## KEY CONCEPTS

- The degree of a polynomial function $f(x)=a_{n} x^{n}+a_{n-1} x^{n-1}+a_{n-2} x^{n-2}+\cdots+a_{2} x^{2}+a_{1} x+a_{0}$ determines the end behaviour as $x$ approaches positive infinity $(x \rightarrow \infty)$ and as $x$ approaches negative infinity $(x \rightarrow-\infty)$.
- The leading coefficient is the coefficient of the term that is used to determine the degree of a polynomial function. It may be a positive number or a negative number.
- A polynomial function may be an odd-degree polynomial or an even-degree polynomial, as shown in the chart.

|  | Odd-Degree Polynomial |  | Even-Degree Polynomial |  |
| :---: | :---: | :---: | :---: | :---: |
| Leading Coefficient | positive | negative | positive | negative |
| End Behaviour | $\begin{aligned} & \text { as } x \rightarrow-\infty, y \rightarrow-\infty \text {; } \\ & \text { as } x \rightarrow \infty, y \rightarrow \infty \\ & \text { (similar to the graph } \\ & \text { of } y=x \text { ) } \end{aligned}$ | $\begin{aligned} & \text { as } x \rightarrow-\infty, y \rightarrow \infty \\ & \text { as } x \rightarrow \infty, y \rightarrow-\infty \\ & \text { (similar to the } \\ & \text { graph of } y=-x \text { ) } \end{aligned}$ | $\begin{aligned} & \text { as } x \rightarrow-\infty, y \rightarrow \infty ; \\ & \text { as } x \rightarrow \infty, y \rightarrow \infty \\ & \text { (similar to the } \\ & \text { graph of } y=x^{2} \text { ) } \end{aligned}$ | $\begin{aligned} & \text { as } x \rightarrow-\infty, y \rightarrow-\infty ; \\ & \text { as } x \rightarrow \infty, y \rightarrow-\infty \\ & \text { (similar to the graph } \\ & \text { of } y=-x^{2} \text { ) } \end{aligned}$ |
| Sketch |  |  |  |  |
| Domain | $\{x \in \mathbb{R}\}$ |  | $\{x \in \mathbb{R}\}$ |  |
| Range | $\{y \in \mathbb{R}\}$ |  | $\{y \in \mathbb{R}, y \geq a\}$ | $\{y \in \mathbb{R}, y \leq a\}$ |
| Maximum/ Minimum Value | neither a maximum value nor a minimum value |  | minimum value is $a$ | maximum value is $a$ |

