Before we begin, are there any questions from last day's work?

Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) make connections between polynomials given in factored form, and the *x*-intercepts of the graph of the polynomial.
- b) identify the zeros of a function or the roots of the corresponding equation and the connection between the two.

Be ready for Unit 2 Summave Tomorrow!!

| 3 | .1. | .1: | Up | to | Now | With | Poly | ynomi | als |
|---|-----|-----|----|----|-----|-------|------|-------|-----|
| _ | | | _ | | | – – – | | , | |

| Date: | | | |
|-------|--|--|--|

Anticipation Guide

Instructions:

- Check "Agree" or "Disagree" beside each statement *before* you start the task.
- Compare your choice and explanation with a partner.
- Revisit your choices after completing the <u>Part C</u> on BLM 3.1.2. Compare the choices you made before the task and after the task.

| Before | | Statament | | After | |
|--------|-----------|--|-------|----------|--|
| Agree | Disagree | Statement | Agree | Disagree | |
| | 15 | The zeros are the y-intercepts on a given graph. | | | |
| 12 | 3 | The solutions of an equation and the zeros of a function are the same thing. | | | |
| 14 | | 3. $x^2 + 5x + 6$ is $(x+3)(x+2)$ in factored form. | | | |
| 6 | \otimes | 4. All parabolas have at least one root/solution. | | | |
| 2 | 13 | 5. The degree of the polynomial $y = 3x^2 - 6x^3 - 2$ is 5. | | | |
| () | 3 | 6. The function $y = (x - 4)(x + 5)$ has two real solutions/roots. | | | |
| 10 | 4 | 7. The function $y = (x - 4)(x - 4)$ has one real solution/root. | | | |
| | 14 | 8. The graph of $y = -7x^3 - 1$ is linear. | | | |
| 14 | | All cubic functions have at least one root/solution. | | | |

3.1.2: Getting to Know Polynomials

✓ X-Axis Date: 0c+10//8

Part A: Before you begin, change your window settings to:

 $-10 \le x \le 10$

- 1. For each function in the chart below, do the following:
 - Set the function equal to zero and solve.
 - Sketch a graph of the function.
 - Determine the x-intercept

✓ Y-Axis

$$-24 \le y \le 20$$

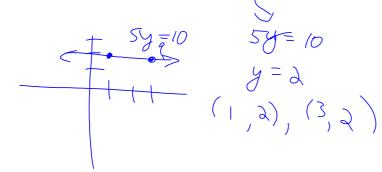
| • Determine the x- | interoept. | $-24 \le y \le 20$ | | |
|--------------------|---|--------------------|-------------|--|
| Function | Solution when y = 0 | Sketch | x-intercept | |
| y = 2x + 16 | (0)=2x+16 -2x=16 x=-8 | | -8 | |
| 5x + 2y - 20 = 0 | 5x+2(0)-20=0 5x-20=0 5x=20 x=4 | | 4 | |
| y = -6(x+3) | (0) = -6(x+3) 0 = x+3 x = -3 | | -3 | |

2. Compare your answer for the solutions to the *x*-intercepts. What do you notice?

The x-intercept is the solution when y=0.

3. If you were given the function 5y = 10, how many x-intercepts would it have? Justify your answer.

Zero. Make a quick sketch.



Part B: Use the same window settings as in Part A to complete the chart below.

| Function | Solution when y = 0 | Sketch | x-intercept |
|--|---|--------|------------------|
| Recall: If $A \times B = 0$ A B $y = -2(x - 4)(x + 1)$ | $(0) = -2(x-4)(x+1)$ $\therefore x-4=0 \text{ or } x+1=0$ $x=4 \text{ or } x=-1$ | | 4,-1 |
| y = -4.9(x - 2) ² | $(0) = -4.9(x-2)^{2}$ $\therefore x-2=0 \text{ or } x-2=0$ $x=2 \text{ or } x=2$ | | 2 |
| y = x ² + x - 20 | $y = (x-4)(x+5)$ $(0) = (x-4)(x+5)$ $\therefore x-4=0 \text{ or } x+5=0$ $x=4 \text{ or } x=-5$ | | 4,-5 |
| $y = x^{2} + 4x - 10$ $y = (x + 2)^{2} - 20$ | $y = x^{2}+4x+2^{2}-2^{2}-16$ $y = x^{2}+4x+4(4-16)$ $(0) = (x+2)^{2}-20$ $20 = (x+2)^{2}$ $\pm \sqrt{20} = x+2$ $x=-2+\sqrt{20}$ $x=-2\pm 4.472$ $\therefore x=2.472 \text{ or } x=-6.472$ | | 2.472 , -6.472 |
| $y = x^{2} + 6x + 10$ $y = (x + 3)^{2} + 1$ v(-3, 1) | $y = x^{2}+6x+3^{2}-3^{2}+10$ $y = x^{2}+6x+9-9+10$ (0) =(x+3) ² +1 -1 =(x+3) ² ±√-1 =x+3 ∴ no Real roots | | no Real roots |

4. Which form of a quadratic function is easier to use for solving algebraically?

□ Factored form □ Standard form (choose one). Give reasons.

| $-150 \le y \le 50$ | | | | | |
|---|--|--------|--------------|--|--|
| Function | Solution when y = 0 | Sketch | x-intercept | | |
| y = (x - 6)(x + 2)(x + 5) | $(0) = (x-6)(x+2)(x+5)$ $\therefore x-6=0 \text{ or } x+2=0 \text{ or } x+5=0$ $x=6 \text{ or } x=-2 \text{ or } x=-5$ | 7 | 6 , -2, -5 | | |
| y = -2(x - 3)(x +1)(x - 5) | | | | | |
| y = (x - 2) ² (x + 2) | | | | | |
| y = (x + 4) ³ | | | | | |
| $y - x^{2} - x^{2} - 6x$ $= x(x^{2} - x - 6)$ $= x(x - 3)(x + 2)$ | If $y = 0$ $0 = x(x-3)(x+2)$ $x = 0$ $x = 3$ $x = -2$ | | x = 0, 3, -2 | | |

3.1.3: The Root of All Knowledge

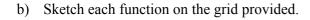
Date:

1. On a test, students were asked to determine the roots of $y = x^2 + 4x - 60$

| Michael's solution | Susie's solution | Jaspal's solution |
|---------------------|---------------------|----------------------|
| $y = x^2 + 4x - 60$ | $y = x^2 + 4x - 60$ | $y = x^2 + 4x - 60$ |
| y = (x-6)(x+10) | y = (x+6)(x-10) | y = (x-6)(x+10) |
| 0 = (x-6)(x+10) | 0 = (x+6)(x-10) | 0 = (x - 6)(x + 10) |
| x = 6 and $x = -10$ | x = 6 and $x = -10$ | x = -6 and $x = +10$ |

- a) Whose solution is correct?
- b) Explain what was done in the correct solution.
- c) Explain what was done incorrectly in the other two solutions.

2. a) Create a linear, quadratic, cubic and quartic function that has the x-intercept of x = 3.



c) Compare and contrast the functions.(i.e. What is the same and what is different about the functions?)

