8.5 Solving Exponential Equations

"I can solve and check any equation that contains exponential expressions.

I can apply what I have learned in unfamiliar settings."

The formula to calculate the mass, M(t), remaining from an original sample of a substance with mass P_0 , can be determined using the formula:

$$M(t) = P_0 \left(\frac{1}{2}\right)^{\frac{t}{h}}$$
, where *t* is time, and *h* is the half-life.

Recall:

the half-life of a substance is the amount of time required to reduce its mass by one-half.

Ex. 1: Jocelyn works in a lab that uses radioactive substances.

The lab received a shipment of 200 g of radioactive iodine and after 7 days, 55.8163 g of the iodine was still remaining.

Calculate the half-life, to the nearest tenth of a day, ofradioactive iodine.

Ex. 2: Solve $5^{x+1} = 7^{x-2}$, to three decimal places.

Ex. 3: Solve $25(2^x) = 150$, to three decimal places.

Ex. 4: Solve algebraically: $9^{x+1} = \frac{1}{27}$

Ex. 5: Solve algebraically: $3^{x+2} - 3^{x+1} = 162$