

LEARNING TARGET:

"I can relate the factors of a trinomial to finding the zeros (x-intercepts) of a parabola."

"I can find the axis of symmetry for a parabola."

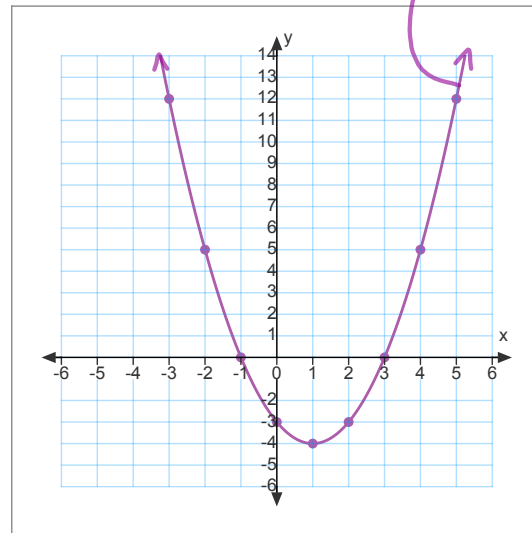
"I can use the equation of the parabola and its axis of symmetry to find the vertex of the parabola."

$$y = x^2 - 2x - 3$$

WHY do we factor parabolas???

Graph the relation, $y = x^2 - 2x - 3$ using a table of values:

x	y = x ² - 2x - 3
-3	$(-3)^2 - 2(-3) - 3 = 12$
-2	$(-2)^2 - 2(-2) - 3 = 5$
-1	$(-1)^2 - 2(-1) - 3 = 0$
0	-3
1	$(1)^2 - 2(1) - 3 = -4$
2	$(2)^2 - 2(2) - 3 = -3$
3	$(3)^2 - 2(3) - 3 = 0$
4	$(4)^2 - 2(4) - 3 = 5$
5	$(5)^2 - 2(5) - 3 = 12$



Now factor the same relation: $y = x^2 - 2x - 3$

$$= (x-3)(x+1)$$

Now set the equation equal to zero and solve for x.

$$A \times B = 0$$

$A=0$ or $B=0$
(or Both)

$$y = (x-3)(x+1)$$

$$0 = (x-3)(x+1)$$

****Notice that if either factor equals zero, the whole expression equals zero.**

$$\begin{array}{l} \downarrow \qquad \qquad \downarrow \\ x-3=0 \qquad x+1=0 \end{array}$$

$$x=3 \quad \text{or} \quad x=-1$$

What do you NOTICE?? (with respect to the graph)

The zeros of the equation, are the x-intercepts on the graph.

can be

A quadratic equation expressed in the form $y = a(x - s)(x - t)$, where $a \neq 0$. In this form, s and t are the zeros or x-intercepts of the graph (parabola) of the relation....SO, this is called **INTERCEPT FORM**.

We can convert from **standard form** to **intercept form** by factoring the trinomial that describes the parabola.

1. Convert the following equations from standard form to intercept form:

a) $y = x^2 + 2x - 8$

$$= (x - 2)(x + 4)$$

b) $y = x^2 - 7x + 12$

$$= (x - 4)(x - 3)$$

2. Now find the zeros (x-intercepts) of each parabola by setting each factor equal to zero:

$$0 = (x - 2)(x + 4)$$

$$x - 2 = 0 \text{ or } x + 4 = 0$$

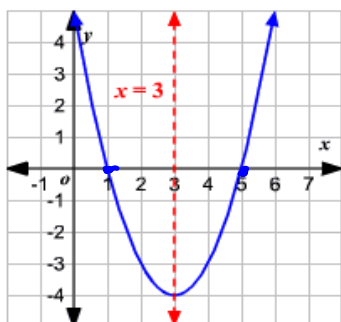
$$x = 2 \text{ or } x = -4$$

$$0 = (x - 4)(x - 3)$$

$$x - 4 = 0 \text{ or } x - 3 = 0$$

$$x = 4 \text{ or } x = 3$$

Parabolas are symmetric (mirror image) about a line that runs vertically through the vertex. We call this line the **AXIS OF SYMMETRY**.



This parabola has an axis of symmetry of $x = 3$.

What are its zeros?

5 and 1

How is the location of the axis of symmetry related to the zeros?

it's half-way between them

Find the axis by:

$$\text{Eq'n of the axis} \quad x = \frac{s+t}{2} = \frac{5+1}{2} \rightarrow x = 3$$

$$x = \frac{2+(-4)}{2}$$

3. For the parabolas $y = x^2 + 2x - 8$ and $y = x^2 - 7x + 12$, find the axis of symmetry

$$\begin{aligned} y &= x^2 + 2x - 8 \\ 0 &= (x + 4)(x - 2) \\ x &= -4 \text{ or } x = 2 \end{aligned}$$

$$\begin{aligned} x &= \frac{-4+2}{2} \\ &= -2/2 \\ x &= -1 \end{aligned}$$

$$y = x^2 + 2x - 8$$

$$y = x^2 - 7x + 12$$

$$0 = (x - 4)(x - 3)$$

$$x = 4 \text{ or } x = 3$$

$$\begin{aligned} \text{Avg} \\ x &= \frac{4+3}{2} \\ &= \frac{7}{2} \\ &= 3.5 \end{aligned}$$

4. Finally, we can find the coordinates of the vertex by substituting the x-value of the axis of symmetry into the equation and solving for y:

$$\begin{aligned} y &= x^2 + 2x - 8 \\ &= (-1)^2 + 2(-1) - 8 \\ &= 1 - 2 - 8 \\ &= -9 \end{aligned}$$

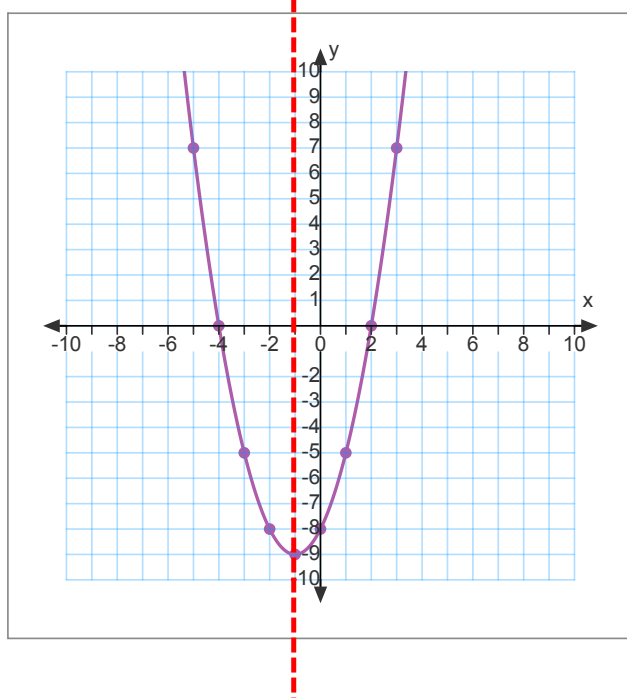
The vertex is at $(-1, -9)$

$$\begin{aligned} y &= (x + 4)(x - 2) \\ &= (-1 + 4)(-1 - 2) \\ &= (3)(-3) \\ &= -9 \end{aligned}$$

HW: p. 281 #1ab, 2ab, 3ab, 4, 5ab, 6

$$y = x^2 + 2x - 8$$

$$x = -1$$



$$y = a(x-h)^2 + k \quad v(h, k)$$

$$y = (x-7)^2 + 3$$

$$v(7, 3)$$

$$y = (x+2)^2 - 8$$

$$v(-2, -8)$$

