

- p. 185 18. a) Factor the expression $x^6 - y^6$ completely by treating it as a difference of squares.
 b) Factor the same expression by treating it as a difference of cubes.

$$\begin{aligned}
 \text{a) } x^6 - y^6 & \quad \left\{ \begin{array}{l} x^2 - y^2 \\ x^3 - y^3 \end{array} \right. \\
 & = (x^3 - y^3)(x^3 + y^3) = (x - y)(x + y) \\
 & = (x - y)(x^2 + xy + y^2)(x + y)(x^2 - xy + y^2)
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } x^6 - y^6 & \\
 & = (x^2)^3 - (y^2)^3 \\
 & = (x^2 - y^2)(x^2 + x^2 y^2 + y^2) \\
 & = (x - y)(x + y)(x^2 + x^2 y^2 + y^2)
 \end{aligned}$$

- p. 186 5. During which intervals of x is the graph of the function $f(x) = -(x+3)(x+5)(x-1)$ below the x -axis?

Zeros: $-3, -5, 1$

Order: $1, 1, 1$

$$f(0) = -(3)(5)(-1) \\ = 15$$



- p. 186 9. The function $f(x) = ax^4 + 8x^2$ has three turning points, an absolute maximum of 8, and one of its zeros at $x = 2$. Determine the value of a and the location of the other zeros. Then sketch the graph of $f(x)$.

$$f(x) = (x-2) \cdot g(x)$$

$$f(x) = ax^4 + 8x^2$$

$$f(2) = a(2)^4 + 8(2)^2$$

$$0 = 16a + 32$$

$$-16a = 32$$

$$a = -2$$

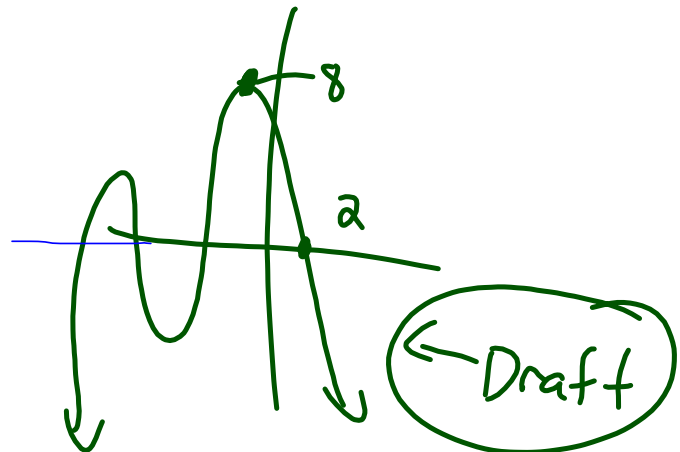
$$\therefore f(x) = -2x^4 + 8x^2$$

$$= -2x^2(x^2 - 4)$$

$$= -2x^2(x-2)(x+2)$$

Zeros: 0, 2, -2

order: 2, 1, 1



$$\begin{array}{r|rrrrr} 2 & -2 & 0 & 8 & 0 & 0 \\ & \downarrow & -4 & -8 & 0 & 0 \\ \hline & -2 & -4 & 0 & 0 & 0 \end{array}$$

$$\therefore f(x) = (x-2)(-2x^3 - 4x^2) \quad R$$

$$= (x-2)(-2x^2)(x+2)$$

