

Are there any Homework Questions you would like to see on the board?

pp. 139-142 # 2bd, 3cd, 4bde, 5be, 6, 7cde, 12bcd, 14  
**READ pp.153-154**

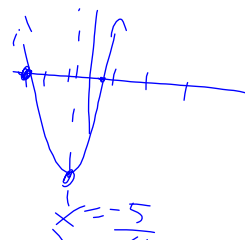
2. Express each quadratic function in factored form. Then determine the zeros, the equation of the axis of symmetry, and the coordinates of the vertex.

a)  $f(x) = 2x^2 + 12x$

b)  $f(x) = x^2 - 7x + 12$

c)  $f(x) = -x^2 + 100$

d)  $f(x) = 2x^2 + 5x - 3$



Axis of Symmetry:  
 $x = -\frac{5}{4}$

$$f\left(-\frac{5}{4}\right) = \left(2\left(-\frac{5}{4}\right) - 1\right)\left(\left(-\frac{5}{4}\right) + 3\right)$$

$$= \left(-\frac{5}{2} - \frac{2}{2}\right)\left(-\frac{5}{4} + \frac{12}{4}\right)$$

$$= \left(-\frac{7}{2}\right)\left(\frac{7}{4}\right)$$

$$= -\frac{49}{8}$$

$\therefore V\left(-\frac{5}{4}, -\frac{49}{8}\right)$   
 or  $(-1.25, -6.125)$

$$0 = (2x - 1)(x + 3)$$

$$\downarrow \quad \downarrow$$

$$2x - 1 = 0 \quad x + 3 = 0$$

$$2x = 1 \quad x = -3$$

$$x = \frac{1}{2}$$

Axis of Symmetry:  $x = \frac{-3 + \frac{1}{2}}{2}$

$$= \frac{-\frac{6}{2} + \frac{1}{2}}{2}$$

$$= \frac{-\frac{5}{2}}{2} \rightarrow -\frac{5}{2} \div \frac{2}{1}$$

$$= \frac{-5}{2} \times \frac{1}{2}$$

$$= \frac{-5}{4} = -\frac{5}{4}$$

4. For each quadratic function, determine the zeros, the equation of the axis of symmetry, and the coordinates of the vertex without graphing.

a)  $g(x) = 2x(x + 6)$

b)  $g(x) = (x - 8)(x + 4)$

c)  $g(x) = (x - 10)(2 - x)$

d)  $g(x) = (2x + 5)(9 - 2x)$

e)  $g(x) = (2x + 3)(x - 2)$

f)  $g(x) = (5 - x)(5 + x)$

d)  $0 = (2x + 5)(9 - 2x)$

$$\downarrow \quad \downarrow$$

$$2x + 5 = 0 \quad \text{or} \quad 9 - 2x = 0$$

$$2x = -5 \quad -2x = -9$$

$$x = -\frac{5}{2} \quad x = \frac{9}{2}$$

Axis of Symmetry:  $x = \frac{-\frac{5}{2} + \frac{9}{2}}{2}$

$$= \frac{\frac{4}{2}}{2}$$

$$= \frac{2}{2}$$

$$x = 1$$

$\rightarrow g(1) = (2(1) + 5)(9 - 2(1))$   
 $= (7)(7)$   
 $= 49$   
 $\therefore (1, 49)$

## Today's Learning Goal(s):

By the end of the class, I will be able to:

- Determine if a relation is a function (or not) given a mapping notation.
- Determine if a relation is a function (or not) given a graph.

MCF 3MI

### 1.0 & 1.1 Characteristics of a Function

Date: Mar. 6/19  
(Every lesson)

Review:

Ex.1: Identify which of the following are linear or quadratic:

a)  $y = 5x + 2$

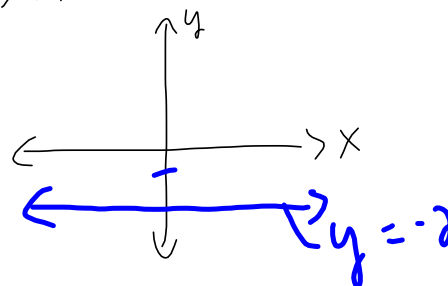
Linear  $y = mx + b$

b)  $y = 2x^2 - 3$

quadratic

c)  $y = -2$

linear: horizontal line



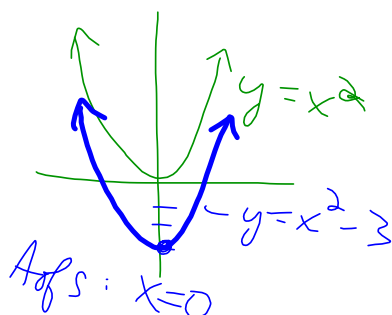
Ex.2: For each relation, determine the y-intercept and the axis of symmetry.

a)  $y = x^2 - 3$

let  $x = 0$

$$y = 0^2 - 3$$

$$y = -3 \leftarrow y\text{-int}$$



b)  $y = 3(x - 2)^2 + 1$

let  $x = 0$

$$y = 3(0 - 2)^2 + 1$$

$$= 3(-2)^2 + 1$$

$$= 3(4) + 1$$

$$y = 13 \leftarrow y\text{-int}$$

$$y = a(x - h)^2 + k$$

$$V(h, k)$$

$$V(2, 1)$$

$$\text{AoS: } x = 2$$

Domain and range describe all the possible values of the relation.

Domain describes ALL of the  $x$ -values.

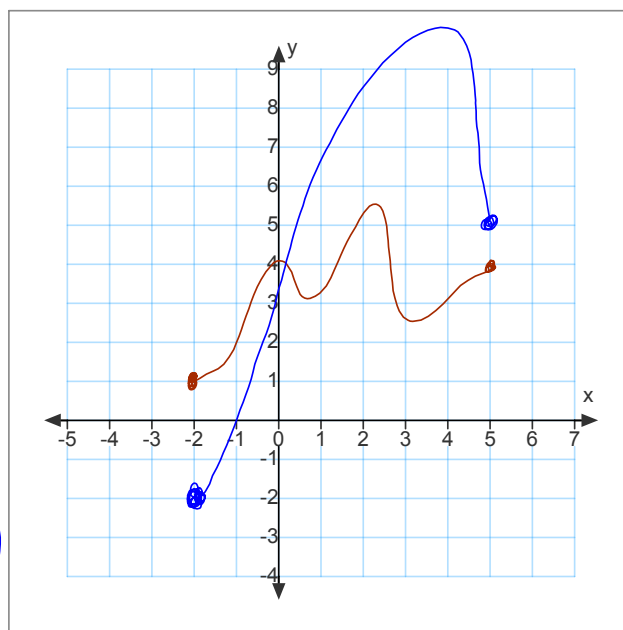
Range describes ALL of the  $y$ -values.

We use set notation to mathematically write the domain & range.

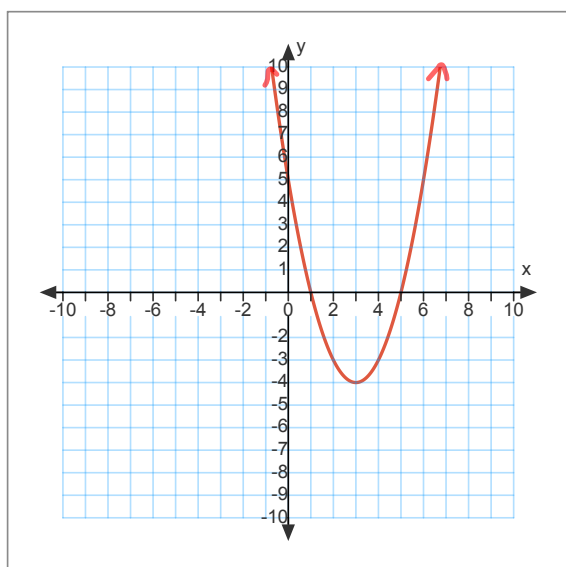
For example:

$$D = \{x \in \mathbb{R} \mid -2 \leq x \leq 5\}$$

$$R = \{y \in \mathbb{R} \mid y \geq -2\}$$



Ex.3: State the domain and range of the quadratic function below:



$$D: \{x \in \mathbb{R}\}$$

$$R: \{y \in \mathbb{R} \mid y \geq -4\}$$

A function is a relation that has a one-to-one relationship.  
This means that for every  $x$ -value there is only one  $y$ -value.

Ex.4: For each of the following relations, determine the domain & range, then state whether or not it is a function.

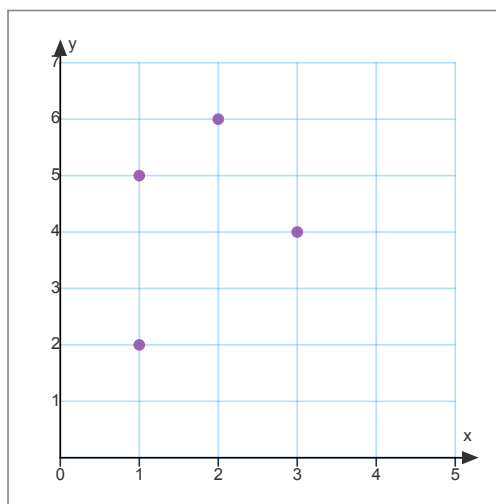
a)

$x$	$y$
-1	-3
0	1
1	5
2	9

D:  $\{-1, 0, 1, 2\}$ R:  $\{-3, 1, 5, 9\}$ 

Function

b)

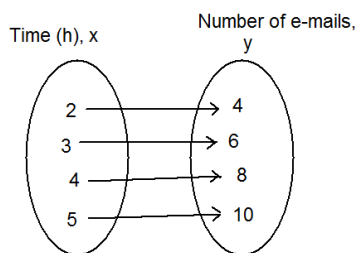
D:  $\{1, 2, 3\}$ R:  $\{2, 4, 5, 6\}$ Not a function  
( $x=1$  repeats)

c)  $G(x, y) = \{\text{number of golfers, score below or above par}\}$   
 $= \{(0, -2), (0, -1), (0, 0), (1, 5)\}$

D:  $\{0, 1\}$ R:  $\{-2, -1, 0, 5\}$ 

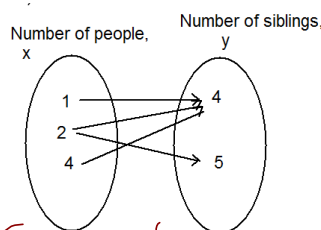
Not a function

d)

D:  $\{2, 3, 4, 5\}$ R:  $\{4, 6, 8, 10\}$ 

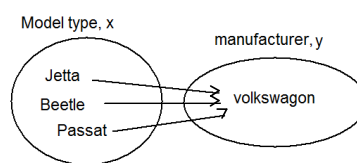
Function

e)

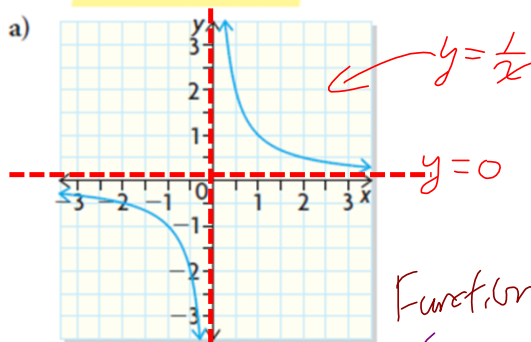
D:  $\{1, 2, 4\}$ R:  $\{4, 5\}$ 

Not a function

f)

D:  $\{Jetta, Beetle, Passat\}$ R:  $\{Volkswagen\}$

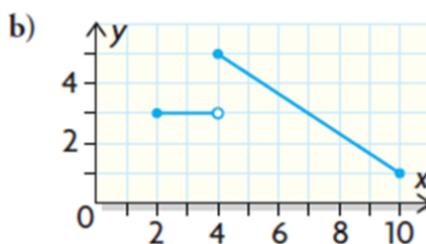
Ex.5: For each of the following relations, determine the domain and the range, using **real numbers**. State whether or not the relation is a function.



Function  
(Passes VLT)

D:  $\{x \in \mathbb{R} \mid x \neq 0\}$

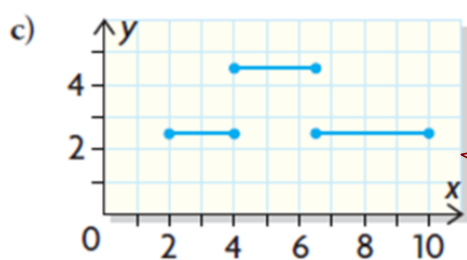
R:  $\{y \in \mathbb{R} \mid y \neq 0\}$



Function  
(Passes VLT)

D:  $\{x \in \mathbb{R} \mid 2 \leq x \leq 10\}$

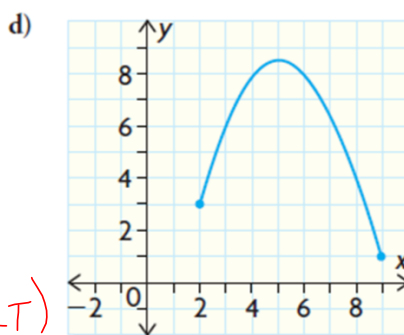
R:  $\{y \in \mathbb{R} \mid 1 \leq y \leq 5\}$



NOT a  
Function  
(FAILS VLT)

D:  $\{x \in \mathbb{R} \mid 2 \leq x \leq 10\}$

R:  $\{2.5, 4.5\}$



Function  
(Passes VLT)

D:  $\{x \in \mathbb{R} \mid 2 \leq x \leq 9\}$

R:  $\{y \in \mathbb{R} \mid 1 \leq y \leq 9\}$

Ex. 6: Which variable would be associated with the domain for the following pairs of related quantities? Which variable would be associated with the range? Explain.

Bill  
Temp

- heating bill, outdoor temperature
- report card mark, time spent doing homework
- ~~person, date of birth~~
- number of slices of pizza, number of cuts

**Range is ALWAYS the DEPENDENT VARIABLE.**