

**Before we begin, are there any questions from last day's work?**

pp.217-218 1, 2c, 3d, 4b, 6, 7

***SWYK 2.1 is first.***

**Today's Learning Goal(s):**

By the end of the class, I will be able to:

- a) use a quadratic model to solve a problem with ***and without*** technology.

## 2.8.1 Modeling using Quadratic Functions

Date: Mar. 7/18

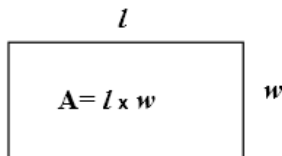
Ex.1

Sixteen metres of fencing are available to enclose a rectangular garden.

- Represent the area of the garden as a function of the length of one side.
- Graph the function.
- What dimensions provide an area greater than  $12 \text{ m}^2$ ?

Solution

- Let  $w$  represent the width of the garden in m.  
Let  $l$  represent the length of the garden in m.



$$P = 2l + 2w$$

$$16 = 2l + 2w$$

$$8 = l + w$$

$$8 - w = l$$

Since  $A = lw$ 

$$0 = (8 - w)w \rightarrow w = 0$$

$$\downarrow$$

$$8 - w = 0$$

$$w = 8$$

b)

the zeros (x-intercepts) are 0 and 8

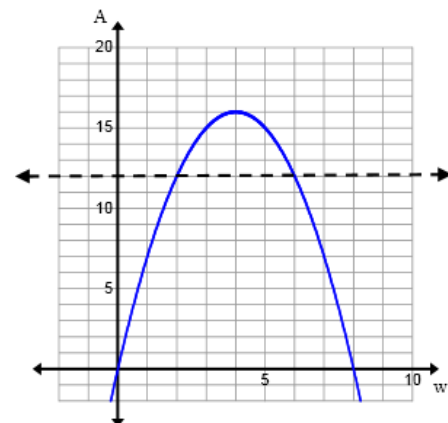
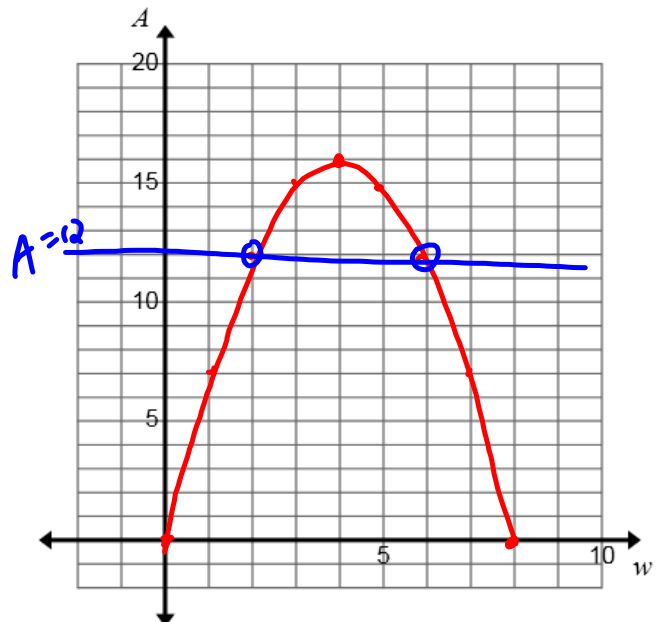
Find the vertex half way between the zeros, or complete the square to get  $A = -1(w-4)^2 + 16$ 

$$\text{if } w = 4 \therefore A = (8-4)(4) = 16 \therefore V(4, 16)$$

$$A = w(8-w)$$

$$= -w^2 + 8w$$

$$\therefore a = -1$$



- Draw in the horizontal line  $y = 12$ .

The intersection points represent the width of the garden when the area is  $12 \text{ m}^2$ .

$\therefore$  if the width is between (but NOT INCLUDING) 2 and 6 m,  
the dimensions provide an area greater than  $12 \text{ m}^2$ .

This is written  $2 < w < 6$ 

$$\text{if c) asked } < 12 \text{ m}^2$$

$$\therefore 0 \leq w < 2 \text{ and } 6 < w \leq 8$$

## 2.8.1 Modeling using Quadratic Functions

Ex. 2

When bicycles are sold for \$300 each, a cycle store can sell 160 in a season.

For every \$25 increase in the price, the number sold drops by 10.

- Represent the sales revenue as a function of the price.
- Use a graphing calculator to graph the function.
- How many bicycles were sold when the total sales revenue is \$33 000?  
What is the price of one bicycle?
- What range of prices will give sales revenue that exceeds \$40 000?

Solution

- The quantities that vary all need to be defined (as variables).

Let  $p$  represent the selling price, in dollars.Let  $n$  represent the number of bicycles sold.Let  $R$  represent the revenue, in dollars.

$$\text{Revenue} = \underset{p}{\text{(price of a bicycle)}} \times \underset{\text{x (needs to be represented as a function of price)}}{\text{(number of bicycles sold)}}$$

(This is the hardest part of this problem.)

Rough work:

- the price increase =  $p - 300$

Check: If the new price is \$375,  
then the price increase =

$$\begin{aligned} & p - 300 \\ &= 375 - 300 \\ &= 75 \end{aligned}$$

- the number of \$25 increases =  $\frac{p-300}{25}$

Check: If the new price is \$375,  
then the number of \$25 increases =

$$\begin{aligned} & \frac{375-300}{25} \\ &= \frac{75}{25} \\ &= 3 \text{ increases of } \$25 \end{aligned}$$

- the number of bicycles sold =  $160 - 10 \left( \frac{p-300}{25} \right)$

$$\begin{aligned} &= 160 - 2 \left( \frac{p-300}{5} \right) \\ &= 160 - \frac{2}{5}(p-300) \\ &= 160 - \frac{2}{5}p + 120 \\ &= -\frac{2}{5}p + 280 \end{aligned}$$

← Show Cancelling

$$\begin{aligned} & -\frac{2}{5}(-300) \\ &= -2(-60) \\ &= 120 \end{aligned}$$

Now, Revenue = (price of a bicycle) x (number of bicycles sold)

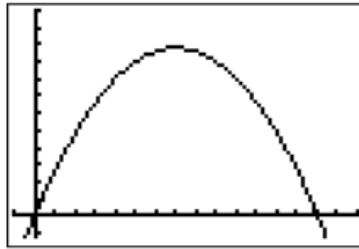
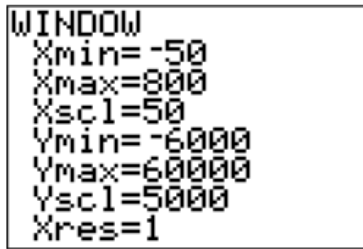
$$= p \left( -\frac{2}{5}p + 280 \right)$$

$$= -\frac{2}{5}p^2 + 280p$$

$$\text{or } (= -0.4p^2 + 280p)$$

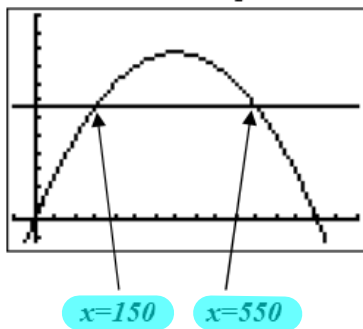
b) Use a graphing calculator to graph the function.

let  $y_1 = -0.4x^2 + 280x$  or  $y_1 = -\frac{2}{5}x^2 + 280x$



c) How many bicycles were sold when the total sales revenue is \$33 000?  
What is the price of one bicycle?

If  $R = 33\ 000$ , let  $y_2 = 33000$



Find the intersection points to represent the price of one bicycle when the revenue is \$33 000.

$\therefore p = 150$  or  $p = 550$

$\therefore$  the price of one bicycle is **\$150** or **\$550**

Recall: Revenue = (price of a bicycle) x (number of bicycles sold)

$\therefore$  number of bicycles sold =  $\frac{\text{Revenue}}{\text{price of a bicycle}}$

if  $p = 150$

number of bicycles =  $\frac{33\ 000}{150}$   
 $= 220$

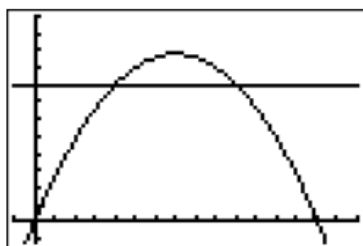
or if  $p = 550$

number of bicycles =  $\frac{33\ 000}{550}$   
 $= 60$

$\therefore$  **60** bicycles were sold if the sales revenue is \$33 000.  
(since the price *increases* will result in lower sales)

d) What range of prices will give sales revenue that exceeds \$40 000?

If  $R = 40\ 000$ , let  $y_3 = 40000$



(Don't forget to "turn off"  $y_2$ )

Find the intersection points to represent the price of one bicycle when the revenue is exactly \$40 000.

$\therefore p = 200$  or  $p = 500$

Because we want when the revenue exceeds \$40 000,  
we DO NOT INCLUDE the intersection points in the solution.

$\therefore$  if  $R > \$40\ 000$ , then  $200 < p < 500$