

Date: _____

Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) calculate the sum of the terms of a geometric series.

Last day's work: pp. 452-453 #(1 – 7)ace, 11, 13 [15,16]

Review:

Sequence: An ordered set of numbers separated by commas .

Each individual number is called a TERM.

The terms are $t_1, t_2, t_3, t_4, \dots, t_n$

Arithmetic Sequence: has a common **difference** between the terms.

In an arithmetic sequence, the first term is a and the common difference is d

$t_1 = a$, and the terms are $a, a+d, a+2d, a+3d, \dots$

The general term is $t_n = a + (n - 1)d$

Geometric Sequence: has a common **ratio** between the terms.

In a geometric sequence, the first term is a and the common ratio is r

$t_1 = a$, and the terms are a, ar, ar^2, ar^3, \dots

The general term is $t_n = ar^{n-1}$

Series: An ordered set of numbers separated by addition and/or subtraction signs .

Each individual number is called a TERM.

But now we have: $t_1 + t_2 + t_3 + t_4 + \dots + t_n$

$$S_1 = t_1 (= a)$$

$$S_2 = t_1 + t_2$$

$$S_3 = t_1 + t_2 + t_3$$

$$S_n = t_1 + t_2 + t_3 + t_4 + \dots + t_n$$

An **Arithmetic Series** is the **sum** of the terms of an arithmetic sequence.

The Arithmetic Series Formula:

$$S_n = \frac{n}{2}[2a + (n-1)d] \quad \text{or} \quad S_n = \frac{n}{2}[t_1 + t_n]$$

where n is the term's position number,

$$a = t_1,$$

d is the common difference, and

$$t_n = \text{last term}$$

7.6 Geometric Series

Date: May 31/18

A **Geometric Series** is the **sum** of the terms of a geometric sequence.

Ex.1 Your grandma agrees to give you 1 cent on Dec.1, 2 cents on Dec.2, 4 cents on December 3, etc. until Christmas Day.
What will be your total sum?

$$t_n = ar^{n-1} \quad t_{25} = (1)(2)^{25-1} = 2^{24}$$

$$\begin{aligned}
 S_{25} &= 1 + 2 + 4 + 8 + \dots + 2^{23} + 2^{24} \quad \textcircled{1} \\
 \textcircled{2} \quad (multiply\ by\ "r") \quad 2S_{25} &= \quad 2 + 4 + 8 + \dots + 2^{23} + 2^{24} + 2^{25} \\
 \textcircled{3} \quad (subtract\ up) \quad \hline
 \textcircled{4} \quad 2S_{25} - S_{25} &= 2^{25} - 1 \\
 \textcircled{5} \quad S_{25} &= 2^{25} - 1 \\
 &= 33554431 \text{ cents} \quad \textcircled{6} \\
 &= \$335\,544.31 \\
 &\quad \text{Thank you grandma!}
 \end{aligned}$$

In general:

$$\begin{array}{l}
 S_n = a + ar + ar^2 + \dots + ar^{n-2} + ar^{n-1} \\
 \textcircled{2} \quad rS_n = ar + ar^2 + \dots + ar^{n-2} + ar^{n-1} + ar^n \\
 \textcircled{3} \quad S_n = a + ar + ar^2 + \dots + ar^{n-2} + ar^{n-1} \\
 \textcircled{4} \quad \text{(subtract)} \\
 \textcircled{5} \quad rS_n - S_n = ar^n - a \\
 \textcircled{6} \quad \text{(factor both sides)} \\
 (r-1)S_n = a(r^n - 1)
 \end{array}$$

$ar^{n-1} \cdot r = ar^n$
 $ar^{n-1} + ar^n$ Same
 $t_n = ar^{n-1}$

The Geometric Series Formula:

$$S_n = \frac{a(r^n - 1)}{r - 1}, \quad r \neq 1$$

where n is the term's position number,

$a = t_1$, and

r is the common ratio

Ex.2 Find S_{10} for $5 + 15 + 45 + \dots$

g. series $t_n = ar^{n-1}$ $S_n = \frac{a(r^n - 1)}{r - 1}$

$S_{10} = 147\,620$

$r = 3$

$a = 5$

$n = 10$

$S_{10} = \frac{5(3^{10} - 1)}{3 - 1}$

$= \frac{5(3^{10} - 1)}{2}$

$= 147\,620$

Ex.3 Find the sum of: $3 - 6 + 12 - 24 + \dots + 768$

$n = 9$

g series

$S_n = \frac{a(r^n - 1)}{r - 1}$

$t_n = ar^{n-1}$ $S_9 = 513$

$r = -2$

$a = 3$

$n = 9$

$S_9 = \frac{3((-2)^9 - 1)}{-2 - 1}$

$= \frac{3((-2)^9 - 1)}{-3}$

$= 513$

$t_n = 3(-2)^{n-1}$

$768 = 3(-2)^{n-1}$

$\frac{768}{3} = (-2)^{n-1}$

$256 = (-2)^{n-1}$

$\therefore n = 9$

$2^? = 256$

$? = 8$

$\therefore 2^8 = 256$

$(-2)^8 = 256$

Are there any Homework Questions you would like to see on the board?

Last day's work: pp. 452-453 #(1 – 7)ace, 11, 13 [15,16]

Today's Homework Practice includes:
pp. 459-461 #(1 – 6)ace, 9, 11, 13 [16,18]