

Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) activate prior knowledge of exponential functions.
- b) determine through investigation with graphing software ([desmos](#)) the impact of changing the base on the graph of an exponential function.
- c) determine through investigation with graphing software, the impact of changing the sign of the exponent on the graph of an exponential function.

Unit 1: Exponential Functions

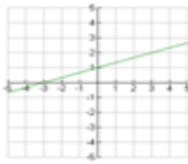
1.1.1 Do You Remember When?

Date: Sept. 5 / 18

Anticipation Guide

Instructions:

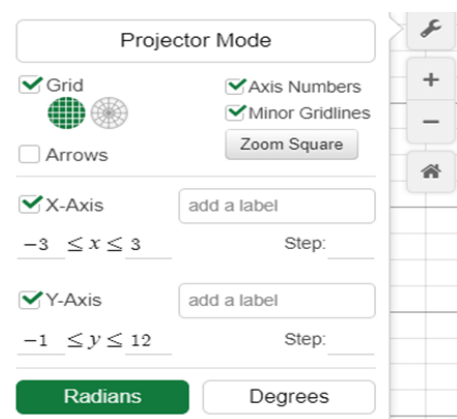
- Compare your choice and explanation with a partner.
- Revisit your choices at the end of the task.
- Compare the choices that you would make *after* the task with the choices that you made before the task.

Before		Statement	After	
Agree	Disagree		Agree	Disagree
10	2	1 ^{not function} 1. All of the following are functions. i. $x = y^2$ x ii. $y = 2x^2 - 5$ ✓ iii. $y = \frac{x}{4} + 7$ ✓ iv. $y = 3^x$ ✓ v. $2x + 3y - 5 = 0$ ✓	13	0 ✓
0	12	2. The base of $y = 2^x$ is x .	0	13 ✓
4	8	3. Audrey is paid \$10/hour. The growth of her earnings over the week is an example of exponential growth. <i>linear</i>	0	13 ✓
0	12	4. $y = 3^x$ is the same as $y = x^3$.	0	13 ✓
0	10	5. The area, y , of a square floor with one side measuring x can be modelled by the equation $y = 2^x$ <i>$y = x^2$</i>	0	13 ✓
2	11	6. If $x = 0$ in the relation $y = 5^x$, then $y = 0$. <i>$y = 1$</i>	0	13 ✓
6	6	7. For the function on the grid, the x-intercept is -3 and the y-intercept is 1. 	3 ✓	10
9	2	8. $y = \left(\frac{1}{5}\right)^x$ is an exponential function.	13 ✓	0
10	2	9. The domain of $y = 2^x$ is $\{x \in R\}$	13 ✓	0
5	7	10. The range of $y = 10^x$ is $\{y \in R / y > 0\}$.	3 ✓	10

1.1.2 The Graphs of Exponential Functions

Date: Sept. 5 / 18

Step 1:

Using **desmos**, adjust to the following window settings.

Step 2:

Each of the equations is in the form: $y = b^x$

For each part of the investigation graph the given equations on the same axes.

Sketch the graphs on the grid provided.

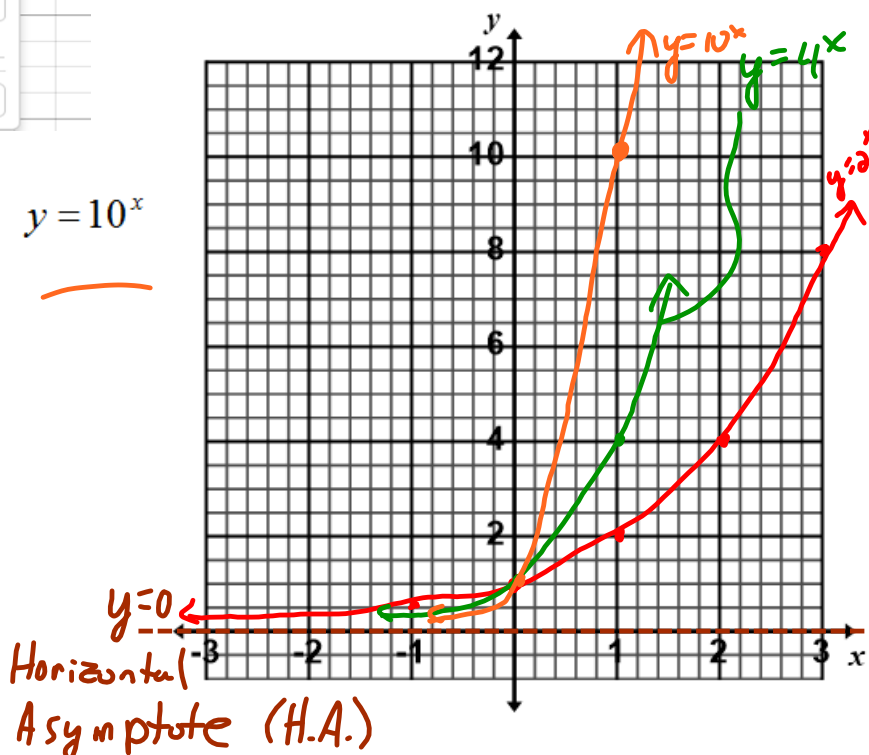
Complete the chart that follows.

Part 1:

$y = 2^x$

$y = 4^x$

$y = 10^x$



$y = 2^x$	$y = 4^x$	$y = 10^x$
y-intercept is 1	y-intercept is 1	y-intercept is 1
x-intercept is none	x-intercept is none	x-intercept is none
function is increasing , decreasing or neither (circle one)	function is increasing , decreasing or neither (circle one)	function is increasing , decreasing or neither (circle one)
Domain is: $\{x \in R\}$	Domain is: $\{x \in R\}$	Domain is: $\{x \in R\}$
Range is: $\{y \in R / y > 0\}$	Range is: $\{y \in R / y > 0\}$	Range is: $\{y \in R / y > 0\}$

1. Describe what these graphs have in common.

- ☞ Same y-intercept (zero exponent rule)
- ☞ all are increasing (up to the right)
- ☞ $y > 0$, $\therefore y = 0$ (the x-axis) is a horizontal asymptote

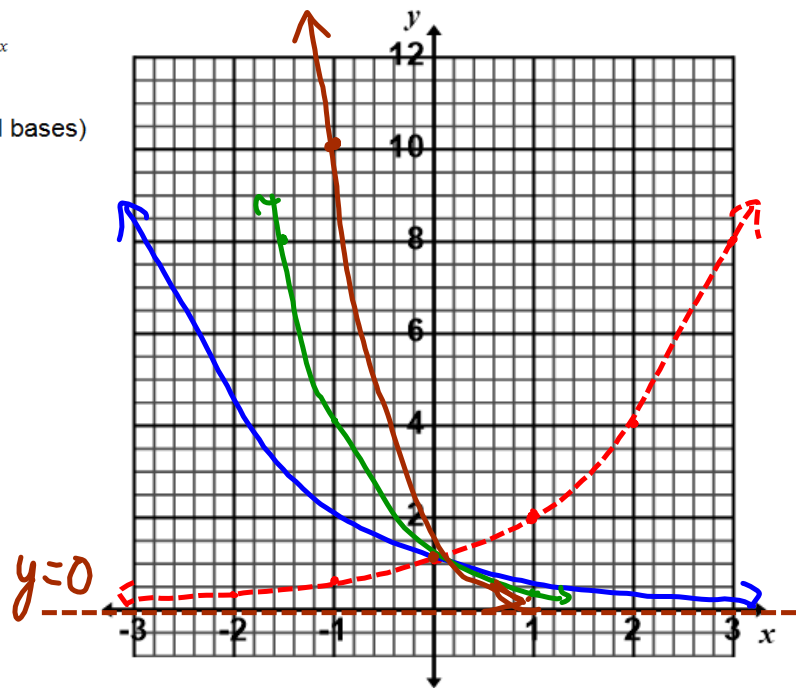
2. Describe the impact of changing the base on the graph of an exponential function.

- ☞ As "b" increases, the function increases more quickly

Part 2:

$$y = 2^x \quad y = \frac{1}{2}^x \quad y = \frac{1}{4}^x \quad y = \frac{1}{10}^x$$

(Consider putting brackets around the fractional bases)



$y = \frac{1}{2}^x$	$y = \frac{1}{4}^x$	$y = \frac{1}{10}^x$
y-intercept is 1	y-intercept is 1	y-intercept is 1
x-intercept is NONE	x-intercept is NONE	x-intercept is NONE
function is increasing, <u>decreasing</u> or neither (circle one)	function is increasing, <u>decreasing</u> or neither (circle one)	function is increasing, <u>decreasing</u> or neither (circle one)
Domain is: $\{x \in R\}$	Domain is: $\{x \in R\}$	Domain is: $\{x \in R\}$
Range is: $\{y \in R / y > 0\}$	Range is: $\{y \in R / y > 0\}$	Range is: $\{y \in R / y > 0\}$

3. Describe what these graphs have in common.

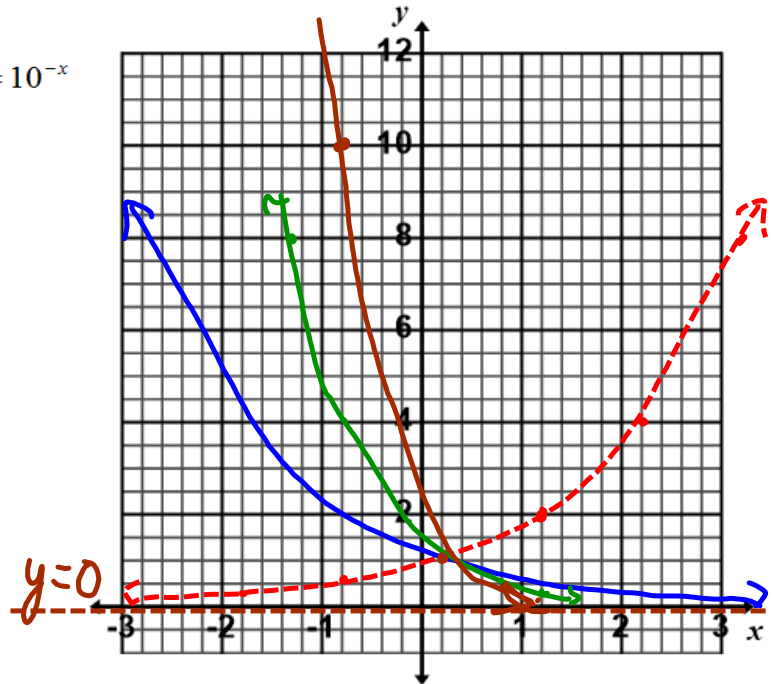
- 👉 Same y-intercept (zero exponent rule)
- 👉 all are decreasing (down to the right)
- 👉 $y > 0$; $y = 0$ (the x-axis) is a horizontal asymptote

4. Describe the impact of changing the base on the graph of an exponential function.

- 👉 When $0 < b < 1$, decreasing the base has the function decrease more quickly

Part 3:

$$y = 2^x \quad y = 2^{-x} \quad y = 4^{-x} \quad y = 10^{-x}$$



$y = 2^{-x}$	$y = 4^{-x}$	$y = 10^{-x}$
y-intercept is 1	y-intercept is 1	y-intercept is 1
x-intercept is NONE	x-intercept is NONE	x-intercept is NONE
function is increasing, <u>decreasing</u> or neither (circle one)	function is increasing, <u>decreasing</u> or neither (circle one)	function is increasing, <u>decreasing</u> or neither (circle one)
Domain is: $\{x \in R\}$	Domain is: $\{x \in R\}$	Domain is: $\{x \in R\}$
Range is: $\{y \in R / y > 0\}$	Range is: $\{y \in R / y > 0\}$	Range is: $\{y \in R / y > 0\}$

5. Describe what these graphs have in common with the graphs in part 2.

👉 They represent the same functions. (due to the negative exponent rule)

👉 $y = 2^{-x}$

$$= \left(\frac{1}{2}\right)^x$$

6. Describe the impact of changing the sign of the exponent on the graph of an exponential function.

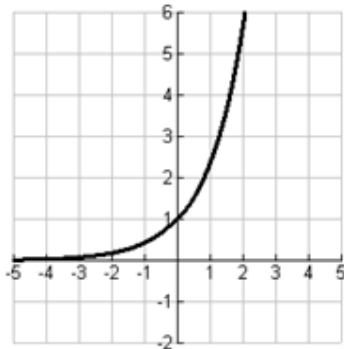
👉 Changing the sign of the exponent changes an exponential function from increasing (growth) to decreasing (decay), or vice versa.

1.1.3 Matching Activity

Date: _____

Match each graph with an equation that best represents the relationship.

For each graph, state the x-intercept, y-intercept, domain, range, and whether the graph is increasing, decreasing or neither.

Equations: i) $y = 3^{-x}$ ii) $y = \left(\frac{1}{4}\right)^x$ iii) $y = 5^{-x}$ iv) $y = 2.4^x$ v) $y = 5.5^x$ vi) $y = 3.4^x$ 

a) Equation:

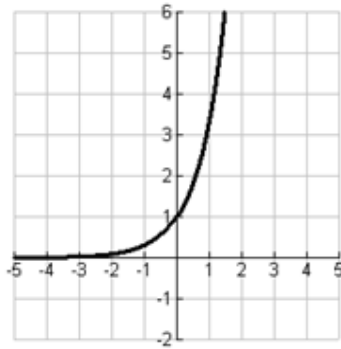
y-intercept is

x-intercept is

function is increasing, decreasing or neither (circle one)

Domain is:

Range is:



b) Equation:

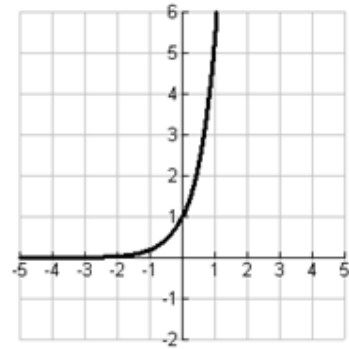
y-intercept is

x-intercept is

function is increasing, decreasing or neither (circle one)

Domain is:

Range is:



c) Equation:

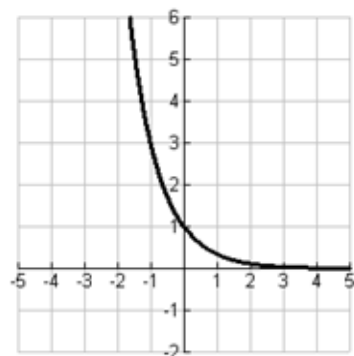
y-intercept is

x-intercept is

function is increasing, decreasing or neither (circle one)

Domain is:

Range is:



d) Equation:

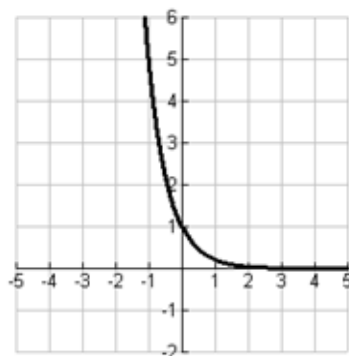
y-intercept is

x-intercept is

function is increasing, decreasing or neither (circle one)

Domain is:

Range is:



e) Equation:

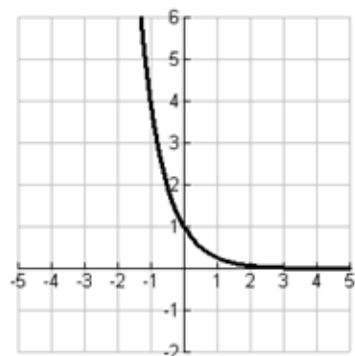
y-intercept is

x-intercept is

function is increasing, decreasing or neither (circle one)

Domain is:

Range is:



f) Equation:

y-intercept is

x-intercept is

function is increasing, decreasing or neither (circle one)

Domain is:

Range is: