

Today's Learning Goal(s):

Date: _____

By the end of the class, I will be able to:

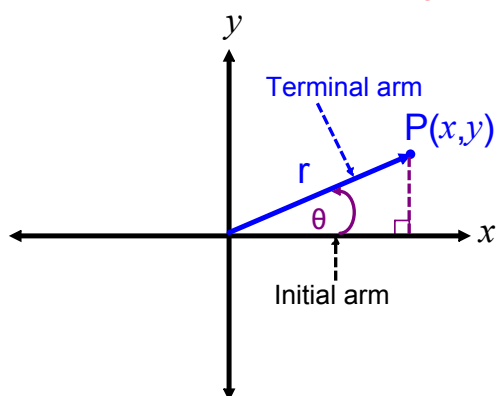
- a) explain the relationship between the ratios of an angle in standard position, and the related acute angle (RAA).
- b) determine the trig ratios of angles between 0° and 360° .

Last day's work: p. 292 #1 – 4 3
pp. 299-300 #(1 – 5)ac
(3 screens away) 3c

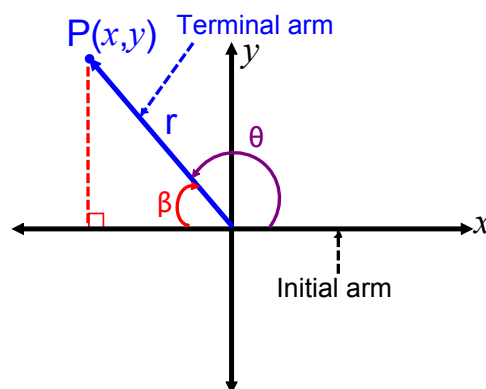
Defining an angle in "standard position". **Explain: $0^\circ \leq \theta \leq 360^\circ$**

θ = Principal Angle

β = Related Acute Angle (RAA)

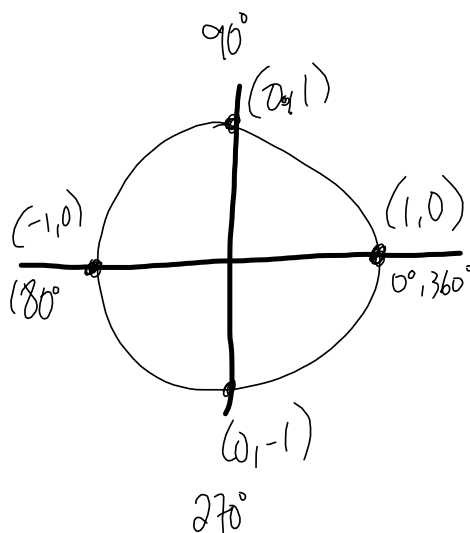


Note: In Quadrant I: $\theta = \beta$



Memorize this Chart!

θ	30°	45°	60°
$\sin \theta$	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$ or $\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$
$\cos \theta$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$ or $\frac{\sqrt{2}}{2}$	$\frac{1}{2}$
$\tan \theta$	$\frac{1}{\sqrt{3}}$ or $\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$



Are there any Homework Questions you would like to see on the board?

From Wednesday: pp. 286-287 # 1 – 9

Last day's work: p. 292 #1 – 4
pp. 299-300 #(1 – 5)ac

Extra STUFF on website!

Today's Homework Practice includes:

pp. 299-300 #(1 – 5)bd

Standard Posion Wkst#8-3

1cd, 2bc, 6, 7a, 9

Worksheet #2b) Answer should be +2

3. Sylvie drew a special triangle in quadrant 3 and determined that $\tan (180^\circ + \beta) = 1$.
- What is the value of angle β ?
 - What would be the exact value of $\tan \theta$, $\cos \theta$, and $\sin \theta$?

p. 292 1. State all the angles between 0° and 360° that make each equation true.

- a) $\sin 45^\circ = \sin$ _____
- b) \cos _____ $= -\cos(-60^\circ)$
- c) $\tan 30^\circ = \tan$ _____
- d) $\tan 135^\circ = -\tan$ _____



a) $\sin 45^\circ = \frac{1}{\sqrt{2}}$

$\therefore \sin 135^\circ = \frac{1}{\sqrt{2}}$

b) $\cos(-60^\circ)$

$\cos(-60^\circ) = \frac{1}{2}$
 $\therefore -\cos(-60^\circ) = -\frac{1}{2}$

$\cos 120^\circ = -\frac{1}{2}$
 and $\cos 240^\circ = -\frac{1}{2}$

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2. Using the special triangles from Lesson 5.2, sketch two angles in the Cartesian plane that have the same value for each given trigonometric ratio.

- a) sine
- b) cosine
- c) tangent

a)

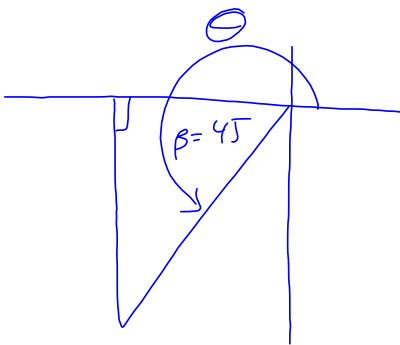
$\sin 30^\circ = \frac{1}{2}$
 $\sin 150^\circ = \frac{1}{2}$

b)

$\cos 240^\circ = -\frac{1}{2}$
 and
 $\cos 120^\circ = -\frac{1}{2}$

p. 292 3. Sylvie drew a special triangle in quadrant 3 and determined that $\tan(180^\circ + \theta) = 1$.

- What is the value of angle θ ?
- What would be the exact value of $\tan \theta$, $\cos \theta$, and $\sin \theta$?



$$\tan(180^\circ + \theta) = 1$$

$$\tan(180^\circ + 45^\circ) = 1$$

$$\tan(225^\circ) = 1$$

$$\tan \beta = 1$$

$$\beta = 45^\circ$$

$$\sin 225^\circ$$

$$= -\sin 45^\circ$$

$$= -\frac{1}{\sqrt{2}}$$

$$\cos 225^\circ$$

$$= -\cos 45^\circ$$

$$= -\frac{1}{\sqrt{2}}$$

$$\tan 225^\circ$$

$$= +\tan 45^\circ$$

$$= 1$$

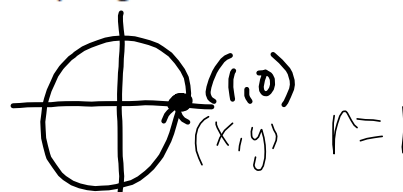
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3. Use the method in Example 3 to determine the primary trigonometric ratios for each given angle.

a) 180°

b) 270°

c) 360°



$$\begin{aligned}\sin 360^\circ &= \frac{y}{r} \\ &= \frac{0}{1} \\ &= 0\end{aligned}$$

$$\begin{aligned}\cos 360^\circ &= \frac{x}{r} \\ &= \frac{1}{1} \\ &= 1\end{aligned}$$

$$\begin{aligned}\tan 360^\circ &= \frac{y}{x} \\ &= \frac{0}{1} \\ &= 0\end{aligned}$$

4. Use the related acute angle to state an equivalent expression.

a) $\sin 160^\circ$

b) $\cos 300^\circ$

c) $\tan 110^\circ$

d) $\sin 350^\circ$