2 - 3x + \frac{9}{4} - \frac{9}{4}\right) + 5$$

$$= -2\left(x - \frac{3}{2}\right)^2 + \frac{9}{2} + 5$$

$$= -2\left(x - \frac{3}{2}\right)^2 + \frac{19}{2}$$

$\frac{3}{2}$

$$-2\left(\frac{-9}{4}\right)$$

$\frac{9}{2}$

Fraction

$$h = -2x^2 + 6x + 5$$

$$= -2(x^2 - 3x) + 5$$

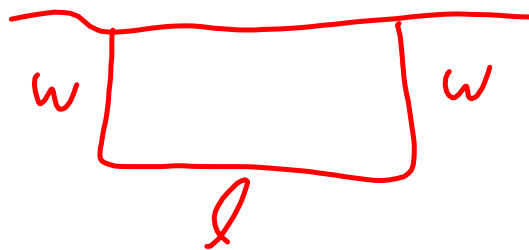
$$= -2(x^2 - 3x + 2.25 - 2.25) + 5$$

$$= -2(x - 1.5)^2 + 4.5 + 5$$

$$= -2(x - 1.5)^2 + 9.5$$

$\frac{9}{2} + 5$

#6



100m

$$100 = 2w + l$$

$$A = lw$$
$$=$$