

**Be ready for tomorrow's Ch.7 SUMMATIVE on Exponential Relations**

Pre-test Warm-up

**Return and Correct SWYK 7.2**

**Correct Homework on Half-life**

## Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) Calculate simple interest.
- b) Use a table to calculate compound interest.

MBF 3CI **Simple and Compound Interest** Date: May 23/17

Banks pay you interest for the use of your money. When you deposit money in a bank account, the bank reinvests your money to make a profit.

If you borrow money from a bank (a loan), you are charged interest.

Simply put, **interest** is the cost of borrowing money.

**Simple Interest** is always calculated on just the **original** value invested (or borrowed), which is called the **principal,  $P$** . The **annual rate of interest is  $r$** , which is always expressed **as a decimal**. The period of **time is  $t$** , which must be stated **in years**.

**Simple Interest ( $I$ ):**  $I = Prt$

The final value or **amount ( $A$ )** of an investment/loan, includes the principal and interest owed.

**Amount, ( $A$ ):**  $A = P + I$

**Compound interest** is calculated on the accumulated value of the investment, which includes the principal and the accumulated interest of prior periods.

**Investigation:**

Ex. 1. Let's compare: **Suppose you are investing \$1000 at 7% per year, for 3 years.**

$$I = Prt$$

$$I = ?$$

$$P = 1000$$

$$r = 7\%$$

$$= 0.07$$

$$t = 1$$

1 year

$$I = (1000)(.07)(1)$$

$$= 70$$

2 years

$$I = (1000)(.07)(2)$$

$$= 140$$

Remember: "r" is ALWAYS expressed as a decimal.

1. Complete this table, for 7% simple interest.

Year	Amount at the Start of the Year (\$)	Simple Interest (\$)	Amount at the End of the Year (\$)
1	1000	70	1070
2	1070	70	1140
3	1140	70	1210

1140  
70  
70

Note: We could calculate the final values in one step.

$$I = Prt$$

$$I = (1000)(.07)(3)$$

$$= 210$$

$$A = P + I$$

$$= 1000 + 210$$

$$= 1210$$

2. Complete this table, for 7% COMPOUND interest. *See below chart for calculations.*

Year	Amount at the Start of the Year (\$)	Compound Interest (\$)	Amount at the End of the Year (\$)
1	1000	70	1070
2	1070	74.90	1144.90
3	1144.90	80.14	1225.04

*Handwritten notes: 1070, 1144.90, 1225.04, 1070, 107, 107*

$$I_1 = (1000)(.07)(1) = 70$$

$$I_2 = (1070)(.07)(1) = 74.90$$

*No Fade in...do by hand?*

$$I_3 = pnt = (1144.90)(.07)(1) = 80.143 \div 80.14$$

$$I_3 = (1144.90)(.07)(1) = 80.14$$

Note: We could calculate the final values in one step, but we'll need a new formula. (*next lesson*)

**3. Look at the last/shaded columns in both tables.**

How does the growth of money in one table differ from the other table?

Chart 1: 🖱️ Growth is constant at \$70

Chart 2: 🖱️ Growth is increasing each time.

**4. Identify the type of growth (linear, quadratic, or exponential) for...**

a) Simple interest

🖱️ linear growth

b) Compound interest

🖱️ exponential growth

**Explain.**

🖱️ Each amount is multiplied by 1.07 to get the next amount.

🖱️ Simple interest grows by a constant amount, so it is linear.

🖱️  $(1.07)(1.07)(1.07)\dots$   
 $= (1.07)^3$

The **compound growth factor** is  $1 + i$ , where  $i$  is the interest rate (as a decimal) per compounding period. In the investigation you just completed, the growth factor was  $1 + 0.07$ , or 1.07.

The number of **compound periods** is denoted by  $n$ . What is the value of  $n$  in the investigation you just completed? Answer: 3

Ex. 2. Determine the amount of, **AND** total interest earned on a \$2500 investment at 3.45%/a, aer 9 years **simple** interest.

$$I = ?$$

$$P = 2500$$

$$r = 3.45\%$$

$$= 0.0345$$

$$I = Prt$$

$$= 2500(0.0345)(9)$$

$$= \$776.25$$

$$A = P + I$$

$$= 2500 + 776.25$$

$$= \$3276.25$$

$$t = 9$$

∴ the amount of the investment is \$3276.25, and total interest earned is \$776.25.

Entertainment: **Study for tomorrow's Ch.7 SUMMATIVE on Exponential Relations**

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