Before we begin, are there any questions from last day's work?
Worksheet 1.1.3 Matching Activity
Worksheet 1.1.4 = pp.370-372 #1, 2, 5, 6, 12

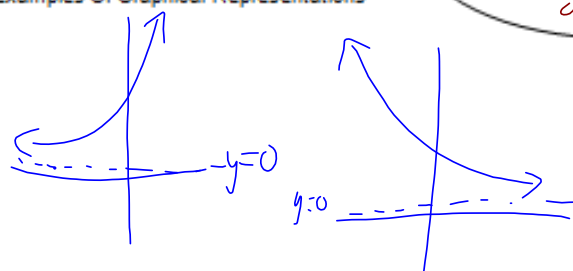# Today's Learning Goal(s):

By the end of the class, I will be able to:

a) solve simple exponential equations numerically and graphically, with technolog

b) connect algebraic and graphical representations of exponential equations.

Day 1: We will work through "Mystery 1" and "Mystery 2".

Day 2: We will work through "Mystery 3" and "Mystery 4".

1.2.1: Frayer Model – Exponential *Functions*

Date: _Sept. 5/19_

Examples Of Algebraic Representations	Characteristics

Examples Of Algebraic Representations

$$y = 2^x \qquad y = \left(\frac{1}{3}\right)^x \qquad y = 10^{-x}$$

Non-Examples Of Algebraic Representations

$$y = 3x - 7 \quad \Big| \quad y = 8 \quad \Big| \quad y = \sqrt{x}$$
$$y = x^2$$

Characteristics

The variable $^{(x)}$ MUST be in the exponent.

The base must be $0 < b < 1$ or $b > 1$

∴ $b \neq 1$ or line $y = 1$

Exponential *Functions*

$$y = b^x$$

Examples Of Graphical Representations

$y = 0$

Non-Examples Of Graphical Representations

1.2.2: Can You Solve This Mystery?

Date: ___Sept. 5/19___

Recall:"To solve an equation" means to determine the value of the variable that makes the equation true.

MYSTERY #1 – How can you solve exponential equations?

1. Solve these exponential equations. Match the solution with the equation.

Equation	Solution
C 1. $2^x = 8$	A. $x = -2$
D 2. $2^x = 16$	B. $x = 0$
A 3. $2^x = \dfrac{1}{4}$	C. $x = 3$
B 4. $2^x = 1$	D. $x = 4$

2. Describe the process that you used to solve the equations above.

☞ trial and error
☞ inspection
☞ substitution

3. Solve $2^x = 5$. Round your answer to the nearest hundredth.

☞ $x \doteq 2.32$

x	$y = 2^x$
2.5	5.65
2.3	4.92
2.35	5.09

4. Use **desmos** to graph the function $y = 2^x$, using the settings below.

☑ X-Axis
$-3 \le x \le 5$

☑ Y-Axis
$-2 \le y \le 20$

5. Complete the following statements.

a) The value of the function is 16 when $x =$ ___4___ ☞

b) The value of the function is $\dfrac{1}{4}$ when $x =$ ___-2___ ☞

c) The value of the function is 8 when $x =$ ___3___ ☞

d) The value of the function is 5 when $x =$ ___2.32___ ☞ (round your answer to two decimal places)

6. Explain how to use the graph of the function $y = 2^x$ to solve the equations in #1.

☞

7. Explain why you **can not** use the graph of the function $y = 2^x$ to solve the equation $2^{2x-3} = 8$ but you **can** use $y = 2^x$ to solve the equation $2^x = 8$.

☞ As you "trace" along y=2^x, you are getting values of x, not 2x-3.
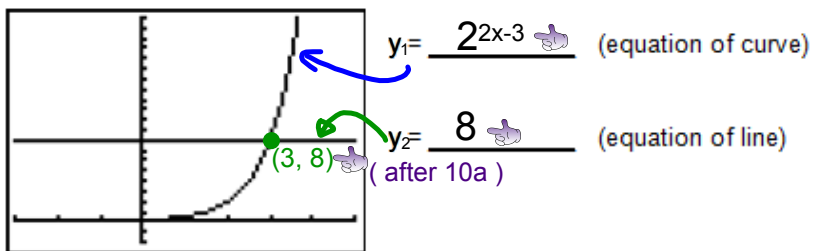☞ Also, y=2^x does not represent y=2^{2x-3}.

MYSTERY #2 – How can you solve more difficult exponential equations?

8. Fear not! There is a way to solve the equation $2^{2x-3} = 8$.

   Enter the left side of the equation as one function and the right side of the equation as another function.

   $$y = 2^{2x-3}$$

   $$y = 8$$

9. Label the functions as $y = 2^{2x-3}$ and $y = 8$ on the screen shot below.

   $y_1 = $ ___2^{2x-3}___ 👉 (equation of curve)

   $y_2 = $ ___8___ 👉 (equation of line)

   (3, 8) 👉 (after 10a)

10. Find the point of intersection of the two functions and complete the following statements. 👉(for all)

a) The point of intersection occurs when $x = $ __3__ and $y = $ __8__.

   The solution to the equation is $x = $ __3__.

   When $x = $ __3__, both functions have a value of __8__.

Day 2: We will work through "Mystery 3" and "Mystery 4".

MYSTERY #3

11. Use **desmos** and the "Intersection Method" to solve the following equations. Record the solution.

Equation	Y_1	Y_2	Solution to Equation
a) $2^{2x-3} = 8$	$Y_1 = 2^{2x-3}$	$Y_2 = 8$	$x =$
b) $2^{2x-3} - 6 = 2$			
c) $2^{2x-3} + 5 = 13$			

12. Solve the mystery...Why are all of the solutions to these equations the same?

MYSTERY #4

13. True or false (check one)? "The solution to any exponential equation is always an exact value."
☐ true   or   ☐ false   Justify your choice.

14. Use trial and error on your calculator to determine the solution to the following equations. Compare your solution using the "Intersection Method".
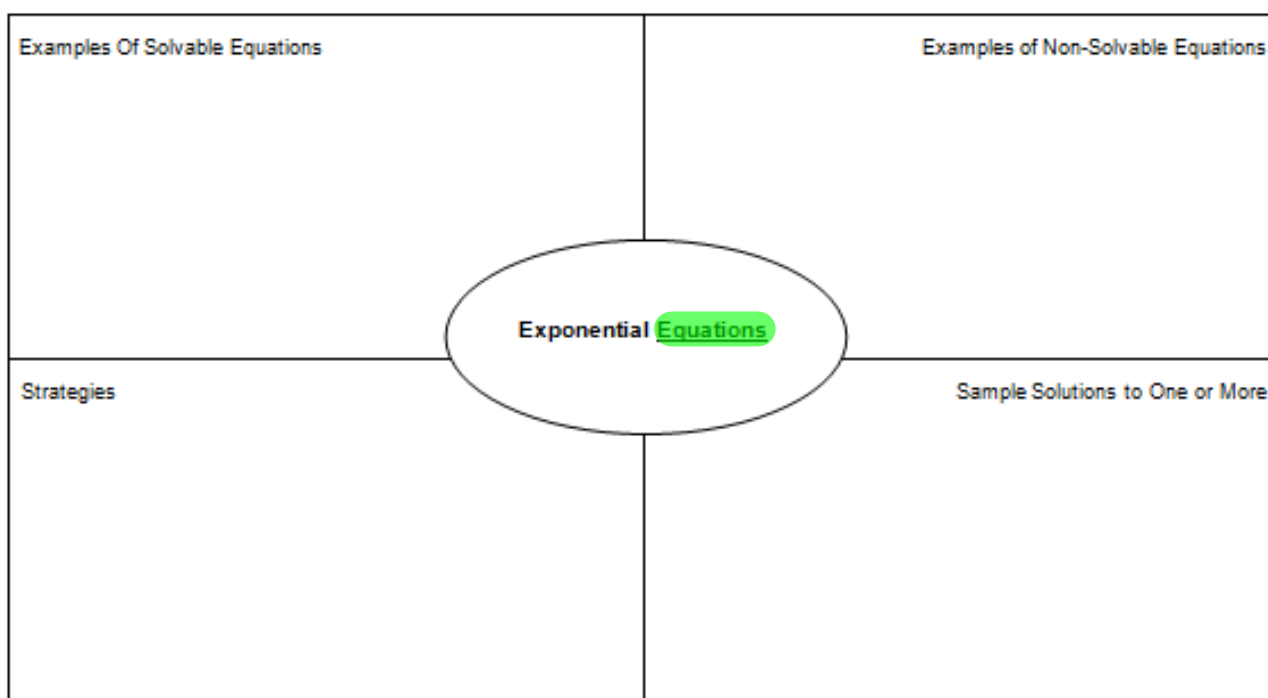
Equation	Solution Using Trial And Error On *Your* Calculator (2 decimal places)	Solution Using The Intersection Method (3 decimal places)
a) $3.05^x = 15$	$x =$	$x =$
b) $2.3^x = 6$	$x =$	$x =$
c) $4.2^{-x} = 7$	$x =$	$x =$
d) $2.7^x = 38$	$x =$	$x =$

15. Make an exponential equation, with base 5, where the solution is

a) an exact value	b) 0.75
c) a negative integer	d) an irrational number (not exact)

1.2.3: Frayer Model – Exponential Equations

Date: _____

Examples Of Solvable Equations	Examples of Non-Solvable Equations

Exponential Equations

Strategies	Sample Solutions to One or More

Review the learning goals. Were we successful today?
Homework: Worksheet 1.2.4

Answer any remaining homework questions
Students ask for "at desk" clarification.

1.2.4: Further Mysteries to Ponder   Date: _____

1. Using only a regular calculator, use trial and error to determine the solution to the equation $1.05^x = 1276$ (to 3 decimal places).

2. Explain why $5^x = -2$ has <u>no</u> solution, but $2^x - 5 = -2$ has a solution. Provide graphical and algebraic support.

3. Is it possible to create an exponential equation that has more than one solution? Provide graphical and algebraic support.

4. Compare and contrast the solutions in group A with those in group B.

Group A	Group B
$2^{-x} = 8$	$2^x = 8$
$2^{-x} = 1$	$2^x = 1$
$2^{-x} = \dfrac{1}{4}$	$2^x = \dfrac{1}{4}$
$2^{-x} = 16$	$2^x = 16$