

Before we begin, are there any questions from last day's work?

pp. 329-331 # 7, 11, 2, 4, 5

Extra Practice p.330 # 9, 10

Today's Learning Goal(s):

By the end of the class, I will be able to:

- a) use the exponent laws to simplify and evaluate expression
- b) solve exponential equations by using common bases.

1.5.1: Simplifying and Evaluating Expressions Using the Laws of Exponents

Date: Sept. 11/19

Ex. 1 Evaluate without using a calculator. [You must use the laws of exponents]

a) 3^{-2} b) $\left(\frac{1}{4}\right)^{-2}$ c) $\frac{1}{4^{-2}}$ d) $\left(\frac{3}{4}\right)^{-2}$ e) $\left(-\frac{2}{5}\right)^{-3}$ f) $\left(\frac{81}{16}\right)^{\frac{1}{2}}$ g) $27^{\frac{2}{3}}$ h) $64^{\frac{4}{3}}$ i) $\left(\frac{16}{81}\right)^{\frac{1}{4}}$

$= \left(\frac{1}{3}\right)^2 = \left(\frac{4}{1}\right)^2 = \left(\frac{4}{1}\right)^2 = \left(\frac{4}{3}\right)^2 = \left(\frac{-5}{2}\right)^3 = \frac{\sqrt{81}}{\sqrt{16}} = (27^{\frac{1}{3}})^2 = (\sqrt[3]{64})^4 = \frac{\sqrt[4]{16}}{\sqrt[4]{81}}$
 $= \frac{1^2}{3^2} = 4^2 = 4^2 = \frac{4^2}{3^2} = \frac{(-5)^3}{2^3} = \frac{\sqrt{81}}{\sqrt{16}} = (27^{\frac{1}{3}})^2 = (\sqrt[3]{64})^4 = \frac{\sqrt[4]{16}}{\sqrt[4]{81}}$
 $= \frac{1}{9} = 16 = 16 = \frac{16}{9} = \frac{(-125)}{8} = \frac{9}{4} = (3)^2 = 256 = \frac{2}{3}$
 $= \frac{1}{9} = 16 = 16 = \frac{16}{9} = \frac{(-125)}{8} = \frac{9}{4} = (3)^2 = 256 = \frac{2}{3}$

Ex. 2 Simplify using the laws of exponents.

a) $\sqrt{x^6 y^{12}}$ b) $x^2 \div x^{\frac{3}{2}}$ c) $\left(x^{\frac{2}{5}}\right)^{\frac{5}{8}}$

$= (x^6 y^{12})^{\frac{1}{2}}$
 $= (x^6)^{\frac{1}{2}} (y^{12})^{\frac{1}{2}}$
 $= x^3 y^6$

$= x^{2 - \frac{3}{2}}$
 $= x^{\frac{4}{2} - \frac{3}{2}}$
 $= x^{\frac{1}{2}}$
 $= \sqrt{x}$

$= x^{\frac{2}{5} \times \frac{5}{8}}$
 $= x^{\frac{1}{4}}$ or $\sqrt[4]{x}$

d) $\sqrt{81x^{16}y^{100}}(2x^{-4}y^3)^2$

$= \sqrt{81}(x^{16})^{\frac{1}{2}}(y^{100})^{\frac{1}{2}}(2)^2(x^{-4})^2(y^3)^2$
 $= 9x^8y^{50} \cdot 4x^{-8}y^6$
 $= 36x^{8+(-8)}y^{50+6}$
 $= 36y^{56}$

$$\begin{array}{l|ll} b^x \cdot b^y & b^x \div b^y & (b^x)^y & b^0 \\ = b^{x+y} & = b^{x-y} & = b^{xy} & = 1 \end{array}$$

$$\begin{aligned} & 9^2 \cdot 9^3 \\ &= 9^{2+3} \\ &= 9^5 \end{aligned}$$

$$\begin{aligned} & 9^8 \div 9^2 \\ &= 9^{8-2} \\ &= 9^6 \end{aligned}$$

$$\begin{aligned} & (9^3)^2 \\ &= 9^6 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{4^{-2}} \\
 = & \frac{1}{\left(\frac{1}{4}\right)^2} \\
 = & \frac{1}{\frac{1}{16}}
 \end{aligned}
 \quad \rightarrow \quad
 \begin{aligned}
 & = 1 \div \frac{1}{16} \\
 & = 1 \times \frac{16}{1} \\
 & = 16
 \end{aligned}
 \quad \left. \vphantom{\begin{aligned} & \frac{1}{4^{-2}} \\ & = 4^2 \end{aligned}} \right\}
 \begin{aligned}
 & \frac{1}{4^{-2}} \\
 & = 4^2
 \end{aligned}
 \quad \frac{1}{a^3}$$

$$\begin{array}{r}
 \begin{array}{cccc}
 -3 & 4 & -5 & \\
 a & b & c & \\
 \hline
 d^{6-7} & f^8 & & \\
 d^1 & f^8 & & \\
 b^4 & e^7 & & \\
 \hline
 d^6 & f^8 & a^3 & c^5
 \end{array}
 \end{array}$$

$$\frac{-20}{4}$$

$$= -5$$

$$\frac{20}{-4}$$

$$= -5$$

$$-\frac{20}{4}$$

$$= -5$$

$$-\frac{3}{4}x$$

$$\frac{3}{-4}x$$

$$-\frac{3}{4}x$$

$$\frac{-3}{-4}x$$

Ex. 3

a) Simplify $\frac{a^3 b^2 c^3}{\sqrt{a^2 b^4}}$, and then evaluate for $a=4$, $b=9$, and $c=-3$.

b) Verify your answer by evaluating the expression *without* simplifying first.

$$\begin{aligned}
 &= \frac{a^3 b^2 c^3}{(a^2 b^4)^{\frac{1}{2}}} \\
 &= \frac{a^3 b^2 c^3}{(a^{\frac{2}{2}} b^{\frac{4}{2}})^{\frac{1}{2}}} \\
 &= \frac{a^3 b^2 c^3}{a^1 b^2} \\
 &= a^{3-1} b^{2-2} c^3 \\
 &= a^2 b^0 c^3 \\
 &= a^2 (1) c^3 \\
 &= a^2 c^3 \text{ Simplified} \\
 &= (4)^2 (-3)^3 \\
 &= 16(-27) \\
 &= -432
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{(4)^3 (9)^2 (-3)^3}{\sqrt{(4)^2 (9)^4}} \\
 &= \frac{64(81)(-27)}{\sqrt{16(6561)}} \\
 &= \frac{-139968}{\sqrt{104976}} \\
 &= \frac{-139968}{324} \\
 &= -432
 \end{aligned}$$

1.5.2: Solving Exponential Equations Using Common Bases

Date: Sept. 11/19

Ex. 1 Solve each exponential equation by determining a common base.

a) $2^x = 32$

$$2^x = 2^5$$

$$\therefore x = 5$$

b) $3^{5x+8} = 27^x$

$$3^{5x+8} = (3^3)^x$$

$$3^{5x+8} = 3^{3x}$$

$$\therefore 5x+8 = 3x$$

$$5x - 3x = -8$$

$$2x = -8$$

$$x = \frac{-8}{2}$$

$$x = -4$$

c) $3^{2x+5} = 27^{4x}$

$$3^{2x+5} = (3^3)^{4x}$$

$$3^{2x+5} = 3^{12x}$$

$$\therefore 2x+5 = 12x$$

$$2x - 12x = -5$$

$$-10x = -5$$

$$x = \frac{-5}{-10}$$

$$x = \frac{1}{2}$$

d) $4^{5x-1} = 2^{2(x+11)}$ **

$$(2^2)^{5x-1} = 2^{2x+22}$$

$$2^{10x-2} = 2^{2x+22}$$

$$\therefore 10x-2 = 2x+22$$

$$10x - 2x = 22 + 2$$

$$8x = 24$$

$$x = 3$$

e) $4^{3x} = 8^{x+1}$

$$(2^2)^{3x} = (2^3)^{x+1}$$

$$2^{6x} = 2^{3x+3}$$

$$\therefore 6x = 3x+3$$

$$6x - 3x = 3$$

$$3x = 3$$

$$\therefore x = 1$$

f) $3(2^{x-1}) = 96$

$$\frac{3(2^{x-1})}{3} = \frac{96}{3}$$

$$2^{x-1} = 32$$

$$2^{x-1} = 2^5$$

$$\therefore x-1 = 5$$

$$x = 6$$

g) $5(3^{x+3}) = 405$

$$3^{x+3} = \frac{405}{5}$$

$$3^{x+3} = 81$$

$$3^{x+3} = 3^4$$

$$\therefore x+3 = 4$$

$$x = 1$$

h) $\sqrt{2} = 4^{x+1}$

$$2^{\frac{1}{2}} = (2^2)^{x+1}$$

$$2^{\frac{1}{2}} = 2^{2x+2}$$

$$\therefore \frac{1}{2} = 2x+2$$

$$\frac{1}{2} - 2 = 2x$$

$$\frac{1}{2} - \frac{4}{2} = 2x$$

$$-\frac{3}{2} = 2x$$

$$-\frac{3}{4} = x$$

i) How could you check your solutions using graphing technology?

Answer: Use the intersection method; i.e. $y_1 = 2^x$, $y_2 = 32$ 

Review the learning goals. Were we successful today?

Homework: p.387 #1, 2a, 3a, 5, 6
Worksheet 1.5.3

Answer any remaining homework questions
Students ask for "at desk" clarification.

1.5.3 Solving Exponential Equations Using Common Bases

Date: _____

1. Solve each exponential equation by determining a common base.

a) $2^x = 64$

b) $5^{2x+6} = 125$

c) $5^x = \frac{1}{25}$

d) $4^x = \frac{1}{8}$

2. Simplify.

a) $\frac{27^3 \times 9^{-2}}{81}$

b) $\frac{25^{m+3n}}{125^{2m+1}}$

3. Solve.

a) $3(2^x) = 48$

b) $4(7^{2x-1}) = 28$

c) $9^{x+1} = 27^{3x-4}$

d) $2^{2x+4} - 5 = 59$

4. Solve.

a) $2^{x^2+5x} = 64$

b) $(3^{x-3})^x = \frac{1}{9}$

c) $3^{3x+1} = 27(9^x)$

d) $(2^{x+2})(4^{x-1})(8^{2x-3}) = 256^x$

Answers

1a) 6

b) $\frac{-3}{2}$

c) -2

d) $\frac{-3}{2}$

2a) 3

b) $5^{6n-4m-3}$

3a) 4

b) 1

c) 2

d) 1

4a) -6 or 1

b) 2 or 1

c) 2

d) 9