

3.5 Dividing Polynomials

Polynomial
Division

Math Learning Target:

"I can determine the quotient when one polynomial is divided by another polynomial."

Ex. 1: Divide 352 by 15 using long division.

$$\begin{array}{r}
 \underline{352} \\
 15 \overline{) 352} \\
 \underline{-30} \\
 52 \\
 \underline{-45} \\
 7
 \end{array}$$

← Quotient
 ← Dividend
 ← Remainder

Division Statement:
 dividend = divisor \times quotient + remainder
 $352 = 15 \times 23 + 7$

Word wall:
 divisor
 quotient
 dividend
 remainder

$$\left. \begin{array}{l}
 \frac{352}{15} = 23 \text{ R } 7 \\
 = 23 \frac{7}{15} \\
 \frac{352}{15} = 23 + \frac{7}{15} \\
 = 23.4\bar{6}
 \end{array} \right\}$$

Ex. 2: Divide: $3x - 2x^4 + 5$ by $x + 3$ using long division.

$$\begin{array}{r}
 -2x^4 + 3x + 5 \\
 x+3 \overline{) -2x^4 + 0x^3 + 0x^2 + 3x + 5} \\
 \underline{-2x^4 - 6x^3} \\
 6x^3 + 0x^2 \\
 \underline{-6x^3 + 18x^2} \\
 -18x^2 + 3x \\
 \underline{-18x^2 - 54x} \\
 57x + 5 \\
 \underline{-57x + 171} \\
 -166 \text{ Remainder}
 \end{array}$$

Dividend = divisor \times Quotient + Remainder

$$-2x^4 + 3x + 5 = (x + 3)(-2x^3 + 6x^2 - 18x + 57) + (-166)$$

Also

$$\frac{-2x^4 + 3x + 5}{x + 3} = -2x^3 + 6x^2 - 18x + 57 + \frac{-166}{x + 3}$$

$$\frac{\text{Dividend}}{\text{Divisor}} = \text{Quotient} + \frac{\text{Remainder}}{\text{Divisor}}$$

Ex. 3: When dividing by $x - k$ we can use synthetic division.
Divide $4x^3 - 10x^2 - 18x + 10$ by $x - 4$.

$$\begin{array}{r|rrrr}
 4 & 4 & -10 & -18 & 10 \\
 & \downarrow & +16 & +24 & +24 \\
 \hline
 & 4 & 6 & 6 & 34
 \end{array}$$

← makes $x-4=0$

multiplied by 4

Coefficients of the Quotient

Remainder

$$\therefore \text{Quotient} = 4x^2 + 6x + 6$$

$$\text{Remainder} = 34$$

Division Statement:

$$4x^3 - 10x^2 - 18x + 10 = (x - 4)(4x^2 + 6x + 6) + 34$$

Ex. 4: Using synthetic division, find the remainder when $13x - 2x^3 + x^4 - 6$ is divided by $x + 2$.

$$x^4 - 2x^3 + 0x^2 + 13x - 6 \quad \text{and } k = -2$$

$$\begin{array}{r|rrrrr}
 -2 & 1 & -2 & 0 & 13 & -6 \\
 & \downarrow & +4 & -8 & +16 & -6 \\
 \hline
 & 1 & 2 & -8 & 29 & -12
 \end{array}$$

Remainder

Division Statement:

$$x^4 - 2x^3 + 13x - 6 = (x + 2)(x^3 + 2x^2 - 8x + 29) - 12$$

If the remainder is zero, then

👉 we have **factors** of the dividend: divisor and quotient.

Alternate using Long Division and Synthetic Division...

Complete pp.168-170 #5cd, 7ad, 8bc, 9ab, 10ae, 11, 12, 15
Challenge yourself! #17, 18, 19