

Are there any questions from last day's assigned work you would like to see on the board?

pp. 232-233 # 1ac, 2abc, 5, 7, 8a, 11

Work ahead on Mid-chapter Review: p. 226 # 8 – 11

Today's Learning Goal(s):

By the end of the class, I will be able to:

- Complete the square to obtain the vertex form of a quadratic function.
- Complete the square with functions that involve fractional values.

If time, Return and Correct Unit 3 Summative

p. 232 2. Determine the number of real solutions of each quadratic equation.

Do not solve.

a) $x^2 + 3x - 4 = 0$

b) $2x^2 - x + 5 = 0$

c) $4x^2 - 8x = 4x - 9$

$a=1$ $b=3$ $c=-4$ $a=2$ $b=-1$ $c=5$

$b^2 - 4ac$

$b^2 - 4ac$

$-(3)^2 - 4(1)(-4)$ $= (-1)^2 - 4(2)(5)$

$= 9 + 16$

$= 1 - 40$

$= 25$

$= -39$

$\therefore b^2 - 4ac > 0$

$\therefore b^2 - 4ac < 0$

$\therefore 2 \text{ Real}$

$\therefore \text{No Real Solutions}$

distinct solutions

- p. 232 5. For what value(s) of k does the function $f(x) = kx^2 - 8x + k$ have no zeros? $a=k$ $b=-8$ $c=k$

$$b^2 - 4ac < 0$$

$$(-8)^2 - 4(k)(k) < 0$$

$$64 - 4k^2 < 0$$

↪ Not Required in this course.

7. For what value of k does $8x^2 + 4x + k = 0$ have two distinct real solutions? one solution? no solution? $a=8$ $b=4$ $c=k$

$$b^2 - 4ac > 0$$

$$(4)^2 - 4(8)(k) > 0$$

$$16 - 32k > 0$$

$$-32k > -16$$

$$k < \frac{-16}{-32}$$

$$k < \frac{1}{2}$$

$$b^2 - 4ac = 0$$

$$(4)^2 - 4(8)(k) = 0$$

$$b^2 - 4ac < 0$$

$$(4)^2 - 4(8)(k) < 0$$

$$16 - 32k < 0$$

$$-32k < -16$$

$$k > \frac{-16}{-32}$$

$$k > \frac{1}{2}$$

8. a) Explain how you would solve this problem: For what value of k does the function $f(x) = 3x^2 - 5x + k$ have only one zero?
b) Use your strategy to find the value of k .

MCF 3MI

4.2 Relating the Standard and Vertex Forms
(by Completing the Square)

$$y = a(x-h)^2 + k$$

Date: Oct. 28/19

STANDARD FORM

$$y = -8x^2 + 80x + 7$$

vs.

$$\left(\frac{1}{2}b\right)^2$$

VERTEX FORM

$$y = -8(x-5)^2 + 207$$

We are able to obtain "vertex form" by completing the square.

$$\begin{aligned} y &= -8x^2 + 80x + 7 \\ &= -8(x^2 - 10x) + 7 \\ &= -8(x^2 - 10x + 5^2 - 5^2) + 7 \\ &= -8(x-5)^2 - 8(-25) + 7 \\ &= -8(x-5)^2 + 200 + 7 \\ &= -8(x-5)^2 + 207 \end{aligned}$$

$$\begin{aligned} &(x-5)^2 \\ &(x-5)(x-5) \\ &= x^2 - 5x - 5x + 25 \\ &= x^2 - 10x + 25 \end{aligned}$$

Ex. 1 Write each quadratic function in vertex form by completing the square.

a) $y = x^2 + 8x + 10$

$$\begin{aligned} &= x^2 + 8x + 16 - 16 + 10 \\ &= (x+4)^2 - 6 \end{aligned}$$

b) $f(x) = -4x^2 + 24x + 5$

$$\begin{aligned} &= -4(x^2 - 6x) + 5 \\ &= -4(x^2 - 6x + 9 - 9) + 5 \\ &= -4(x-3)^2 - 4(-9) + 5 \\ &= -4(x-3)^2 + 36 + 5 \\ &= -4(x-3)^2 + 41 \end{aligned}$$

Ex. 2 Write $y = 2x^2 - 3x - 4$ in vertex form.

$$\begin{aligned} y &= 2(x^2 - \frac{3}{2}x) - 4 \\ &= 2(x^2 - \frac{3}{2}x + (\frac{3}{4})^2 - (\frac{3}{4})^2) - 4 \\ &= 2(x - \frac{3}{4})^2 + 2(-\frac{9}{16}) - 4 \\ &= 2(x - \frac{3}{4})^2 - \frac{9}{8} - \frac{32}{8} \\ &= 2(x - \frac{3}{4})^2 - \frac{41}{8} \end{aligned}$$

$$\begin{aligned} \frac{1}{2}(\frac{3}{2}) \\ &= \frac{3}{4} \\ 0.5(1.5) \\ &= 0.75 \end{aligned}$$

$$\begin{aligned} y &= 2(x^2 - 1.5x) - 4 \\ &= 2(x^2 - 1.5x + 0.75^2 - 0.75^2) - 4 \\ &= 2(x - 0.75)^2 + 2(-0.5625) - 4 \\ &= 2(x - 0.75)^2 - 1.125 - 4 \\ &= 2(x - 0.75)^2 - 5.125 \end{aligned}$$

Ex. 3 Judy wants to fence three sides of the yard in front of her house. She bought 100 m of fence and wants the maximum area she can fence in. The function $A(x) = 100x - 2x^2$ represents the area to be enclosed, where x is the width of the yard in metres.

a) Write the function in vertex form.

$$A(x) = 100x - 2x^2$$

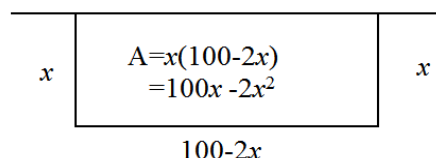
$$= -2x^2 + 100x$$

$$= -2(x^2 - 50x)$$

$$= -2(x^2 - 50x + 25^2 - 25^2)$$

$$= -2(x - 25)^2 - 2(-625)$$

$$= -2(x - 25)^2 + 1250$$



b) Determine the maximum area that can be enclosed.

\therefore the max. area is 1250 m^2

(and happens when $x = 25$)

If time, Return and Correct Unit 3 Summative

Today's Assigned Practice:

p. 232 # 2def, 4 **AND**

p. 194 # 6 **AND**

p. 214 # 4, 6a-e, 7a-e, 8 **AND**

READ p. 225 **AND**

Work ahead on Mid-chapter Review: p. 226 # 1 – 4

Today's Assigned Practice:

p. 232 # 2def, 4 **AND**

p.194 # 6 **AND**

p. 214 # 4, 6a-e, 7a-e, 8 **AND**

READ p. 225 **AND**

Work ahead on Mid-chapter Review: p. 226 # 1 – 4