

## Today's Learning Goal(s):

Date: May 15, 19

By the end of the class, I will be able to:

- a) determine how each transformation affects the sine and cosine curves.

### Show Level 4 Exemplars

Last day's work: pp. 363-364 #1 – 4, 8, 9 [15,16]  
pp. 370-372 #1 – 8, 13 [15]

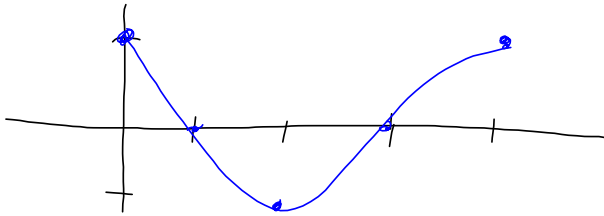
Today's Homework Practice includes:

pp. 377-378 A – U

p. 379 #1 – 3

p. 363 2. a) If  $h(x) = \sin(5x) - 1$ , calculate  $h(25^\circ)$ .

b) If  $f(x) = \cos x$  and  $f(x) = 0$ , list the values of  $x$  where  $0^\circ \leq x \leq 360^\circ$ .



$f(x) = 0$   
if  $x = 90^\circ$  or  $x = 270^\circ$

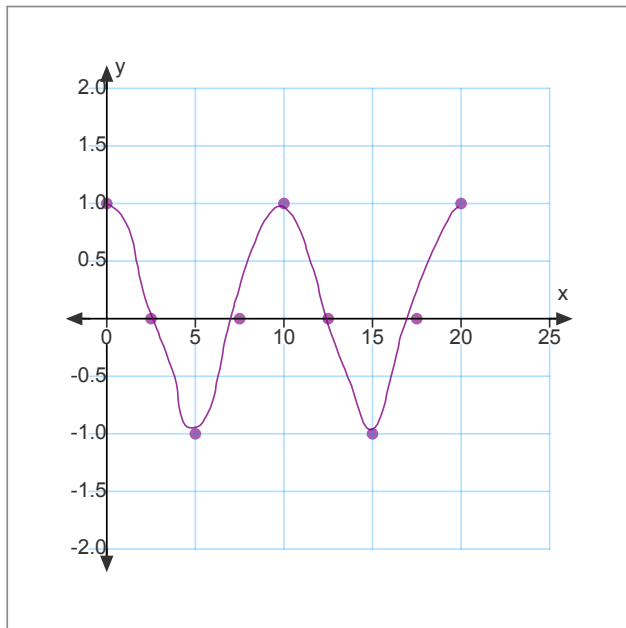
3. A buoy rises and falls as it rides the waves. The equation  $h(t) = \cos(36t)^\circ$  models the displacement of the buoy,  $h(t)$ , in metres at  $t$  seconds.

a) Graph the displacement from 0 s to 20 s, in 2.5 s intervals.

b) Determine the period of the function from the graph. - 10 sec

c) What is the displacement at 35 s?  $h(35) = \cos(36(35)) = -1$

d) At what time, to the nearest second, does the displacement first reach  $-0.8$  m? From Graph,  $t = 4$  sec



| t    | h(t) |
|------|------|
| 0    | 1    |
| 2.5  | 0    |
| 5    | -1   |
| 7.5  | 0    |
| 10   | 1    |
| 12.5 | 0    |
| 15   | -1   |
| 17.5 | 0    |
| 20   | 1    |

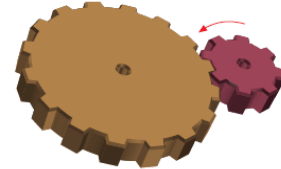
$-0.8 = \cos(36t)$   
Let  $x = 36t$   
 $-0.8 = \cos x$   
 $\cos^{-1}(-0.8) = x$   
 $x = 143.13$

But  $x = 36t$

$\therefore \frac{x}{36} = t$   
 $t = \frac{143.13}{36}$   
 $\approx 3.97$   
 $\approx 4$  sec.

## p. 372 Extending

15. A gear of radius 1 m turns counterclockwise and drives a larger gear of radius 4 m. Both gears have their axes along the horizontal.
- In which direction is the larger gear turning? - clockwise
  - If the period of the smaller gear is 2 s, what is the period of the larger gear?
  - In a table, record convenient intervals for each gear, to show the vertical displacement,  $d$ , of the point where the two gears first touched. Begin the table at 0 s and end it at 24 s. Graph vertical displacement versus time.
  - What is the displacement of the point on the large wheel when the drive wheel first has a displacement of  $-0.5$  m?
  - What is the displacement of the drive wheel when the large wheel first has a displacement of 2 m?
  - What is the displacement of the point on the large wheel at 5 min?



b) Smaller

$$\begin{aligned} \text{Speed}_S &= \frac{d}{t} \\ &= \frac{2\pi r}{\text{period}} \\ &= \frac{2\pi(1)}{2} \\ &= \pi \text{ m/s} \end{aligned}$$

larger

$$\begin{aligned} \text{Speed}_L &= \frac{d}{t} \\ \pi &= \frac{2\pi(4)}{\text{period}} \\ \pi &= \frac{8\pi}{\text{period}} \\ \text{period} &= \frac{8\pi}{\pi} \\ &= 8 \text{ sec.} \end{aligned}$$

## 6.4 Exploring Transformations of Sinusoidal Functions

*EXPLORE the Math:* pp. 377-378 A-U

Date: May 15/19

Part 1: The Graphs of  $y = a \sin x$  and  $y = a \cos x$ .

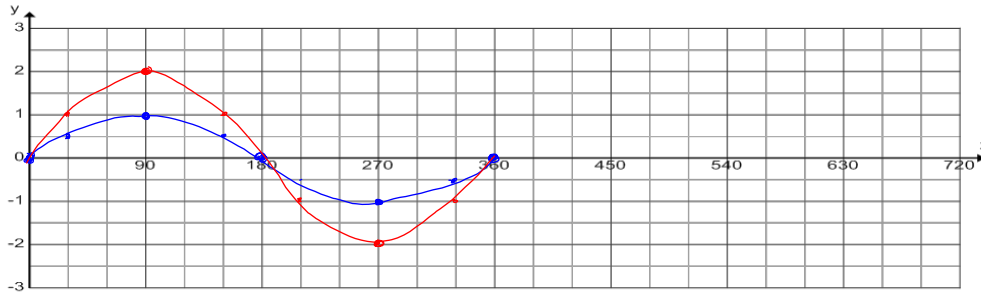
**Start with the 5 Key Points from the parent function.**

You may choose to add a few more for accuracy.

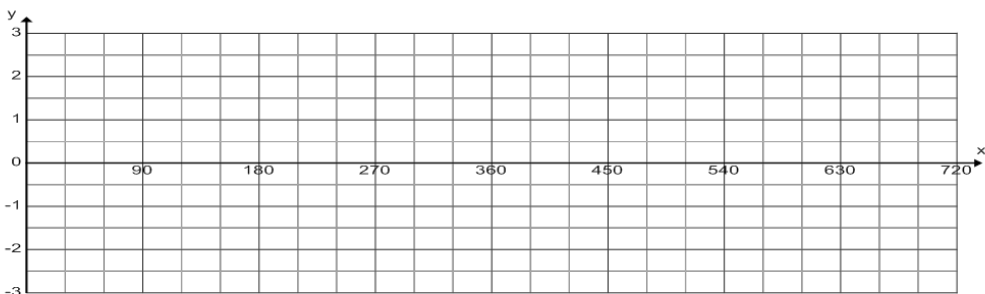
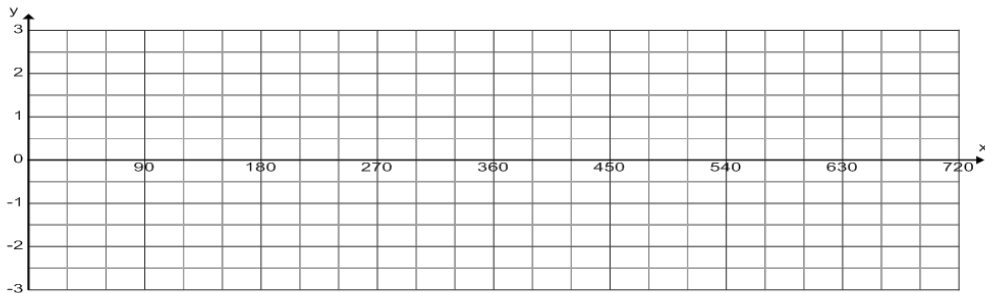
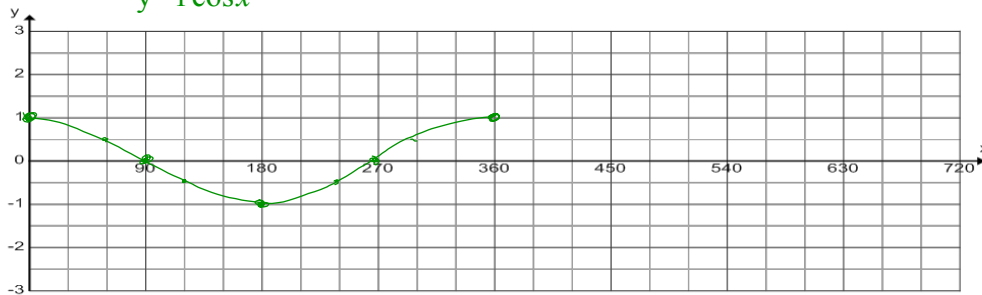
Note: Only 1 complete cycle is required.

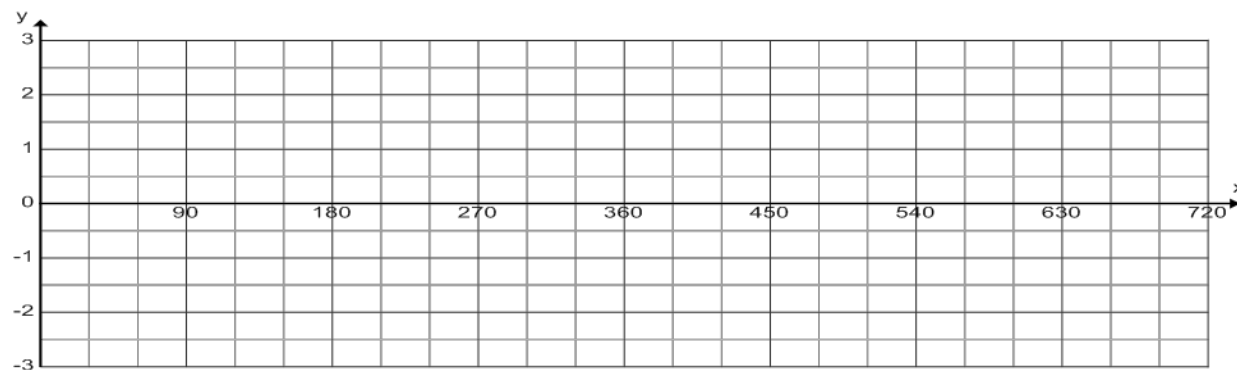
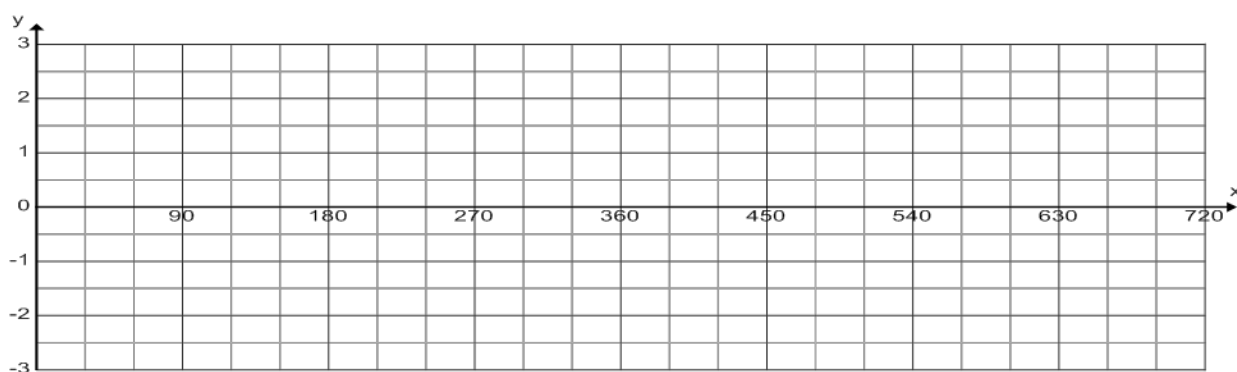
$y = 1 \sin x$

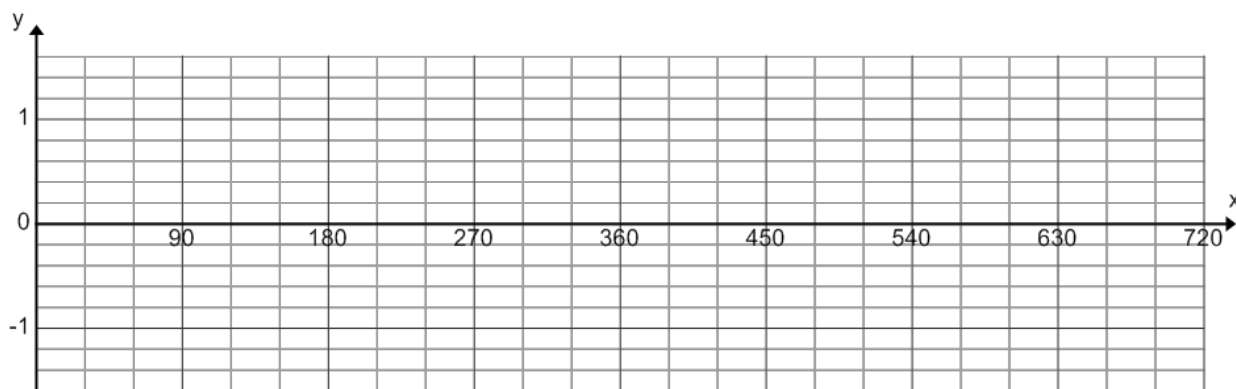
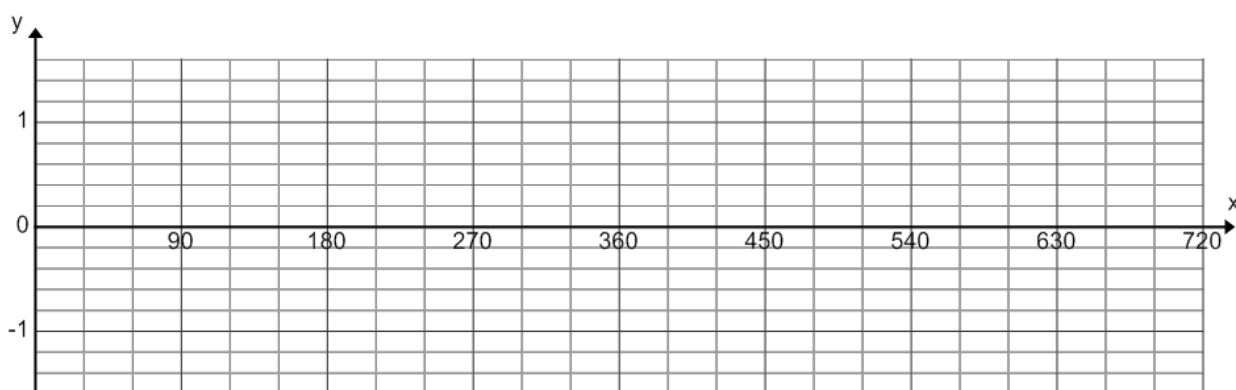
$y = 2 \sin x$



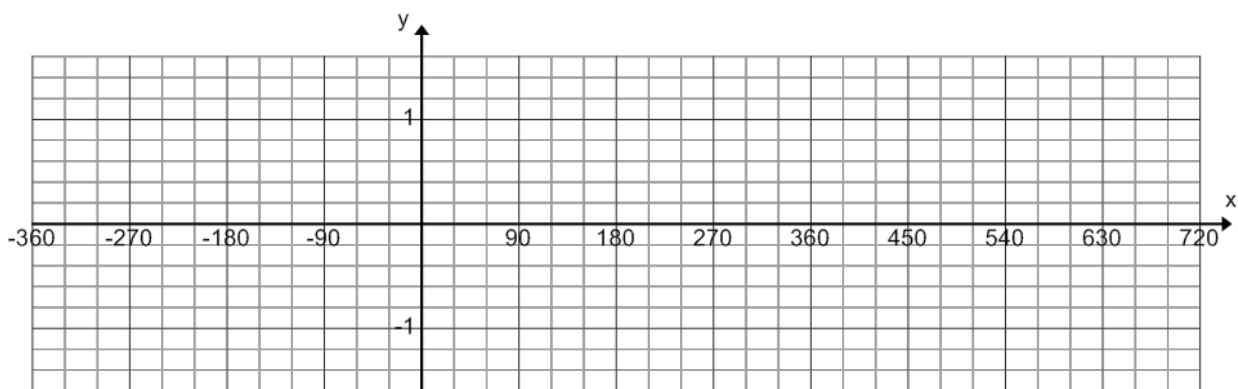
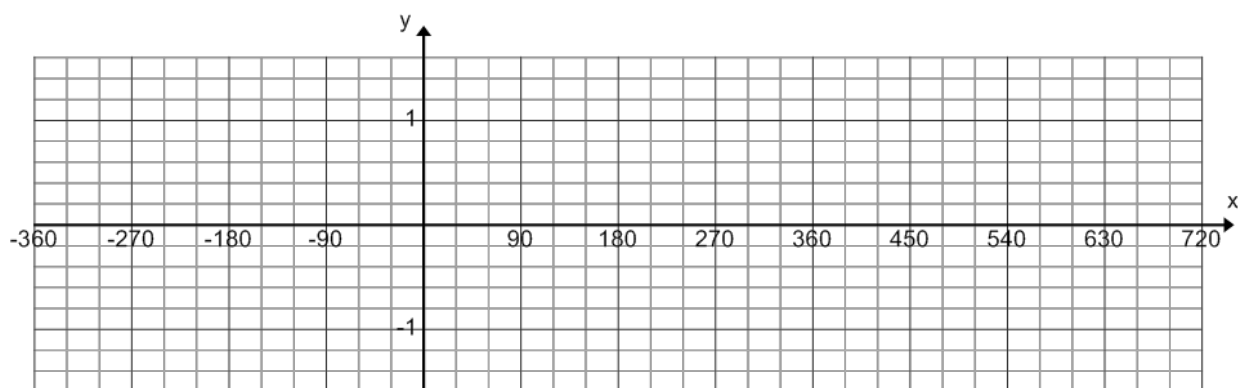
$y = 1 \cos x$



Part 2: The Graphs of  $y = \sin x + c$  and  $y = \cos x + c$ .

Part 3: The Graphs of  $y = \sin kx$  and  $y = \cos kx$ .

Part 4: The Graphs of  $y = \sin(x - d)$  and  $y = \cos(x - d)$ .



Summary of  $y = a \sin(k(x-d)) + c$  and  $y = a \cos(k(x-d)) + c$

The transformations that have occurred to  $y = \sin x$  and  $y = \cos x$  are:



**Are there any Homework Questions you would like to see on the board?**

Last day's work: pp. 363-364 #1 – 4, 8, 9 [15,16]  
pp. 370-372 #1 – 8, 13 [15]

Today's Homework Practice includes:

pp. 377-378 A – U

p. 379 #1 – 3

6.2 SineTracer.gsp