

Piecewise Functions (1.6)

Math Learning Target:



"I can graph all piecewise functions.

I know how to apply piecewise functions in a problem.

I know how to determine if a function is continuous.

If a function is discontinuous, I know how to describe the discontinuity."

A **piecewise function** is a function defined by using two or more functions, on two or more intervals.

Recall: $f(x) = |x|$ defines the distance the value x is from the origin.

The absolute value function may be expressed as a piecewise function.

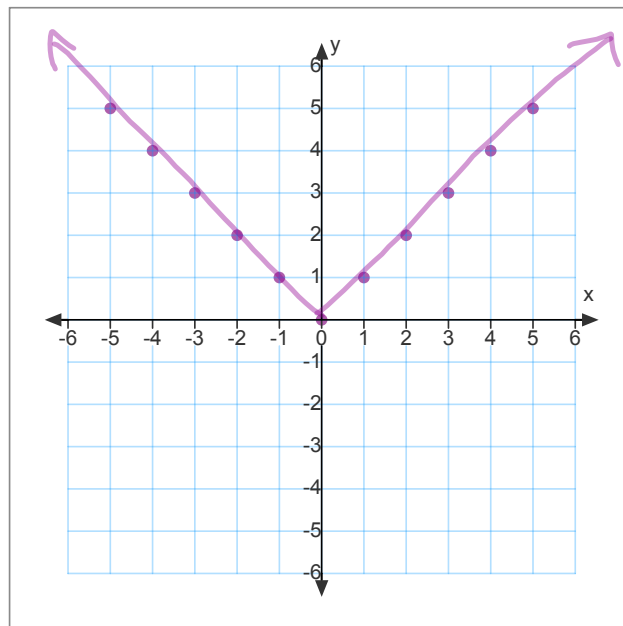
$$f(x) = |x| = \begin{cases} x & \text{when } x > 0 \\ -x & \text{when } x \leq 0 \end{cases}$$

$$\text{if } x = -1$$

$$f(x)$$

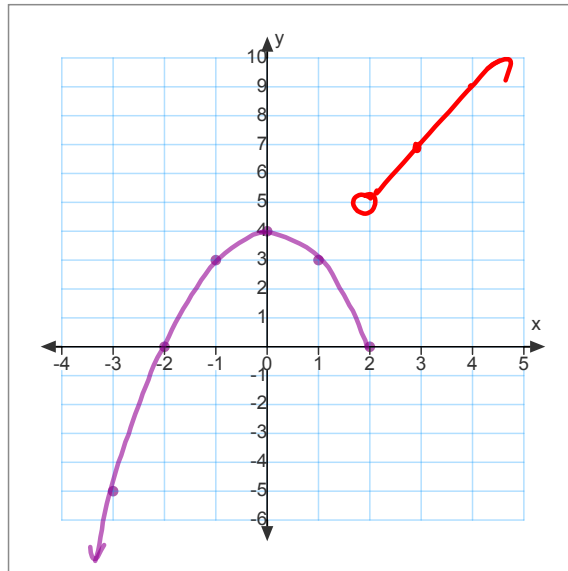
$$= -(-1)$$

$$= 1$$



Ex. 1: Graph:

$$f(x) = \begin{cases} -x^2 + 4 & \text{if } x \leq 2 \\ 2x + 1 & \text{if } x > 2 \end{cases}$$



Click here for the video: "[Continuity of Functions: Photostory](#)"
 (The video is posted in our Google Classroom for your convenience).

A function is **continuous** when there are no "holes", vertical asymptotes and "jumps" over its entire domain.

If the function is not continuous, it is **discontinuous**

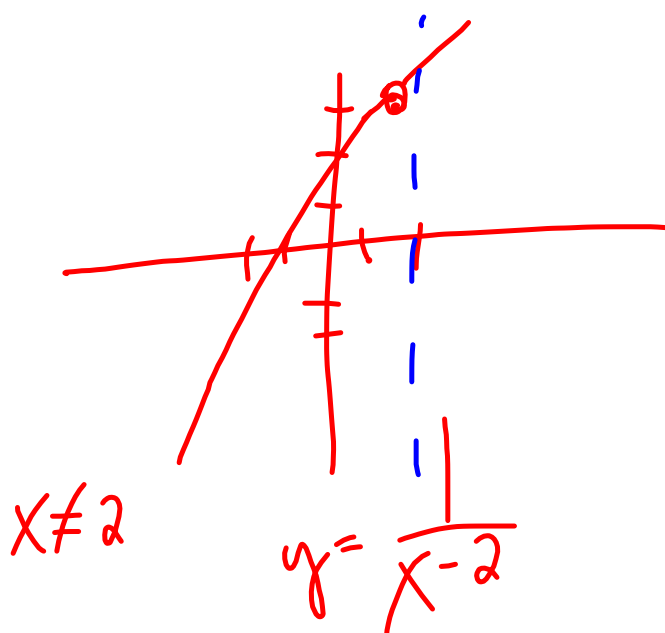
Ex. 2: Is the function in Ex. 1 continuous? Explain.

No, it is discontinuous because there is a "jump".
 i.e, the value of both functions at $x=2$ is not equal.

$$\begin{array}{l} \text{if } x = 2 \\ f(2) = -(2)^2 + 4 \\ \quad = -(4) + 4 \\ \quad = 0 \text{ (closed)} \end{array} \left. \vphantom{\begin{array}{l} \text{if } x = 2 \\ f(2) = -(2)^2 + 4 \\ \quad = -(4) + 4 \\ \quad = 0 \text{ (closed)} \end{array}} \right\} \begin{array}{l} f(2) = 2(2) + 1 \\ \quad = 4 + 1 \\ \quad = 5 \text{ (open)} \end{array}$$

If time: Discuss using GeoGebra

$$\begin{aligned}y &= \frac{x^2 - 4}{x - 2} \\ &= \frac{\cancel{(x-2)}(x+2)}{\cancel{x-2}} \\ &= x+2\end{aligned}$$



MHF 4U1 Unit 1 (Enrichment #3)

Present an organized solution to the following...

Determine all linear functions $f(x) = ax + b$ such that if $g(x) = f^{-1}(x)$ for all values of x , then $f(x) - g(x) = 44$ for all values of x . (Note: f^{-1} is the inverse function of f .)

$$\text{if } g(x) = f^{-1}(x)$$

$$y = ax + b$$

$$x = ay + b$$

$$\frac{x-b}{a} = y$$

$$\therefore g(x) = \frac{x-b}{a}$$

$$f(x) - g(x) = 44$$

$$f(x) = g(x) + 44$$

$$= \frac{x-b}{a} + 44$$

$$= \frac{x}{a} - \frac{b}{a} + \frac{44a}{a}$$

$$= \frac{1}{a}x + \frac{44a-b}{a}$$

When does $ax + b = \frac{1}{a}x + \frac{44a-b}{a}$

$$ax = \frac{1}{a}x$$

$$b = \frac{44a-b}{a}$$

$$a = \frac{1}{a}$$

$$\text{if } a = 1$$

$$ab = 44a - b$$

$$b = 44 - b$$

$$2b = 44$$

$$b = 22$$

$$\text{or } a = -1$$

$$ab = 44a - b$$

$$(-1)b = 44(-1) - b$$

$$-b = -44 - b$$

$$-b + b = -44$$

$$0 = -44$$

Not possible

$$\therefore f(x) = 1x + 22$$