

4.3 Solving Polynomial Inequalities (Day 2)

**Math Learning Target:**

"By the end of class, I can solve any polynomial inequality."

Ex. 1: For the functions $f(x)$ and $g(x)$,
determine graphically the intervals for:

a) $f(x) > g(x)$

$$(-1, 1) \cup (2, \infty)$$

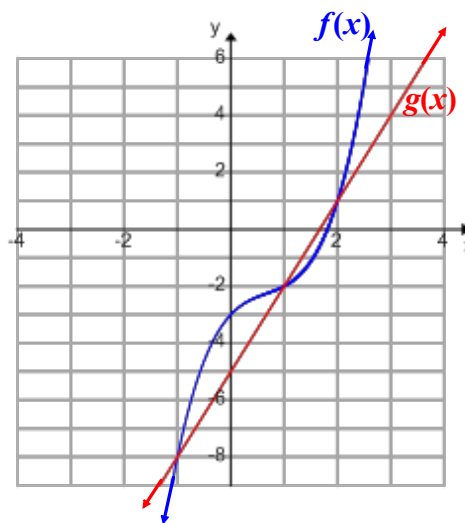
b) $g(x) > f(x)$ or $f(x) < g(x)$

$$(-\infty, -1) \cup (1, 2)$$

c) $f(x) = g(x)$

$$x = -1, 1, 2$$

$$\text{or } [-1, -1] \cup [1, 1] \cup [2, 2]$$



Entertainment: **Do #7 first...**pp.227-228 #7*ef, 3, 8, 9, 12**, 13**, 14, 15

Challenge: #18

* use **desmos** to confirm your answers;

** the text has answers rounded in the back, but you must state your answers as exact values

Ex. 2: Determine the intervals for $g(x) < f(x)$ given that

$$f(x) = x^4 - 5x^3 + 4x^2 + 17x - 40$$

$$g(x) = 2x^3 - 5x^2 - 10x + 14$$

$$g(x) < f(x)$$

$$2x^3 - 5x^2 - 10x + 14 < x^4 - 5x^3 + 4x^2 + 17x - 40$$

$$\begin{aligned} 2x^3 - 5x^2 - 10x + 14 - x^4 + 5x^3 - 4x^2 - 17x + 40 < 0 \\ \underline{\underline{-x^4 + 7x^3 - 9x^2 - 27x + 54}} < 0 \end{aligned}$$

$$\begin{aligned} \text{Let } P(x) &= -x^4 + 7x^3 - 9x^2 - 27x + 54 \\ &= -(x^4 - 7x^3 + 9x^2 + 27x - 54) \end{aligned}$$

Find when $P(x) = 0$

$$P(-2) = 0$$

$$\begin{array}{r|rrrrr} -2 & 1 & -7 & 9 & 27 & -54 \\ & \downarrow & & & & \\ & & -2 & 18 & -54 & 54 \\ \hline & 1 & -9 & 27 & -27 & 0 \end{array} \text{OR}$$

$$\begin{array}{r|rrrr} 3 & 1 & -9 & 27 & -27 \\ & \downarrow & & & \\ & & 3 & -18 & 27 \\ \hline & 1 & -6 & 9 & 0 \end{array} \text{OR}$$

$$\begin{aligned} P(x) &= -(x+2)(x^3 - 9x^2 + 27x - 27) \\ &= -(x+2)(x-3)(x^2 - 6x + 9) \\ &= -(x+2)(x-3)(x-3)(x-3) \end{aligned}$$

$$P(x) = -(x+2)(x-3)^3$$

Zeros: $-2, 3$

Order: $1, 3$

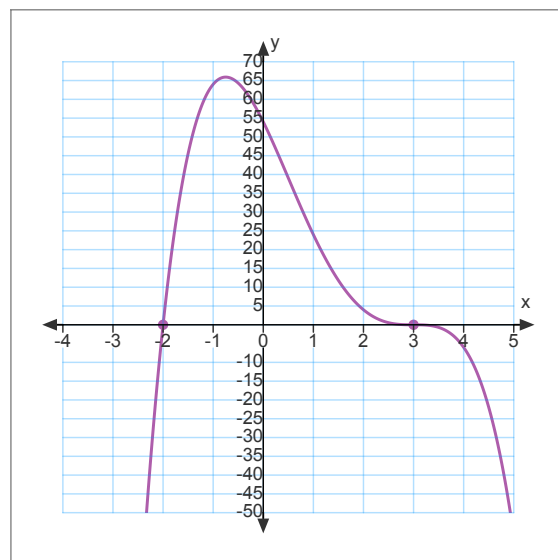
$$-(x+2)(x-3)^3 < 0$$

$x < -2$	$-2 < x < 3$	$x > 3$
$-(-)(-)$	$-(+)(-)$	$-(+)(+)$
$= -$	$= +$	$= -$
Yes!	NO!	Yes!

$$\therefore (-\infty, -2) \cup (3, \infty)$$

$$y = x^4 - 5x^3 + 4x^2 + 17x - 40$$

$$y = 2x^3 - 5x^2 - 10x + 14$$



$$y = -x^4 + 7x^3 - 9x^2 - 27x + 54$$

$y =$

Last Day's Work:

Entertainment: Use a chart to organize your solution instead of a "number line strategy".
pp. 225-228 #1ab, 2, 5, 6*, 7abc, Challenge #17

Error in answer for 6e. The answer should be: $x \leq \frac{-3}{2}$ or $x \geq 3$

p. 225 1. Solve each of the following using a number line strategy. Express your answers using set notation.

a) $(x + 2)(x - 3)(x + 1) \geq 0$

b) $-2(x - 2)(x - 4)(x + 3) < 0$

$$x = 2, 4, -3$$

$x < -3$	$-3 < x < 2$	$2 < x < 4$	$x > 4$
$-(-)(-)(-)$	$-(-)(-)(+)$	$-(+)(-)(+)$	$-(+)(+)(+)$
+	-	+	-
No	Yes	No	Yes

$$\therefore (-3, 2) \cup (4, \infty)$$

$$\{x \in \mathbb{R} \mid -3 < x < 2 \text{ or } x > 4\}$$

p. 227 7. Solve the following inequalities algebraically. Confirm your answer with a graph.

a) $x^2 - 6x + 9 \geq 16$

b) $x^4 - 8x < 0$

b) $x^4 - 8x < 0$

$$x(x^3 - 8) < 0$$

$$x(x-2)(x^2 + 2x + 4) < 0$$

\therefore Zeros: 0, 2

order: 1, 1

$x < 0$	$0 < x < 2$	$x > 2$
$(-)(-)(+)$	$(+)(-)(+)$	$(+)(+)(+)$
$= +$	$= -$	$= +$
NO	Yes	NO.

$\therefore (0, 2)$

or $\{x \in \mathbb{R} / 0 < x < 2\}$