

Are there any questions from last day's assigned work you would like to see on the board?

Last day's work: pp. 186-188 # 1 – 15 (All Multiple Choice)

Note: p. 184 5a,b are on the next screens

Today's Learning Goal(s):

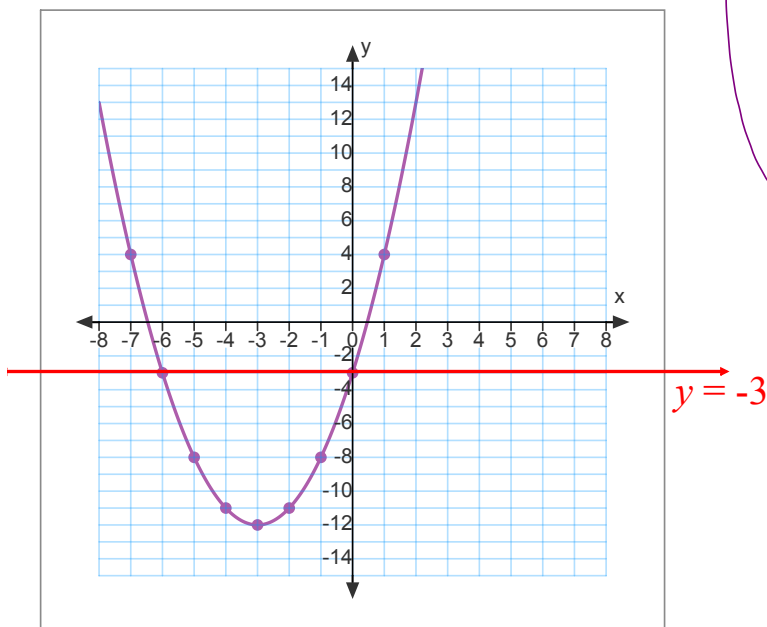
By the end of the class, I will be able to:

- a) Compare the standard and vertex forms of a quadratic function.

p. 184 5. Solve by graphing.

a) $x^2 + 6x - 3 = -3$

$y = -3$

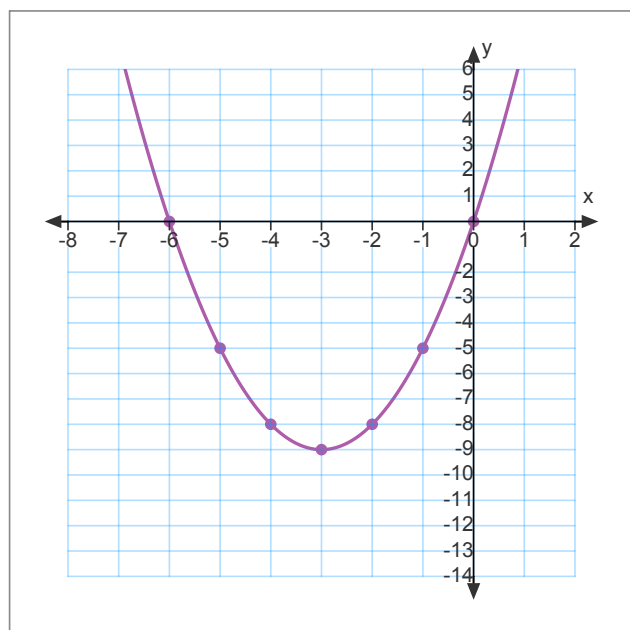


$y = x^2 + 6x$

 \therefore the solutions are $x = -6$ and $x = 0$

$y = -3$

$x^2 + 6x - 3 = -3$



$y = -3$

$x^2 + 6x - 3 + 3 = 0$

$x^2 + 6x = 0$

$\therefore y = x^2 + 6x$

$$\begin{aligned} \text{Ans: } x &= \frac{-b}{2a} \\ &= \frac{-(6)}{2(1)} \\ &= -3 \end{aligned} \quad \left. \begin{array}{l} \text{if } x = -3 \\ y = (-3)^2 + 6(-3) \\ = 9 - 18 \\ = -9 \end{array} \right\} \therefore \sqrt{(-3, -9)}$$

 \therefore the solutions are $x = -6$ and $x = 0$

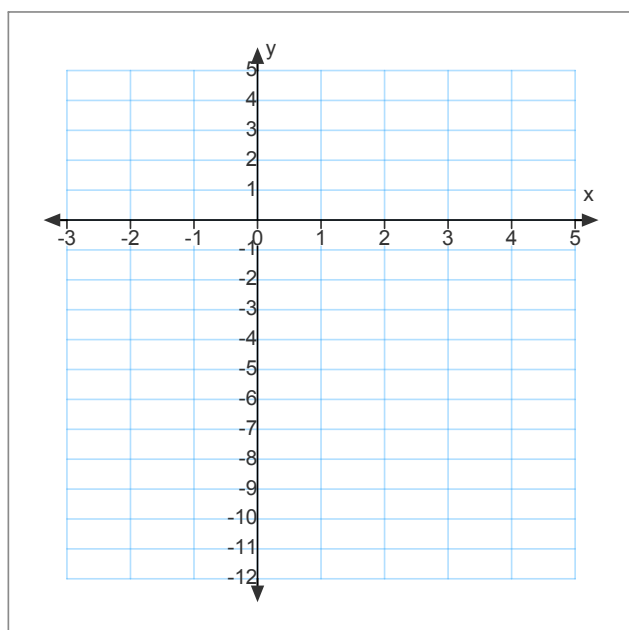
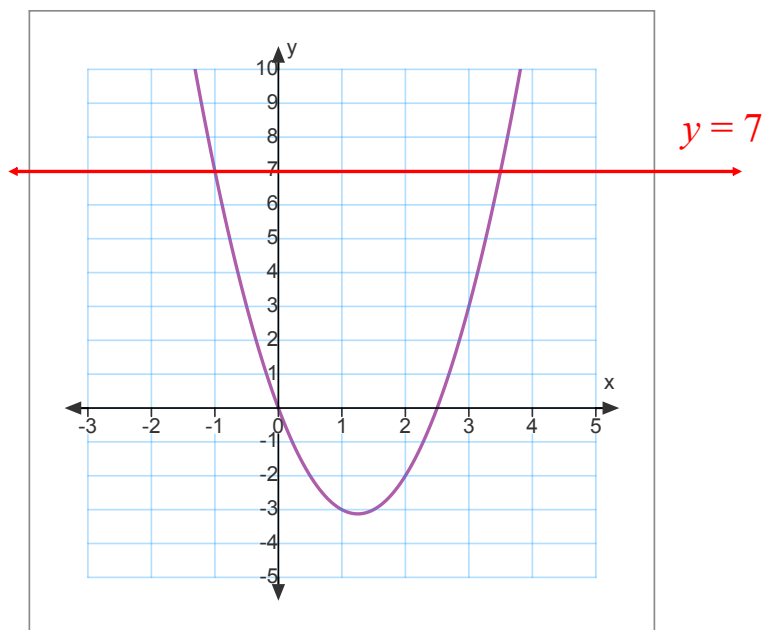
p. 184 5. Solve by graphing.

b) $2x^2 - 5x = 7$

$y = 7$

$y = 2x^2 - 5x$

$= x(2x - 5)$



$y = 2x^2 - 5x - 7$

$$\begin{aligned}
 \text{Ans: } x &= \frac{-b}{2a} \\
 &= \frac{-(-5)}{2(2)} \\
 &= \frac{5}{4} \\
 &= 1.25
 \end{aligned}$$

MCF 3MI 4.1 The Vertex Form of a Quadratic Function

Date: Oct. 21/19

VERTEX FORM

$$f(x) = a(x-h)^2 + k \quad v(h, k)$$

vs.

STANDARD FORM

$$f(x) = ax^2 + bx + c$$

$$g(w) = -(w-15)^2 + 225 \quad (\text{Show by expanding})$$

$$f(w) = -w^2 + 30w$$

We are able to obtain "standard form" by expanding the vertex form.

$$\begin{aligned} g(w) &= -(w-15)(w-15) + 225 \\ &= -(w^2 - 30w + 225) + 225 \\ &= -w^2 + 30w - 225 + 225 \\ &= -w^2 + 30w \end{aligned}$$

(use the back of the handout)

Ex. 1: Given $f(x) = 3(x+4)^2 - 8$, determine the:

f) sketch of the graph (no technology)

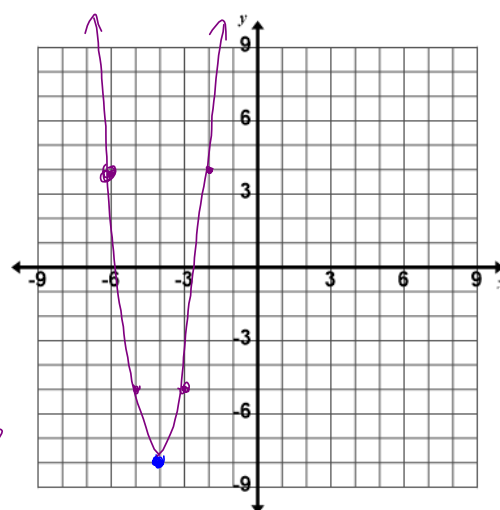
a) direction of opening upwardsb) equation of the axis of symmetry $x = -4$ c) ~~max~~ min value -8 d) vertex $(-4, -8)$

e) State the Domain and Range

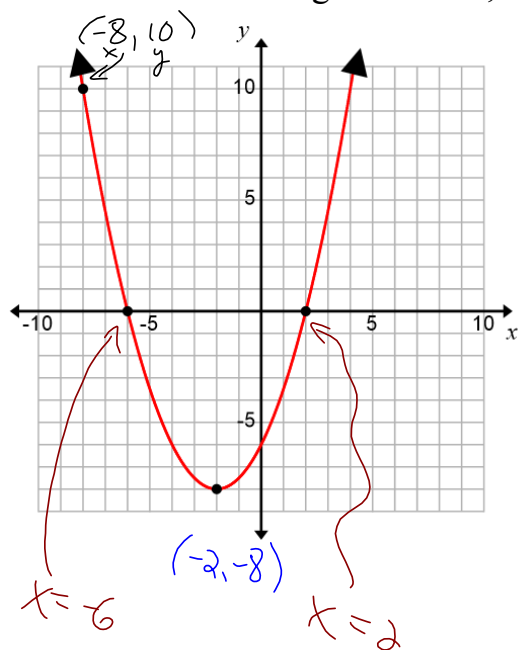
D: $\{x \in \mathbb{R}\}$

R: $\{y \in \mathbb{R} \mid y \geq -8\}$

$$\begin{aligned} \text{MG } a=3 \\ 1 &\rightarrow 3 \\ 2 &\rightarrow 12 \\ 3 &\rightarrow 27 \end{aligned}$$



Ex. 2: Given the diagram below, write the quadratic function in each of the 3 forms.



Vertex Form

$$y = a(x-h)^2 + k$$

$$y = a(x+2)^2 - 8$$

$$10 = a(-8+2)^2 - 8$$

$$10 = a(-6)^2 - 8$$

$$10 = 36a - 8$$

$$10 + 8 = 36a$$

$$18 = 36a$$

$$\frac{18}{36} = a$$

$$\frac{1}{2} = a$$

$\therefore y = \frac{1}{2}(x+2)^2 - 8$
is the equation
in vertex form

Factored Form

$$y = a(x-r)(x-s)$$

$$y = a(x+6)(x-2)$$

$$10 = a(-8+6)(-8-2)$$

$$10 = a(-2)(-10)$$

$$10 = 20a$$

$$\frac{10}{20} = a$$

$$\frac{1}{2} = a$$

$\therefore y = \frac{1}{2}(x+6)(x-2)$
is the equation in
factored form

Standard Form

$$\begin{aligned} y &= \frac{1}{2}(x+6)(x-2) \\ &= \frac{1}{2}(x^2 - 2x + 6x - 12) \\ &= \frac{1}{2}(x^2 + 4x - 12) \\ &= \frac{1}{2}x^2 + 2x - 6 \end{aligned}$$

Ex. 3: What information about the parabola does each form provide?

Standard Form

$$f(x) = ax^2 + bx + c$$

c is the
y-intercept

Factored Form

$$f(x) = a(x-r)(x-s)$$

x-intercepts
 $x=r$ or $x=s$

Vertex Form

$$f(x) = a(x-h)^2 + k$$

vertex (h, k)

Ex. 4: Write the equation of the quadratic function,
first in **vertex form** and then in **standard form**,
given vertex $(-6, 7)$ and passing through $(2, -9)$.

$$y = a(x+6)^2 + 7$$

$$-9 = a(2+6)^2 + 7$$

$$-9 = a(8)^2 + 7$$

$$-9 - 7 = 64a$$

$$-16 = 64a$$

$$-\frac{16}{64} = a$$

$$a = -\frac{1}{4}$$

$$\therefore y = -\frac{1}{4}(x+6)^2 + 7$$

is the equation in vertex form.

(x, y)

$$\begin{aligned} y &= -\frac{1}{4}(x+6)^2 + 7 \\ &= -\frac{1}{4}(x^2 + 12x + 36) + 7 \\ &= -\frac{1}{4}x^2 - 3x - 9 + 7 \\ &= -\frac{1}{4}x^2 - 3x - 2 \end{aligned}$$

is the equation in standard form.

Be prepared for tomorrow's Unit 3 Summative!!

Today's Assigned Practice:

READ pp. 196 – 203

pp. 203-205 # 1 – 4, 6, 8 – 10