Today's Learning Goal(s):

By the end of the class, I will be able to:

a) use the Sine Law to solve a triangle that is the ambiguous case.

5.6 The Sine Law

Date: 188

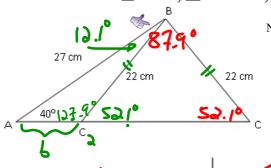
Recall: We use the Sine Law when we are have an "opposite pair". The formula:

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \quad \text{or} \quad \frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

$$\frac{A}{B} = \frac{C}{D}$$

$$AD = BC$$

Ex. 1 Consider \triangle ABC, \angle A = 40°, AB=27 cm, and BC = 22 cm. *Make a sketch*.



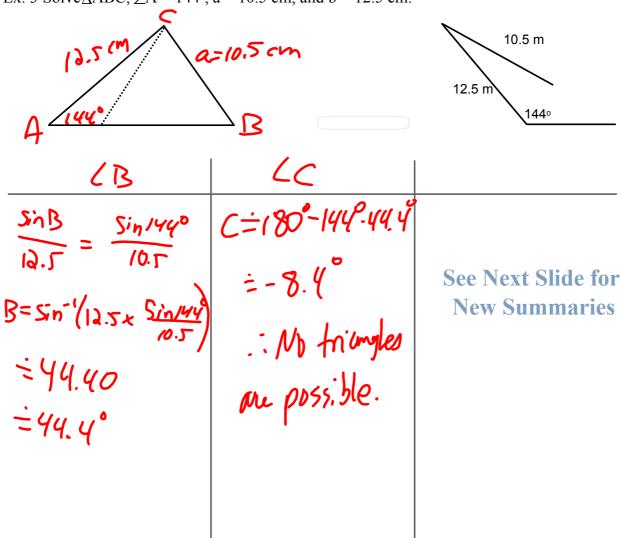
Note: There are 2 different ways to sketch $\triangle ABC$ using this information. This means there are two possible ways to solve this triangle. This is the ambiguous case of the Sine Law.

| | 2.10 c | |
|------------------------|-----------------|-------------------------|
| A 40°(2) 3.9° S21° S | | |
| £ .3 | | |
| <u> </u> | < B | 6 |
| | B=180-40-52.1° | 5in87.9° = 22 5in40° |
| 27 22 | = 87.9° | |
| 22 sinc = 27 sin 40° | | b= sin879°x 22 sin40° |
| Sinc = 27 sin 40° | | ÷34,202 |
| C= 2in_1 (35 2in 100) | | = 34.20 cm |
| ₹25.08 | | |
| = 29.1° < C | CB | 6 |
| C=189,-27°1, | B=1803-40-1279° | 6 = 22 |
| = 19160 | ≐12.1° | Sin12.1° - Sin40° |
| | | b= sin/2.6 x 32 |
| | | 3 3/140 |
| | | =7.174 |
| | | =7.17cm |
| | | |

Ex. 2 Solve \triangle ABC, \angle A = 44.3°, a = 11.5 cm, and b = 7.7 cm.

| . 2 501veдаве, да — 44.5 | , $a = 11.5$ cm, and $b = 7.7$ cm. | |
|------------------------------------|---|---------------------------------|
| 7.7cm 10186/ | 1.5cm | |
| A <u>4483°</u> 27.9° 27 15.67an | 90 | |
| LB | (C | <u></u> |
| | C=180°-44.3°-27.9° = 107.8° | |
| B-Sin-1/7.7x sin443 | | C= 5ih 107.8°x 11.5 5in44.3° |
| = 27.88 | | ≐15.677 |
| =27.9° | | =15.68 (M |
| LB | <i>LC</i> | |
| B=180°-27.9° | C=180°-44.3°-152.1° | |
| =152.10 | = - lb. 4° | |
| | =-16.4° : only 1 triangle possible. | |
| | | |

Ex. 3 Solve \triangle ABC, \angle A = 144°, a = 10.5 cm, and b = 12.5 cm.

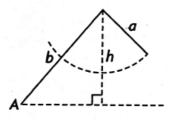


The ambiguous case arises in a SSA (side, side, angle) triangle. In this situation, depending on the size of the given angle and the lengths of the given sides, the sine law calculation may lead to 0, 1, or 2 solutions.

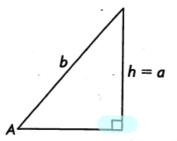
Need to Know

• In the ambiguous case, if $\angle A$, a, and b are given and $\angle A$ is acute, there are four cases to consider. In each case, the height of the triangle is $h = b \sin A$.

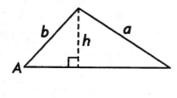
If $\angle A$ is acute and a < h, no triangle exists.



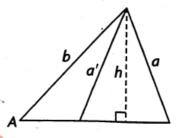
If $\angle A$ is acute and a = h, one right triangle exists.



If $\angle A$ is acute and a > b, one triangle exists.

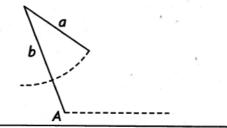


If $\angle A$ is acute and h < a < b, two triangles exist.

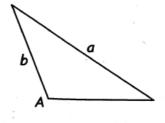


If $\angle A$, a, and b are given and $\angle A$ is obtuse, there are two cases to consider.

If $\angle A$ is obtuse and a < b or a = b, no triangle exists.



If $\angle A$ is obtuse and a > b, one triangle exists.



Are there any Homework Questions you would like to see on the board?

Last day's work: pp. 300-301 #6 – 9ace, 10, 12 [15] Review p. 304 #1 – 13

Today's Homework Practice includes:

pp. 318-319 #1, 2, 3a, 4, 5ac, 7 [15,17]