

## 8.6 Solving Logarithmic Equations



"I can solve and check any equation with logarithmic expressions.  
I also know what the restrictions are in an equation."

**Recall:** Given:  $y = \log_b x$ .

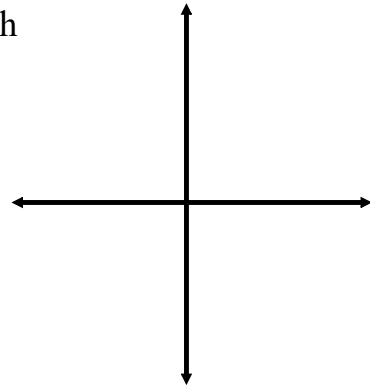
(Refer to p.450)

$$D: \{x \in R \mid x > 0\}$$

$$R: \{y \in R\}$$

$$b > 0, b \neq 1$$

Sketch



Since the domain of  $y = \log_b x$  is  $D: \{x \in R \mid x > 0\}$ , when solving equations involving logarithms, one must always identify the restrictions on  $x$ .

It is best to do this **as soon as possible**.

For example, if one is asked to solve  $\log_5(2x - 5) = \log_5 7$ , then whatever the final solution is for  $x$ , it must be greater than  $\frac{5}{2}$ .

Ex. 1: Solve:  $\log_5(2x - 5) = \log_5 7$

Ex. 2: Solve:

a)  $\log_3(x - 4) + \log_3 5 = \log_3 10$

b)  $\log_2(x - 3) + \log_2(x + 4) = 3$