

## Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) Identify the “order of the moves” when graphing using transformations.
- b) State the domain and range for “multiple move” transformations.

MCF 3MI

### 3.1.5 Graphing Quadratic Functions Using Transformations

Date: Mar. 8/19  
(Every lesson)

$$f(x) = a(x - h)^2 + k$$

Correct yesterday's worksheet:

**a -- p. 39 E,F**

**h -- p. 39 C,D**

**k -- p. 38 A,B**

**You will be completing an EXIT card 10 minutes before class finishes.**

Possible Transformations: (RST)

R: reflection in the  $x$ -axis

S: vertical stretch (v.s.) by a factor of  $\underline{a}$

OR vertical compression (v.c.) by a factor of  $\underline{\frac{1}{a}}$

T: horizontal translation (h.t.)  $\underline{h}$  units to the right or left

T: vertical translation (v.t.)  $\underline{k}$  units to up or down

$$y = a(x-h)^2 + k$$

$$V(h, k)$$

Ex. 1 i) Identify the values of the parameters  $a$ ,  $h$ , and  $k$ .

ii) Identify the transformations.

iii) Use transformations to sketch each graph.

$$(x - (-2))^2$$

iv) State the Domain and Range.

a)  $f(x) = \underline{(x-3)^2 + 4}$  vertex  $(\underline{3}, \underline{4})$  b)  $g(x) = (x+2)^2 + 1$  vertex  $(\underline{-2}, \underline{1})$

$\cdot a = \underline{1}$ ,  $h = \underline{3}$ ,  $k = \underline{4}$

h.t. 3 units to the right

v.t. 4 units up

MG  
1 1  
2 4  
3 9

$$y = (x-3)^2 + 4$$

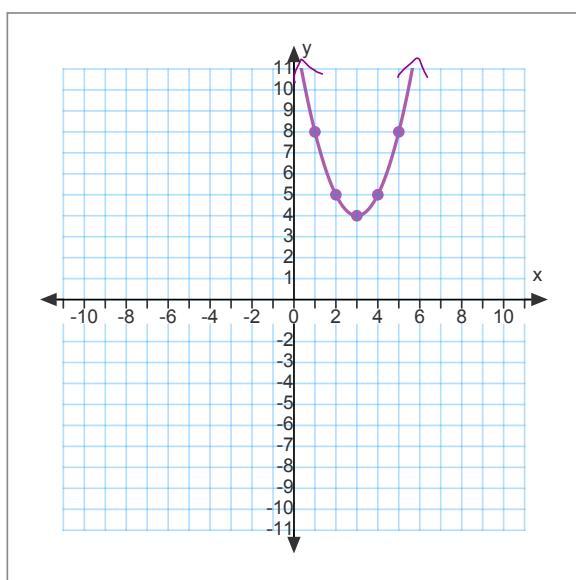
$a = \underline{1}$ ,  $h = \underline{-2}$ ,  $k = \underline{1}$

h.t. 2 units left

v.t. 1 unit up

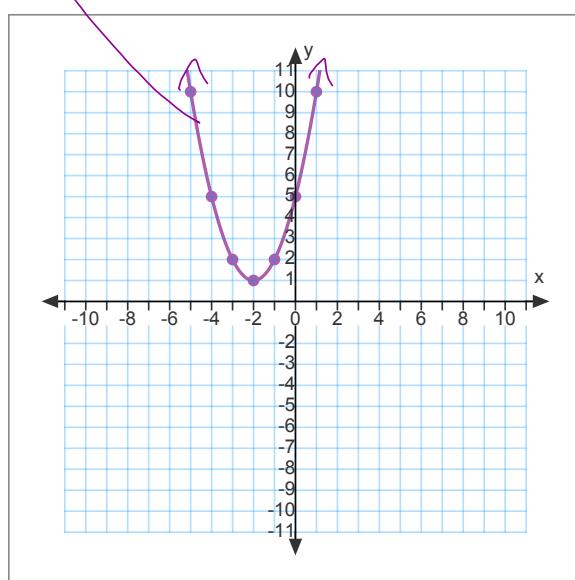
MG  
1 1  
2 4  
3 9

$$y = (x+2)^2 + 1$$



Domain:  $\{x \in \mathbb{R}\}$

Range:  $\{y \in \mathbb{R} / y \geq 4\}$



Domain:  $\{x \in \mathbb{R}\}$

Range:  $\{y \in \mathbb{R} / y \geq 1\}$

Ex. 1 (cont'd)

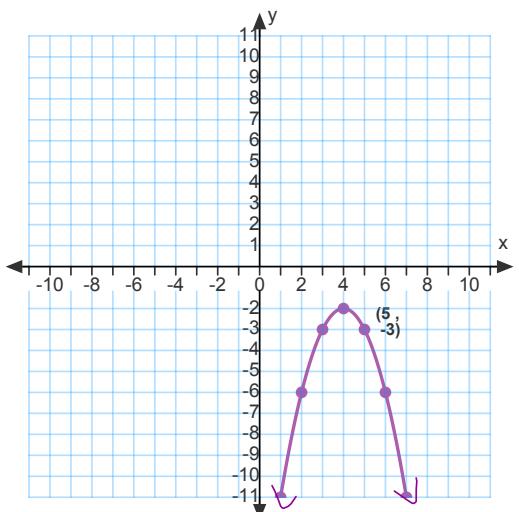
- Identify the values of the parameters  $a$ ,  $h$ , and  $k$ .
- Identify the transformations.
- Use transformations to sketch each graph.
- State the Domain and Range.

c)  $h(x) = -(x-4)^2 - 2$  vertex (4, -2)  
 $a = -1$ ,  $h = 4$ ,  $k = -2$

reflection in the x-axis  
h.t. 4 units right  
v.t. 2 units down

MG

1	-1
2	-4
3	-9



\*\* Check using 1 (non-vertex) point

Domain:  $\{x \in \mathbb{R}\}$

Range:  $\{y \in \mathbb{R} / y \leq -3\}$

$$h(x) = -(x-4)^2 - 2$$

$$h(5) = -(5-4)^2 - 2$$

$$= -(1)^2 - 2$$

$$= -1 - 2$$

$$= -3$$

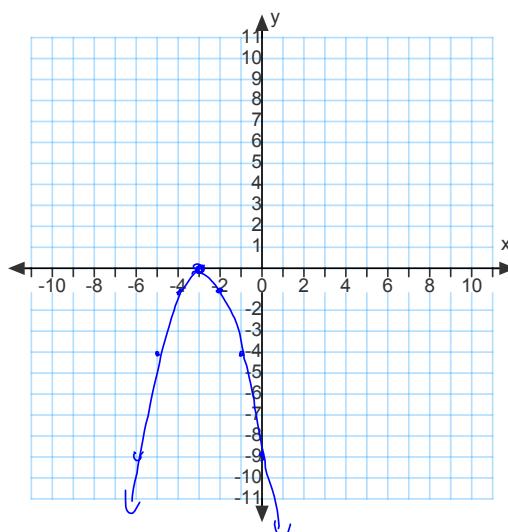
d)  $i(x) = -(x+3)^2 + 0$  vertex (-3, 0)  
 $a = -1$ ,  $h = -3$ ,  $k = 0$

reflection in the x-axis  
h.t. 3 units left

MG

1	-1
2	-4
3	-9

$$y = -(x+3)^2$$



Domain:  $\{x \in \mathbb{R}\}$

Range:  $\{y \in \mathbb{R} / y \leq 0\}$

## Ex. 1 (cont'd)

- Identify the values of the parameters  $a$ ,  $h$ , and  $k$ .
- Identify the transformations.
- Use transformations to sketch each graph.
- State the Domain and Range.

e)  $j(x) = x^2 + 2$  vertex (0, 2)  
 $a = \underline{1}$ ,  $h = \underline{0}$ ,  $k = \underline{2}$

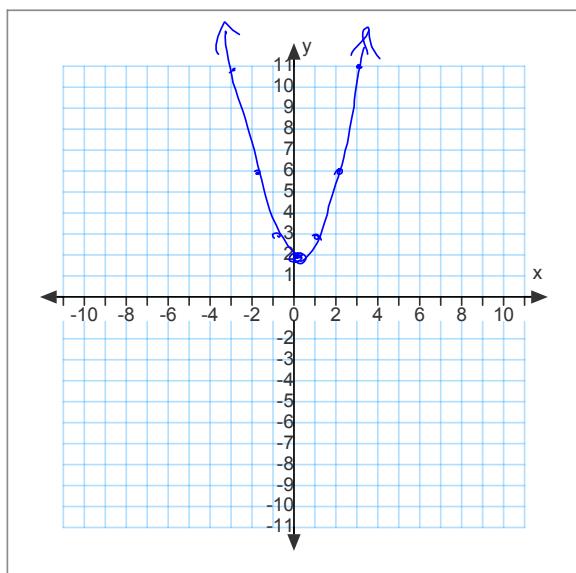
v.t. 2 units up

f)  $k(x) = -x^2 + 2$  vertex (0, 2)  
 $a = \underline{-1}$ ,  $h = \underline{0}$ ,  $k = \underline{2}$

reflection in the x-axis  
v.t. up 2 units

MG

$$y = x^2 + 2$$

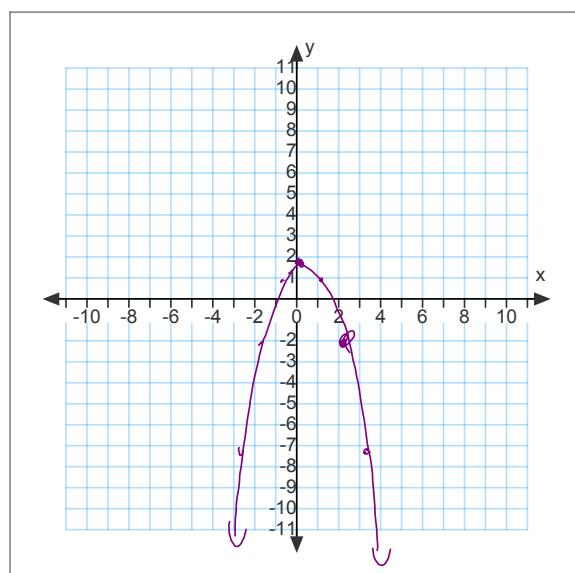


Domain:  $\mathbb{R}$

Range:  $y \geq 2$

MG

$$y = -x^2 + 2$$



Domain:  $\mathbb{R}$

Range:  $y \leq 2$

**Homework today is modified as follows:**

**READ p.46 “In Summary” CAREFULLY, and ask me if anything is unclear!**

i) Complete the CheckPoint/Exit Card and submit it to the teacher

**BEFORE the end of class!**

ii) Sketch the 2 functions on the bottom of the handout. (on next screen,

ii) Complete: p. 40 # 1 and tomorrow's file.)

pp. 47-49 # 1, 2\*, 9

\*for 2iii) use graph paper to sketch by hand, then check using **desmos**

Distribute EXIT CARD: **Put your name on it!**

Additional homework questions from the bottom of the handout:

$$1. \quad a(x) = -(x+5)^2 - 3 \quad \text{vertex } ( \quad , \quad )$$

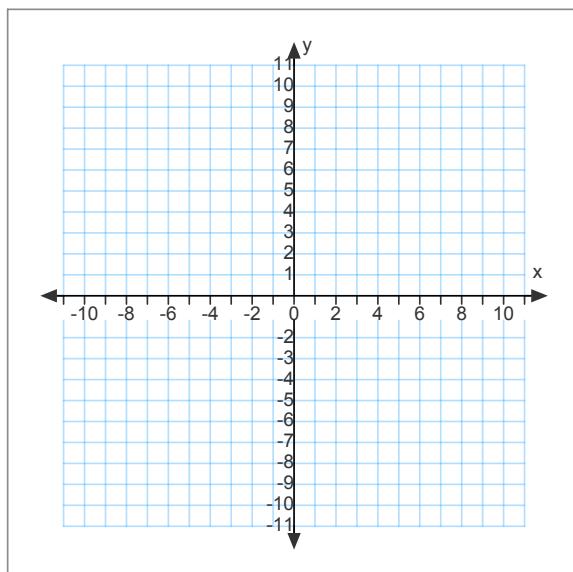
$a = \underline{\hspace{2cm}}$ ,  $h = \underline{\hspace{2cm}}$ ,  $k = \underline{\hspace{2cm}}$

$$2. \quad b(x) = 2(x-1)^2 - 7 \quad \text{vertex } ( \quad , \quad )$$

$a = \underline{\hspace{2cm}}$ ,  $h = \underline{\hspace{2cm}}$ ,  $k = \underline{\hspace{2cm}}$

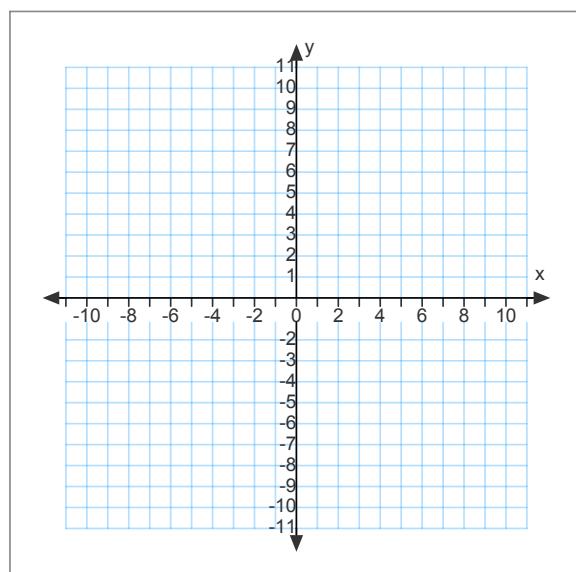
MG

$$y = -(x+5)^2 - 3$$



MG

$$y = 2(x-1)^2 - 7$$



Domain: \_\_\_\_\_

Domain: \_\_\_\_\_

Range: \_\_\_\_\_

Range: \_\_\_\_\_