

Correct Last Day's Homework: pp. 245-247 #1a, 2e, 3d, 4c, 6, 7ab, 11
Challenge: #14

Factoring Warm-up: *This part is not on the handout.*

- a) List all the factors of 12
(This means list all the numbers that divide into 12 with no remainder)

1, 2, 6, 4, 3, 12

1	12
2	6
3	4
4	

- b) List all the factors of 20

1	20
2	10
4	
4	5
5	

- c) List all the factors of 30

1	30
2	15
3	10
4	
5	6

Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) **Expand** two simple binomials (in one step).
- b) List all the factors of any number.
- c) **Factor** a trinomial.
- d) Understand how the "+" and "-" signs of a trinomial can help to determine its factors.

MBF 3CI 5.3 Factoring Trinomials $x^2 + bx + c$ (Day 1)

"The Background"

Date: Apr-26/17

Expand the following:

$$1) (x+3)(x+5)$$

$$= x^2 + 5x + 3x + 15$$

$$= x^2 + 8x + 15$$

$$2) (x+5)(x+6)$$

$$= x^2 + 6x + 5x + 30$$

$$= x^2 + 11x + 30$$

$$3) (x+2)(x+7)$$

$$= x^2 + 9x + 14$$

Expanding (pointing to the expansion) and *Factoring* (pointing to the original expression)

$$4) (x-4)(x-2)$$

$$= x^2 - 2x - 4x + 8$$

$$= x^2 - 6x + 8$$

$$5) (x-7)(x-3)$$

$$= x^2 - 10x + 21$$

$$6) (x-2)(x-5)$$

$$= x^2 - 7x + 10$$

Ex.1 Factor the following trinomials, where **last term is positive**, using the Product/Sum method:

1) $x^2 + 8x + 15$

2) $x^2 - 7x + 12$

3) $x^2 - 22x + 40$

$$= (x+3)(x+5) = (x-3)(x-4) = (x-2)(x-20)$$

$$\begin{array}{r} 1 \quad 15 \\ \times \\ 3 \quad 5 \\ \hline 5 \end{array}$$

$$\begin{array}{r} 1 \quad 12 \\ \times \\ 2 \quad 6 \\ 3 \quad 4 \end{array}$$

$$\begin{array}{r} -1 \quad -40 \\ -2 \quad -20 \\ \times \\ 2 \\ -4 \quad -10 \\ 5 \quad 8 \\ \hline 1 \end{array}$$

4) $x^2 - 14x + 40$

5) $x^2 - 13x + 40$

6) $x^2 + 9x + 18$

$$= (x-4)(x-10) = (x-5)(x-8)$$

$$= (x+3)(x+6)$$

$$\begin{array}{r} 1 \quad 18 \\ \times \\ 2 \quad 9 \\ 3 \quad 6 \end{array}$$

7) $x^2 + 3x + 2$

8) $x^2 - 17x + 72$

9) $x^2 + 5x + 2$

$$= (x+1)(x+2) = (x-9)(x-8)$$

$$= \text{D.N.F.}$$

(Does Not Factor)

SUMMARY:

When the last term is **POSITIVE**, the two factors have the same sign, and must add to get the middle term.

- The middle sign indicates the sign of both factors.

Ex.2 Factor the following trinomials, where the *last term is negative*, using the Product/Sum method:

$$1) x^2 + 18x - 40 = (x+20)(x-2)$$

$$2) x^2 - 18x - 40$$

$$= (x+2)(x-20)$$

$$3) x^2 + 6x - 16$$

$$= (x+8)(x-2)$$

1	40
2	20
3	
4	10
5	8

-1	+16
-2	+8
3	
-4	+4

$$4) x^2 - 14x - 72$$

$$= (x+4)(x-18)$$

$$5) x^2 + 9x - 10$$

$$= (x+10)(x-1)$$

$$6) x^2 - 13x - 30$$

see purple below
before correcting

$$= (x+2)(x-15)$$

1	-72
2	-36
3	-24
4	-18
5	
6	-12
7	
8	-9

$$x^2 - 18x + 4x - 72$$

$$= x^2 - 14x - 72$$

Summary 2: When the *last term is negative*, the two factors have **opposite** signs, and must **add** to get the middle term.

The middle sign indicates the sign of **the larger factor**.

Always Remember: Factoring is the opposite of expanding.

Therefore, you can **always check your factors by expanding**.

(It may take an extra minute or two, but you will catch when you make an error with your signs.)
For example, you may want to check number 6 from above to see if you have the correct signs.

Entertainment: pp. 253-255 #2, 3aceg, 9ace

Challenge: #15a

Knowledge Hook?