This file is now in **Order by unit**, not by the day on which the question was asked.

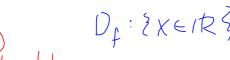
Hopefully, the new order make it easier for you to find the questions you want.

2. State the domain and range of each function.

a) 
$$y = |x - 1|$$

b) 
$$y = -2|x+3|-4$$

c) 
$$y = \left| \frac{x-3}{6} \right|$$



$$y = \left| \frac{1}{6} (x - s) \right|$$

c)  $y = \left| \frac{1}{6} \right|$ (4) Parent F(x) = |x|D<sub>f</sub>:  $2x \in R$   $X \in R$ 

- Ch.1 Self-test p.62 9. A certain tax policy states that the first \$50 000 of income is taxed at 5% and any income above \$50 000 is taxed at 12%.
  - a) Calculate the tax on \$125 000.
  - b) Write a function that models the tax policy.

$$T(50000) = 0.05(50000)$$

$$= 25000$$

$$f(x) = 0.05 \times -0.12 \times -50000$$

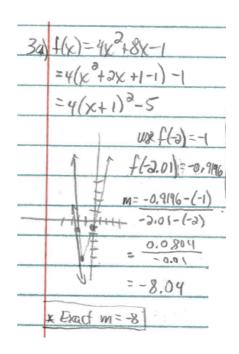
$$= 0.12 \times -6000 + 2500$$

$$= 0.12 \times -3500$$

$$f(x) = \begin{cases} 0.05 \times & \text{if } 0 \le x \le 50000 \\ 0.12x - 3500 & \text{if } x > 50000 \end{cases}$$

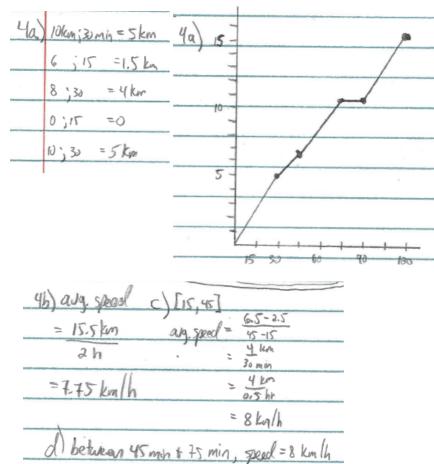
3. Sketch the graph of each of the following functions. Draw a secant line on each sketch that you could use to estimate the slope of the tangent when x = -2. Use the results to estimate the slope of the line tangent to each of the functions when x = -2.

a)  $f(x) = 4x^2 + 8x - 1$ 



4. Matthew leaves his house to go for a run. He ran at a constant speed of 10 km/h for 30 minutes. The path sloped upward, so he ran at a rate of 6 km/h for 15 minutes. At the top of the hill, he increased his speed to 8 km/h for 30 minutes. He stopped for 15 minutes to rest. Finally, he ran at a constant speed of 10 km/h for 30 minutes.

- a) Sketch a graph of Matthew's distance versus time while running.
- b) What is Matthew's average speed during the entire time that he ran?
- c) What is Matthew's average speed between 15 and 45 minutes?
- d) What is Matthew's instantaneous speed at 60 minutes?



: instantaneous at 60 min is 8 km/h

#### Ch.3 Self-test #1a

p.186

- **1.** a) Write the standard form of a general polynomial function. Then state the degree and leading coefficient of this function.
  - b) What is the greatest number of turning points that this function can have?
  - c) What is the greatest number of zeros that this function can have?
  - d) If the least number of zeros is one, describe the degree of this function.
  - e) A polynomial function is less than zero for all *x*. Describe the degree and the leading coefficient of this function.

# Chapter Self-Test, p. 186

**1. a)**  $f(x) = a_n x^n + a_{n-1} x^{n-1} + ... + a_1 x + a_0,$ 

where  $a_0$ ,  $a_1$ , ...,  $a_n$  are real numbers and n is a whole number. The degree of the function is n; the leading coefficient is  $a_n$ .

$$y = x^4 - 2x^3 + x^2 - 2x + 8.$$

The degree of this function is 4, and the leading coefficient is 1.

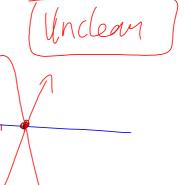
- **b)** The maximum number of turning points is n-1.
- **c)** The function may have at most *n* zeros (the same as the degree).
- d) If the least number of zeros is one, it is an odd degree function.
- **e**) The function is an even degree function with a negative leading coefficient.

1. Draw the graph of a polynomial function that has

f(x) < 0 when x < -1

The domain is the set of real numbers.

all of the following characteristics: f(1) = 8, f(-1) = 0, f(5) = 0The y-intercept is 10. f(x) > 0 when -1 < x < 2 f(x) < 0 when x < -1



Wkst #3 8. Factor each polynomial using the factor theorem.

a) 
$$x^3 + 2x^2 - 5x - 6$$

b) 
$$2x^3 + 3x^2 - 59x - 30$$

c) 
$$4x^4 - 23x^3 + 38x^2 - 13x - 6$$

d) 
$$x^4 + 8x^3 + 11x^2 - 8x - 12$$

$$if f(x) = 4x^{4} - 23x^{3} + 38x^{3} - (3x - 6)$$

$$f(1) = 4(1)^{4} - 23(1)^{3} + 38(1)^{3} - 13(1) - 6$$

$$= 0$$

$$if (x) = 4x^{4} - 23x^{3} + 38x^{3} - (3x - 6)$$

$$= (x - 1) g(x)$$

$$f(x) = 4(x^3 - 19x^3 + 19x + 6)$$

$$g(a) = 4(8) - 19(4) + 19(a) + 6$$
  
= 3a - 76 + 38 + 6  
= 0 : x-2 is a factor

$$= (x-1)(x-2)(4x^2-11x-3)$$

$$= (x-1)(x-3)(4x+1)(x-3)$$

- 1. Determine the zeros of the following functions algebraically.
  - a)  $x^3 = 7x + 6$

b) 
$$16 - 12x = 8x^2 - 3x^3 - x^4$$

c) 
$$2x^3 - 8x^2 + 2x = -12$$

b) 
$$16 - 12x = 8x^2 - 3x^3 - x^4$$
  
c)  $2x^3 - 8x^2 + 2x = -12$   
d)  $2x^4 = -6x^3 + 6x^2 + 14x - 12$ 

e) 
$$-20 = -35x + 10x^2 + 5x^3$$

f) 
$$7x^4 - 14x^2 - 56 = 21x^3 - 84x$$

(a) 
$$x^{3}-7x-6=0$$
  
if  $f(x)=x^{3}-7x-6$   
 $f(-1)=(-1)^{3}-7(-1)-6$   
 $=-1+7-6$   
 $=0$   
 $\therefore X+1$  is a factor.

$$x^{3}-7x-6=0$$
 $(x+1)(x^{2}-x-6)=0$ 

$$(x+1)(x-3)(x+2)=0$$

4. Solve the following double inequalities algebraically and determine if x = 2 is a solution. Express your solution in interval notation.

a) 
$$2x + 1 < 3x + 2 < 9 + 2x$$

b) 
$$-\frac{3}{2} < \frac{x}{4} \le \frac{1}{2}$$

c) 
$$-2 + 5x > 4x > -8 + 5x$$

d) 
$$3 \le 3x - 6 \le 39$$

e) 
$$x + 5 < 2x + 4 < x + 6$$

f) 
$$0 \le (3x+6) + (x-13) \le 3$$

$$0 \le 3 \times 46 + \times -13 \le 3$$
  
 $0 \le 4 \times -7 \le 3$   
 $0 + 1 \le 4 \times -7 + 7 \le 3 + 7$   
 $7 \le 4 \times = 10$   
 $7 \le 4 \times = 10$ 

$$\chi \in \left[\frac{1}{4}, \frac{5}{2}\right]$$

Wkst #4 5. Solve the following inequalities.

a) 
$$(x+2)(x-4) < 0$$

b) 
$$(3x - 6)(x - 5) \ge 0$$

c) 
$$(2x-2)(x+6)(x-1) > 0$$

$$\frac{1}{d} -2x(x+4)(x-6)(x+1) \le 0$$

e) 
$$(-3x + 9)(x + 1)(x - 4) > 0$$

f) 
$$x^2(x-4)(-5x+10) \ge 0$$

$$d) - 2 \times (x+4) (x-6) (x+1) \leq 0$$

Burndary Values are x = 0, -4, b, -1

$$\frac{\chi(2-4) - 4 / \chi(2-1) - 1 / \chi(2)}{-(-1)(-1)(-1)(-1)} = -\frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} = -\frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} = -\frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} = -\frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} = -\frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(+1)} - \frac{1}{(-1)(+1)(-1)(-1)} - \frac{1}{(-1)(-1)(-1)(-1)} - \frac{1}{(-1)(-1)(-1)(-1)} - \frac{1}{(-1)(-1)(-1)(-1)} - \frac{1}{(-1)(-1)(-1)(-1)} - \frac{1}{(-1)(-1)(-1)(-1)} - \frac{1}{(-1)(-1)(-1)(-1)} - \frac{1}{$$

$$\chi \in (-\infty, -4] \cup [-1, 0] \cup [6, \infty)$$

Wkst #4 5. Solve the following inequalities.

a) 
$$(x+2)(x-4) < 0$$

b) 
$$(3x - 6)(x - 5) \ge 0$$

c) 
$$(2x-2)(x+6)(x-1) > 0$$

d) 
$$-2x(x + 4)(x - 6)(x + 1) \le 0$$

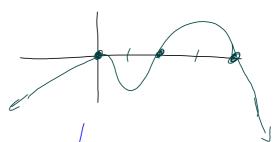
e) 
$$(-3x + 9)(x + 1)(x - 4) > 0$$

f) 
$$x^2(x-4)(-5x+10) \ge 0$$

$$-2\bar{x}_{3}(x-4)(x-9) \leq 0$$

$$x_{3}(x-4)(-2(x-9)) \leq 0$$

BU: 0,4,2



8. Estimate the instantaneous rate of change at x = 1and let h = 0.001 for the following functions.

a) 
$$f(x) = -3x + 2$$

b) 
$$g(x) = -x^2 - 8$$
  
c)  $h(x) = 2^x + 1$ 

c) 
$$h(x) = 2^x + 1$$

d) 
$$j(x) = \sqrt{x+7} - 5$$

e) 
$$k(x) = 2|x + 4| - 1$$

$$f) I(x) = 3x^{4} - x^{2} + 8x - 1$$

$$INDC = \frac{1}{2}(x + \lambda) - \frac{1}{2}(x +$$

= 0.18

3. For each function, state the equation of the vertical asymptote, if it exists.

$$a) f(x) = \frac{3}{3x + 8}$$

b) 
$$f(x) = \frac{1 - 4x}{2}$$

c) 
$$f(x) = \frac{7 + 5x}{2 - x}$$

$$d) f(x) = \frac{9x + 3}{2x - 9}$$

4. State the horizontal asymptote for each function in Question 3, if it exists.

Question 3, if it exists.

((c) 
$$f(x) = \frac{5x+7}{-x+2}$$

$$y = \frac{5}{-1} (x)$$

$$y = -1 (x)$$

5. Solve each equation algebraically. Check your

a) 
$$0 = \frac{x-3}{500}$$

b) 
$$\frac{x+3}{7} = 10$$

c) 
$$\frac{5x+2}{3} = 6 - x$$

d) 
$$-\frac{4}{2x+3} = 1(-2+3x)$$

e) 
$$\frac{4}{5x} = \frac{6}{2x - 1}$$

$$\frac{-4}{2 \times +3} = -2 + 3 \times$$

$$-4 = (-2+3x)(2x+3)$$

$$0 = -4x - 6 + 6x^{2} + 9x + 4$$

$$0 = 6x^{2} + 5x - 2$$

$$0 = (x_3 + 2x - 5)$$

$$X = \frac{-5 \pm \sqrt{52-4(6)(-3)}}{2(6)}$$

$$= \sqrt{5} \pm \sqrt{25+48}$$

$$X = \frac{5 + \sqrt{73}}{\sqrt{a}} \quad \text{or} \quad x = \frac{-5 - \sqrt{73}}{\sqrt{a}}$$

$$= 0.2953 = -1.1286$$

$$= 0.2953 = -1.1286$$

Wkst #5 7. Use an algebraic process to find the solution set of each inequality. Verify your answers using graphing technology.

a) 
$$\frac{1}{x^{2}} > 0$$
b)  $x - 2 < \frac{1}{x + 2}$ 
c)  $\frac{100}{x + 20} > -x$ 

$$(X - 2) \frac{(X + 2)}{(X + 2)} - \frac{1}{(X + 2)} = 0$$

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$$(X - 2) \frac{($$

$$X(-55)$$
 -55( $X(-2)$  -2( $X(-55)$   $X > 55$   
 $(+)$   $(-)$   $(-)$   $(+)$   $(+)$   $(+)$   
 $= =+$   $= =+$   
:True :False :True :False  
 $:X \in (-\infty, -55) \cup (-2, \sqrt{5})$   
or  $\{x \in \mathbb{R} \mid x < -55 \text{ or } -2 < x < \sqrt{55}\}$ 

Use an algebraic process to find the solution set of each inequality. Verify your answers using graphing technology.

a) 
$$\frac{1}{x^2} > 0$$
  
b)  $x - 2 < \frac{1}{x + 2}$   
c)  $\frac{100}{x + 20} > -x$   

$$\frac{100}{x + 20} + \frac{x}{x + 20} > 0$$

$$\frac{100}{x + 20} + \frac{x}{x + 20} > 0$$

$$\frac{100 + x^2 + 20x}{x + 20} > 0$$

$$\frac{x^2 + 20x + 100}{x + 20} > 0$$

$$\frac{(x + 10)^3}{x + 20} > 0$$

Boundary Values: 
$$X = -20, -10$$

$$\frac{(+)}{(-)} = +$$

$$\frac{(+)}{(-)} = +$$

$$\frac{(+)}{(-)} = +$$

$$\frac{(+)}{(+)} =$$

8. Estimate the slope of the line tangent to the function at the given value of *x*. At what point(s) is it not possible to do so?

a) 
$$f(x) = \frac{x+10}{x-20}$$
,  $x = 30$ 

$$= \frac{f(x+h)-f(x)}{h}, h > 0$$

$$= \frac{(30+h)+10}{(30+h)-20} - \left(\frac{30+10}{30-20}\right), as h > 0$$

$$= \left(\frac{40+h}{h+10} - \frac{40}{10}\right) = h + a h > 0$$

$$= \left(\frac{40+h}{h+10} - 4\left(\frac{h+10}{h+10}\right)\right) \times \frac{1}{h}, as h > 0$$

$$= \frac{h + 40 - 4h - 40}{h + 10} \times \frac{1}{h}, as h > 0$$

$$= \frac{-3k}{h+10} \times \frac{1}{k}, as h \Rightarrow 0$$

$$= \frac{-3}{h+10}, h > 0$$

: the slope of the tangent at

$$X = 30 \text{ is } \frac{-3}{10}$$

[Not possible to estimate at x = 20]

8. Estimate the slope of the line tangent to the function at the given value of *x*. At what point(s) is it not possible to do so?

a) 
$$f(x) = \frac{x+10}{x-20}$$
,  $x = 30$ 

8c\* (\* you MUST use "first principles" and algebraically determine the EXACT value of the instantaneous rate of change),

c) 
$$f(x) = \frac{2x}{3x+4}$$
,  $x = -2$ 

$$iroc = \frac{f(x+h) - f(x)}{h}, h > 0$$

$$= \frac{2(-2+h)}{3(-2+h) + 4} - \frac{2(-a)}{3(-a) + 4}, as h > 0$$

$$= \left[ \frac{-4+2h}{-6+3h+4} - \frac{-4}{-6+4} \right] = h + 100h > 0$$

$$= \left[ \frac{2h-4}{3h-2} + \frac{4}{-2} \right] \times \frac{1}{h}, as h > 0$$

$$= \left(\frac{2h-4}{3h-a} - 2\left(\frac{3h-a}{3h-a}\right) \times \frac{1}{h} \right) \times \frac{1}{h} = 0$$

$$= \left[\frac{2h-4-6h+4}{3h-2}\right] \times \frac{1}{h}, \text{ an } h-70$$

$$= \frac{-4h}{3h-2} \times \frac{1}{h} \cdot 40 h \Rightarrow 0$$

$$= \frac{-4}{3h-2}, as h \rightarrow 0$$

.. the slope of the tongert at

[Not possible to estimate at  $X = -\frac{4}{3}$ ]

4. A clock is hanging on a wall, with the centre of the clock 4.5 metres above the ground. Both the minute hand and the second hand are 13 cm long, while the hour hand is 6 cm long. Determine the equations of the sine function that describe the distance of the tip of each hand above the ground as a function of time. Assume that the time t is in hours and that the distance D(t) is in cm. Also assume that at t = 0 it is 3 AM.

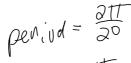
11 61 1	Maria de la companya della companya
4. (13cm) \$	Minute hand; time in hours
-13	The le period pariod=1h
	= ar d= 4 h
450cm DEFA sink(t-d)+	C =2T
a=13, c=450	D(t)=-13 sin (20(t-4))+450
	or Olt)= B Sin (211(t+4))+450
Hour hand	Second hand; time in hours
R = 2T period = 12h	R = 217 period= to of hour
0 = 0 (std. pss.)	65
= 16	= 120TT d= 4 8 to 6 horas
: D(t) = -6 sin ( = + ) + 450	= 540 of home
	: D(E) = -13 Sin(120 17 (E-240))+450
	or = 1381 (100 m (++ + + + + + + + + + + + + + + + + +

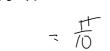
5. State two points where each of the following functions has an instantaneous rate of change that is a positive value.

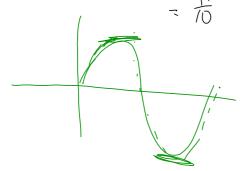
a) 
$$y = -\frac{19}{20}\sin(24\pi x) + \frac{1}{40}$$

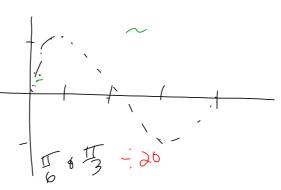
$$b) y = 35 \cos\left(\frac{x}{12}\right) - 31$$

c) 
$$y = \frac{1}{36} \sin(20x) + \frac{1}{18}$$





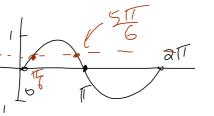






5. With the help of a graphing calculator, sketch a graph that could be used to help solve each of the following equations. Also state the solution(s) to the equations, where  $0 \le x \le 2\pi$ .





3. Solve for x.

a) 
$$\log_2 \frac{1}{256} = x$$

$$\lambda^{\times} = \frac{1}{256}$$

$$\lambda^{\times} = (256)^{-1}$$

$$\lambda^{\times} = (256)^{-1}$$

$$\lambda^{\times} = (256)^{-1}$$

$$\lambda^{\times} = (256)^{-1}$$

$$5d) \left(\frac{1}{2}\right)^{x-2} - \left(\frac{1}{2}\right)^x = \frac{3}{32}$$

$$\left(\frac{1}{2}\right)^x \left(\frac{1}{2}\right)^x - \frac{1}{32} = \frac{3}{32}$$

$$\left(\frac{1}{2}\right)^x \left(\frac{1}{2}\right)^2 - \frac{3}{32}$$

$$\left(\frac{1}{2}\right)^x \left(\frac{1}{2}\right)^2 - \frac{3}{32}$$

$$\left(\frac{1}{2}\right)^x - \frac{3}{32}$$

$$\left(\frac{1}{2}\right)^x - \frac{3}{32}$$

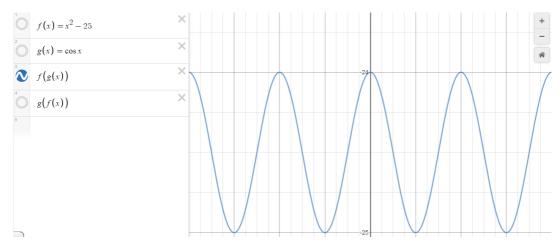
$$\left(\frac{1}{2}\right)^x - \frac{1}{32}$$

Wkst #9 5. For each of the following sets of functions, determine the domain and range of  $f \circ g$  and  $g \circ f$ .

a) 
$$f(x) = x^2 - 25$$
;  $g(x) = \cos x$ 

$$f \circ g(x) = (\circ Sx)^2 - 25$$





$$(g \circ f)(x) = cos(x^2-af)$$

