

Before we begin, are there any questions from last day's work? [4.3.3](#)

## Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) state the key properties of the sine and cosine functions.
- b) perform horizontal and vertical translations of the sine and cosine functions.

## 4.4.1 The Sine and Cosine Functions: Key Properties

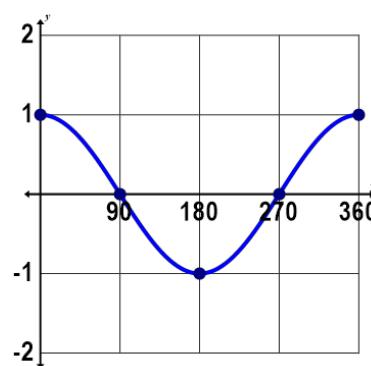
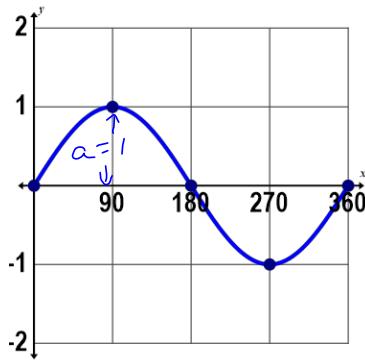
Last day we created the graphs of:

Date: Oct. 30/18

a)  $y = \sin x$

and

b)  $y = \cos x$



Key Properties

Domain:  $\{x \in \mathbb{R}\}$

Maximum Value: 1

Minimum Value: -1

Range:  $\{y \in \mathbb{R} | -1 \leq y \leq 1\}$

Intercepts:  $0^\circ, 180^\circ, 360^\circ$

Amplitude: 1 (always positive)

Period:  $360^\circ$

Increasing Interval:  $0^\circ \leq x \leq 90^\circ, 270^\circ \leq x \leq 360^\circ$

Decreasing Interval:  $90^\circ \leq x \leq 270^\circ$

Key Properties

Domain:  $\{x \in \mathbb{R}\}$

Maximum Value: 1

Minimum Value: -1

Range:  $\{y \in \mathbb{R} | -1 \leq y \leq 1\}$

Intercepts:  $90^\circ, 270^\circ$

Amplitude: 1

Period:  $360^\circ$

Increasing Interval:  $180^\circ \leq x \leq 360^\circ$

Decreasing Interval:  $0^\circ \leq x \leq 180^\circ$

## 4.4.2 Investigating Horizontal and Vertical Translations

Using **desmos**, change your window settings to:

(Be certain to change to Degrees)

*(You don't need to type the degree symbol in Desmos.)*

A. Comparing  $y = \sin(x - d)$  to  $y = \sin x$

1. Enter  $y = \sin x$ , then:

a) Enter  $y = \sin(x - 60^\circ)$ . Describe the transformation relative to  $y = \sin x$ .

b) Sketch  $y = \sin(x - 60^\circ)$  on the grid on the top left of the next page.

X-Axis add a label

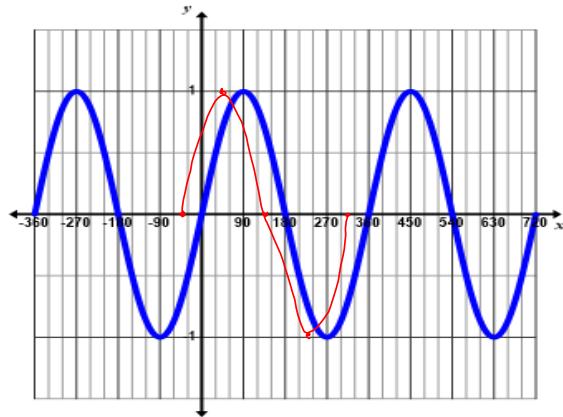
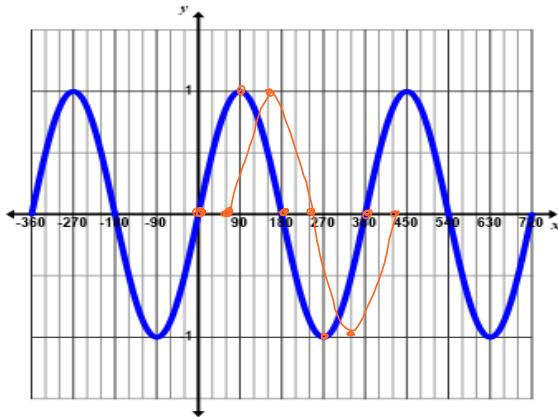
$-360^\circ \leq x \leq 720^\circ$  Step: 30

Y-Axis add a label

$-2 \leq y \leq 2$  Step: \_\_\_\_\_

Radians Degrees

translated  $60^\circ$  to the right



c) Turn off  $y = \sin(x - 60^\circ)$ . Enter  $y = \sin(x + 45^\circ)$ , then sketch it on the grid (above right). Describe this transformation relative to  $y = \sin x$ .

translated  $45^\circ$  to the left

d) Experiment with different values of  $d$ .  
Try  $y = \sin(x - 25^\circ)$ ,  $y = \sin(x + 70^\circ)$ , etc.

If time permits, repeat the above, but replace all sin with cos. All else is the sa

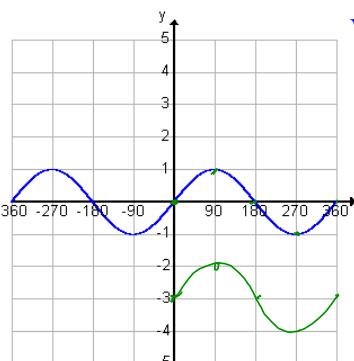
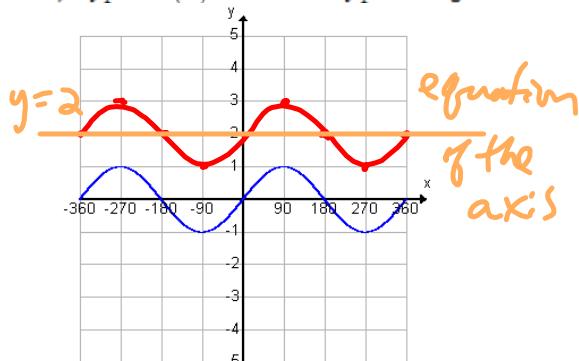
B. Comparing  $y = \sin x + c$  to  $y = \sin x$

Modify the WINDOW settings:

<input checked="" type="checkbox"/> X-Axis	add a label
$-360 \leq x \leq 360$	Step: 90
<input checked="" type="checkbox"/> Y-Axis	add a label
$-5 \leq y \leq 5$	Step: _____
Radians <input checked="" type="radio"/> Degrees	

1. On the calculator, enter  $y_1 = \sin x$ , then :

- a)  $y_2 = \sin(x) + 2$ . Sketch  $y_2$  on the grid below. Describe the transformation relative to  $y = \sin x$ .



v.t. up 2 units

vertical translation up 2

- b) Turn off  $y_2$ . Enter  $y_3 = \sin(x) - 3$ , then sketch it on the grid (above right).

Describe this transformation relative to  $y = \sin x$ .

vertical translation down 3

- c) Experiment with different values of  $c$ .

Try  $y = \sin(x) - 1$ ,  $y = \sin(x) + 2.5$ , etc.

If time permits, repeat the above, but replace all sin with cos. All else is the same

### Summary

The graph of the function  $y = \sin(x - d) + c$  is congruent to the graph of  $y = \sin x$ .

The differences are only in the placement of the graph.

Move the graph of  $y = \sin x$ :

$d^\circ$  to the left when  $d < 0$ .  $\leftarrow$

$d^\circ$  to the right when  $d > 0$ .  $\rightarrow$

$\text{ex } d = -30^\circ$   $c$  units up when  $c > 0$ .  $\uparrow$

$x - (-30^\circ) = (x + 30^\circ)$   $c$  units down when  $c < 0$ .  $\downarrow$

A vertical translation affects the range of the function,

but has no effect on the period, amplitude, or domain.

A horizontal translation slides a graph to the left or right,

but has no effect on the period, amplitude, domain, or range.