Before we begin, are there any questions from last day's work?

# Today's Learning Goal(s):

By the end of the class, I will be able to:

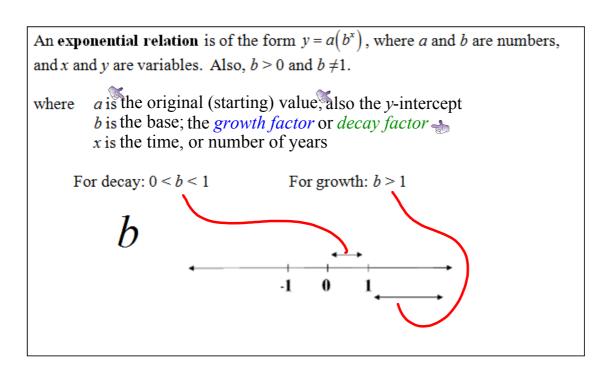
- a) use an exponential relation to mode exponential growth or decay
- b) solve problems involvingexponential growth or decay.

MBF 3CI

### Date: 02/16

## 7.5 Modelling Exponential Growth and Decay Problems (Day1)

Population growth and price increases can be modeled by increasing exponential graphs. Decreasing exponential relations can represent declining populations and depreciation in value.



#### **Exponential Growth**

Ex.1 In 2001, the population of Canada was 31 051 000.

The annual growth rate is assumed to be about 1%.

Recall:  $y = a (b)^x$ 

a) What is the change factor as a decimal?

Recall: 
$$y = a (b)^x$$

Next year's population is 100 % + 1 %

the base, b = 1.01 (as a decimal)..."b" is the "growth factor" or "change factor"

b) Write a formula that models the population  $\psi$ ), with the number of years since 2001 (x).

$$y = 31\ 051\ 000\ (1.01)^x$$

c) Predict the population of Canada in 2010, to the nearest thousand.

$$y = 31\ 051\ 000\ (1.01)$$
 9  
 $= 33\ 960\ 021.4$ 

<u>→</u>=33 960 000

the population in 2010 should be 33 960 000

Ex.2 A population increases by 7.8% each year.

If the initial population is 124, determine the population after:

- a) 5 years
- b) 10 years
- Let y represent the population.

Let x represent the number of years.

$$b=100\% + 7.8\%$$

$$\phi$$
 b= 1.078

$$y = 124(1.078)^x$$

$$y = 124(1.078)^5$$

$$y = 180.5$$

$$b = 1.078$$

$$v = 124(1.078)^{x}$$

$$y = 124(1.078)^{10}$$

$$rightharpoonup y = 262.7$$

after 10 years the population is 262

• after 5 years the population is 180.

### **Exponential Decay**

Ex. 1 The price of a new car is \$24 599. Its value depreciates by 30% each year.

a) Write a formula to model the decrease in value of the new car. DEFINE YOUR VARIABLES.

Let y represent the value of the car, in dollars. Recall:  $y = a (b)^x$ 

Let x represent the number of years. The base, b, must represent a 30% decrease: b = 100% - 30%

$$\therefore y = 24 \ 599(0.70)^{x} = 70\%$$

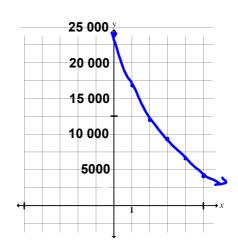
$$= 0.70$$

b) What is the depreciated value of the car after 5 years?

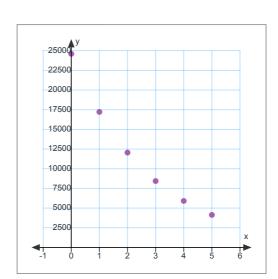
$$y = 24599(0.7)^5$$
  
 $\Rightarrow \pm 4134.35$ 

c) Graph this relation that models that value of the car for the first five years.

x	y
0	24,599
1	17,219.3
2	12,053.51
3	8,437.46
4	5,906.22
5	4,134.35



X	У				
0	24 599				
1	17 219.30				
2	12 053.51				
3	8 437.46				
4	5 906.22				
5	4 134.35				



Ex.2 Caffeine is present in coffee, tea, chocolate and other products.

This chemical is eliminated from the human body over time exponentially.

The table shows the mass of caffeine remaining in an average-sized person drinking a cup of coffee containing 130 mg of caffeine:

time	0	1	2	3	4	5	6	7
mg	130	113.1	98.4	85.6	74.5	64.8	56.4	49.0

a) Why is it an example of exponential decay?

Check the y-ratios. 
$$\frac{113.1}{130}$$
  $\frac{98.4}{113.1}$   $\frac{85.6}{98.4}$   $=0.87$   $=0.870$   $=0.869$ 

the y-ratios are constant, : the table represents exponential decay

 $\clubsuit$  we know it is decay, because the base is between 0 and 1  $\clubsuit$ 

b) What percent of caffeine is eliminated from a person's body per hour?

: approximately 87% is **remaining**. (the base represents the % remaining)

**∴** 13% of the caffeine is being eliminated from a person's body per hour.

Entertainment: p. 401 #1bcd, 2bc, 3 (for 3b graph without a graphing calculator), 5abcd, 6, 7ab, 12

Return and 2016

Return

Be ready for SWYK 7.2!

(It will have more exponent law questions, plus some sketching.)